RUDIMENTARY TREATISE

ON

SUBTERRANEOUS SURVEYING,

RANGING THE LINE WITHOUT THE MAGNET, &c.

BY

THOMAS FENWICK,

COAL VIEWER.

WITH

IMPROVEMENTS AND MODERN ADDITIONS,

BY T. BAKER, C.E.

15. 8. 623

A TREATISE

ON

SUBTERRANEOUS SURVEYING,

ETC. ETC. ETC.

ELEMENTARY AND PRACTICAL TREATISE

ON

SUBTERRANEOUS SURVEYING,

AND THE

MAGNETIC VARIATION OF THE NEEDLE.

By THOMAS FENWICK,

Colliery Viewer and Surveyor of Mines.

ALSO

THE METHOD OF CONDUCTING

SUBTERRANEOUS SURVEYS WITHOUT THE
USE OF THE MAGNETIC NEEDLE,

And other Modern Improvements.

By THOMAS BAKER, C.E.,

Author of "Railway Engineering," "Theodolite Surveying, Levelling," &c., in
Nesbit's "Surveying, Rudimentary, Land and Engineering Surveying, Statics
and Dynamics, Elements of Mechanism, Mensuration, Integration," in Weale's
Series, &c.

THE THIRD EDITION.

PREFACE.

THE mineral wealth of this kingdom had become of such great importance, about half a century ago, as to induce *Mr. T. Fenwick, of Dipton, in the County of Durham,* to compose a Treatise on Subterraneous Surveying (which forms the basis of the present Work) for the use and instruction of young men designed for the profession of mining agents and surveyors, usually called colliery viewers: much more, then, is such a treatise now necessary, as these mineral productions have, up to the present time, been more than quadrupled in value; and by the more general diffusion of mathematical, philosophical, and mechanical science, the working of mines has been conducted with greater skill and precision for the full development of their vast wealth.

The general use of the magnetic needle in subterraneous surveys has been found to be a great source of error, on account of ferruginous substances (which exist in almost all mines) attracting the needle, and causing it to give erroneous indications; whence, in general, old surveys are found to be extremely defective. Indeed, *Mr. Fenwick* himself was so sensible

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of this deficiency of the needle, that he proposed, in
the Second Edition of his Work, about forty years
ago, to dispense with its general use; though he still
proposed to use it, at the first departure, or com-
mencement of the survey, from the top to the bottom
of the shaft of the mine.

This Edition of the Work contains, in a small
compass, the essentials of Subterraneous Surveying
in all its branches, both with and without the use of
the magnetic needle; and to make it still more useful
to that class of men for whom it is chiefly intended
to convey information, there are added a great number
of explanatory figures and examples.

PART I. contains the method of surveying, with the
use of the magnetic needle, without attending to its
variation, as being more readily intelligible to begin-
ners; and the magnetic bearings being, at the same
time, at once adapted to the use of the Traverse
Tables. This part is arranged after *Mr. Fenwick's*
plan (whose method and examples are still retained),
in the following order:—

1. Geometrical problems.

2. Theorems, and the methods of conducting sub-
terraneous surveys.

3. Of determining the magnitude of angles.

4. Of determining bearings, and reducing angles
to the bearings which they form with the magnetic
meridian, with a rule and examples.

5. The method of reversing bearings.

6. Of reducing bearings to the angles they form with the magnetic meridian, with rules and examples; and the manner of finding the magnitude of the angle that two bearings form with each other.

7. The method of reducing bearings and distances to the northing or southing, and easting or westing, they contain, by the Traverse Table, with a rule and examples.

8. The manner of surveying subterraneous excavations with the form of the survey-book.

9. The method of taking back sights.

PART II.—In this part, which treats extensively on conducting subterraneous surveys, without the use of the magnetic needle, Mr. Fenwick's examples are in several cases retained, with full directions for adapting them to the new method (they being already adapted to the use of the Traverse Table), which will constitute a useful exercise for the student in transferring the angles from their magnetic bearings to the angles which one line makes with the preceding one, as taken by the theodolite. This part has the following arrangement:—

1. Mr. Fenwick's method of subterraneous surveying, without the use of the needle, except at the first departure or commencement of the survey.

2. Mr. Baker's method of commencing the survey by suspending two weights down the shaft in the direction

of the first headway, and marking the same direction on the surface; and afterwards conducting the survey with the theodolite, without the use of the needle.

3. Mr. Beauland's method of making the commencement of the survey by the help of a transit instrument, not using the needle, as in Baker's method.

4. Plotting and protracting surveys in various ways.

5. Of reducing the bearings and distances of a survey into one common bearing and distance, or any number of bearings and distances fewer than those that compose the survey, whether the angles be taken with the needle, or the theodolite independent of the needle.

6. The method of plotting on the surface in various ways.

7. The method of making the survey where the excavation inclines from the horizon.

8. A promiscuous collection of practical examples, some of which relate to tunnelling.

PART III. contains subterraneous surveys, under the necessary attention to the magnetic variation of the needle. As the magnetic meridian has been found to be in a state of variation from the true meridian for upwards of 300 years, and still continues to vary, therefore surveys made by the circumferentor, or any other instrument under magnetic influence, must vary accordingly as that meridian varies. For instance, suppose the bearing of any one known object to have

been taken from a given point by the magnetic meridian in the year 1700, and recorded; and if the bearing of the same object be now retaken by the magnetic meridian from the same given point, these two bearings will be found, on comparison, to differ about 14°, the magnetic meridian having in that time changed thus far in its direction (see table, p. 96). It is also well known to directors of mines that the plans of their excavations, on examination, are always found to be erroneous,—some even to a great extent. This frequently misleads the miner, adding expense to his subterraneous pursuits, and the cause of such errors originates through his inattention to the variation of the needle in the plotting from time to time of his surveys.

This part, therefore, shows the method of rectifying the bearings of old surveys, in order to connect them with those made by the scientifically correct method laid down in the second part of this work.

The third part is thus arranged :—

1. Axioms and observations.

2. The method of finding the true and invariable meridian.

3. To determine the variation of the needle of the circumferentor or other instrument used in surveying.

4. To reduce bearings taken by an instrument, the needle of which has any known variation, to bearings with the true meridian, with rules and examples.

5. To reduce bearings from one magnetic meridian to bearings with any other magnetic meridian, with rules and examples.

6. To find the kind of meridian by which a plan has been constructed, with rules and examples.

7. On planning surveys, and finding the magnitude of an error in plotting, caused by inattention to the magnetic variation, with examples.

8. On running bearings on the surface by the circumferentor or theodolite without error.

9. To determine the antiquity of a plan by its delineated meridian.

10. On recording bearings.

11. The Traverse Tables, with examples of their use.

12. An expeditious method of calculating the produce of coal strata of any given thickness, with examples.

13. Concluding examples in mining surveying.

Having now described the plan, and enumerated the heads of this publication, I must leave it to practical colliery viewers of scientific skill to judge of its merits and utility, in its present improved form; and I trust, from my own practical experience in surveys of almost every kind during the last forty years, that the difficulties and intricacies of such a work will, to candid and liberal minds, be sufficiently obviated.

                                        T. BAKER.

CONTENTS.

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                              PART III.

EXPLANATION

OF

TERMS AND EXPRESSIONS IN THIS WORK.

Bearing to the right or left of a meridian. A line is said to bear on the right or left of the north or south meridian, when it is to the right or left of a person, whose face is turned towards the north or south.

Bearing on different sides of a meridian. Two lines are said to bear on different sides of a meridian, when the one bears on the east side, and the other on the west side thereof.

A Bord is an excavation in a seam of coal driven in a direction across its fibres.

A Drift is a narrow excavation driven in any direction in coal or stone.

A Headway is an excavation in a seam of coal driven in the direction of its fibres.

Different Meridians. When one line bears in a given direction with the north meridian, and another bears in a given direction with the south meridian, those lines are called bearing with different meridians. Also, when one line bears on the east side of the north meridian, and another on the west side of the south meridian, those lines are said to bear on different sides of different meridians, and *vice versâ*.

TREATISE

ON

SUBTERRANEOUS SURVEYING,

ETC.

PART I.

GEOMETRICAL PROBLEMS.

1.—*To divide a given line AB into equal parts.*

WITH any distance greater than half AB, and one foot of the compasses on A and B, describe two arches cutting each other in C and D; through the intersecting points CD draw a line CD, which will cut AB in I into equal parts.
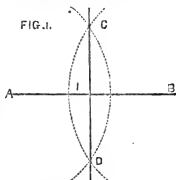
2.—*To draw a line parallel to a given line CD, to pass through any assigned point A.*

From the given point A take the nearest distance to the given line CD; with that distance, and one foot of the compasses, any where towards C describe an arch O; through A draw a line AB, just to touch the arch O in O; and the line AB will be the parallel required.
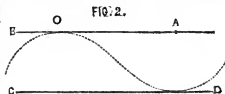
3.—*To raise a perpendicular from a given point* P *in a given line* AB.

From the given point P describe the arch FD; take PF, and set from F to C, and from C to D; then with any convenient distance from C and D describe the arches O, and through their point of intersection from the point P draw the line PO, the perpendicular required.

FIG. 3.
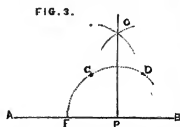
4.—*To raise a perpendicular from a given point* A, *at the end of a given line* AB.

Set one foot of the compasses on A, and extend the other to any point C, above the line AB; on the centre C describe the semicircle FAP, to cut AB in F; draw FC cutting the semicircle in P; then draw AP, which will be perpendicular to AB.

FIG. 4.
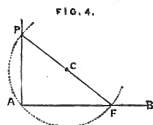
5.—*From a given point* P *to let fall a perpendicular upon a given point line* AB.
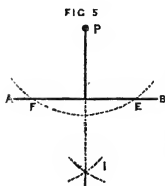
On the given point P as a centre, describe the arch EF to cut AB in E and F; with any convenient distance, and one foot of the compasses on E and F, describe two arches to cut each other in I; through P and I draw PI, which is perpendicular to AB.

FIG 5

6.—*To make an angle ABC equal to a given angle CDE.*

With any convenient extent of the compasses, and one
foot on D, draw the arch FG;
equal to the measure of the
given angle D draw a line BC,
and with the distance DF de-
scribe the arch HI; then make
the arch HI equal to the arch
FG, and through I draw the line
BA, forming the angle;—so the
angle ABC is equal to the angle
CDE.

FIG. 6.
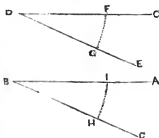
7.—*To lay down an angle FDG equal to any determined
number of degrees, which suppose 35°*

Draw the line DF at pleasure, and with 60° off the scale
of chords describe the arch
EH on the centre D; from
the same chords take 35°
(the quantity of the angle),
and lay upon the arch from E
to H, through which from D
draw the line DG, and the
angle FDG will contain just
35°.

FIG. 7.
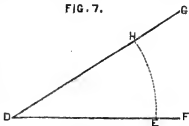
8.—*To determine the number of degrees contained in any
angle, suppose angle FDG.*

With 60°, taken from the scale of chords, describe the
arch EH; then extend the compasses from E to H, and
observe, on the same line of chords, what number of degrees
the extension measures,—which will be the measure of the
angle EDH.

Or, apply the centre of the protractor to the angular
point D, and bring its straight edge upon the line DF, and
the degree the other line cuts on the divided arch is the
measure of the angle.

THEOREMS.

1. Every right angle, as ACB, contains 90 degrees or equal parts.

FIG. 8.
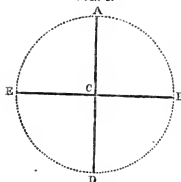
2. Every circle ABDE, is supposed to have its periphery divided into, or to contain, 360 equal parts, called degrees,—and those degrees are divided into 60 equal parts, called minutes,—and each minute is divided again into 60 equal parts, called seconds, &c.

3. Every circle AD, contains four right angles, at angles ACB, BCD, DCE, and ECA, which, from theorem 1, must contain 90° each.

4. Every semicircle EAB, contains two right angles, as angles ECA and ACB, which, from theorem 1, must contain 90° each.

Draw the diameter AD, which will divide the circle EABD into two equal parts EAB and EDB, each containing a semicircle, or 180°; if, therefore, a line AC be drawn perpendicular to EB from the centre C, it will divide the semicircle EAB into two equal parts, making two right angles ECA, ACB.
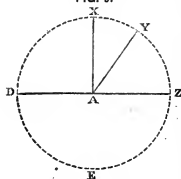
FIG. 9.

5. If any right line AY stands upon another right line DZ, it will make therewith two right angles, or two angles whose sum is equal to two right angles. — (Euc. b. 1, p. 13.) If a line AY, be drawn from any part Y of the circumference to A, it will

divide the semicircle DXZ into two unequal parts, making the angles DAY, YAZ, unequal; but these two angles are equal to a semicircle, or two right angles.

6. If two right lines IL, KM, intersect each other, the opposite angles A and C, as also B and D, are equal; that is, the angle A = the angle C, and the angle B = the angle D.—(Euc. b. 1, p. 15.)

FIG. 10.
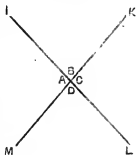
7. If a right line OR, cuts two parallel right lines NP and SQ, the alternate angles NaR, QbO, are equal, and consequently the lines parallel.—(Euc. b. 1, p. 29.)
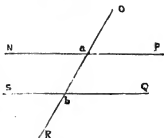
8. If any side of a right-lined triangle be continued, see fig. 12, the external angle is equal to the sum of the two opposite internal ones.—(Euc. b. 1, p. 32.)

FIG. 11.

Let UST be the given triangle; then the ∠ STZ is = ∠ SUT + ∠ UST, = the sum of the opposite internal angles.
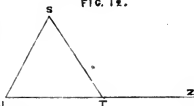
9. The three angles of any triangle are together equal to two right angles, or 180°.—(Euc. b. 1, p. 32.) See fig. 12.

FIG. 12.

In the triangle STU, the ∠ STU + ∠ TSU + ∠ SUT = 180°, or two right angles.

10. The sides of similar triangles are proportional, and the angles subtended by proportional or equal sides are equal.—(Euc. b. 6, p. 45.)

11. In any four-sided right-lined figure, called a square parallelogram, rhombus, trapezium, &c., the sum of the

four angles is equal to four right angles, or 360°.—(Euc. b. 1, p. 32.)

12. The sum of all the angles of any right-lined figure (though it contain never so many sides) is equal to double as many right angles, abating four, as there are sides in the figure.—(Euc. b. 1, p. 32.)

13. In right-lined triangles, equal sides subtend equal angles (Euc. b. 1, p. 5). The greatest side subtends the greatest angle (Euc. b. 1, p. 19), and the least side subtends the least angle.

14, An angle in a semicircle is a right angle; or if two

FIG. 13.
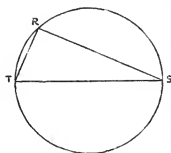
lines, as TR, SR, be drawn from T and S (the ends of the diameter) to R in the circumference, they will form a right angle TRS.— (Euc. b. 3, p. 31.)

15. In any right-angled triangle, the square of the hypothenuse (or longest side) is equal to the sum of the squares of the other two sides or legs. —(Euc. b. 1, p. 47.)

16. The compass is divided into four cardinal points, called north, south, east, and west; the two first, north and south, are formed where the meridian cuts the horizon,—

FIG. 14.
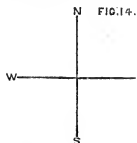
and the other two, east and west, are each 90 degrees distant from the points north and south; therefore they divide a circle into four equal parts of 90 degrees each.

17. When the face is turned to the north N, the right hand is towards the east E, and the left hand towards the west W; and when the face is turned towards the south S, the right hand is towards the west W, and the left hand towards the east E.

18. The magnetic meridian is that line in which the magnetic needle of the compass settles; and every particular place on the earth has its respective magnetic meridian.

19. The magnetic needle is here assumed to retain its parallelism in every situation within the limits of a subterraneous survey.

If in the situation A, a magnetic needle is placed, and is found to settle in the direction of *ab*, — if the same needle is removed to B or C, it will settle itself in the direction of *cd* and *ef*, both parallel to *ab*. But the magnetic meridian of places very distant from each other will not be parallel; for the magnetic meridian of London will vary a few degrees from its parallelism with that of Edinburgh. The magnetic needle has a small diurnal variation, being greatest about noon, also a small annual variation, which seldom exceeds a few minutes of a degree.

FIG. 15.
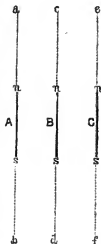
Part First of this work consists of the manner of surveying under-ground, without attending to the magnetic variation of the needle,—with several easy and expeditious modes of plotting the same.

The instruments used in subterraneous surveying are the circumferentor, the theodolite, Gunter's chain, in the coal mines, which contains 100 links. In the lead mines, a chain, divided into 100 feet, is now frequently used instead of Gunter's chain.

The manner of conducting a subterraneous survey by the magnetic needle.

(1.) Place the circumferentor, or instrument used, where

the survey is intended to commence; then let a person go forward in the direction of the line to be surveyed, with a lighted candle in his hand, to the utmost distance his light can be seen through the sights of the instrument; its bearing then is taken by the circumferentor (the manner of taking bearings will be shown hereafter), and noted down in the survey book; proceed then to take the distance of the light or object from the instrument; remove the instrument, and let a person stand on the exact spot where it stood, holding in his hand one end of the chain, while another, going towards the object, holds the other end, together with a lighted candle, in the same hand; then being directed by the former until that hand which holds the candle and the chain is in a direct line with the object or light whose bearing was taken, there mark the first chain; then he that stood where the instrument was placed comes forward to the mark at the end of the first chain, the other advancing another chain forward, with the candle and chain in the same hand, directed as before, there mark the second chain, — so proceeding in the same kind of way until the distance of the object is determined, which being noted down in chains and links in the survey book, opposite to the bearing, then the first bearing and distance is completed:—Fix the instrument again where the light, as an object, stood, or at the termination of the preceding bearing and distance, and take the second bearing, by directing the person to go forward as before, so far as his light can be seen, or at any shorter convenient distance, and proceed as before until the whole is completed.

There should not be fewer than five people employed in such surveys, to carry forward the work with expedition, —viz., one to carry forward the survey, and make the necessary observations and remarks; another to carry the instruments; another to direct the chain; another to lead it; and another to go forward with a light, as an object,

from station to station. During the time of making the survey, be careful in not admitting any iron, steel, or other ferruginous substance, within ten feet of the instrument, for fear of attracting the needle; I have seen the needle affected at almost twice the above distance, by a very massy piece of iron. Also if the glass of the instrument stand in need of cleaning, it must be rubbed as gently as possible, and not with any silken substance, for that will be apt to excite electrical matter, which will prevent the needle from traversing; but if that matter should be excited, it may be very easily discharged, by touching the surface of the glass with the wet finger.

In order for familiarising the young miner with this system of surveying, previous to his practising it in mines, it would be necessary for him to fix up a number of marks on the surface, and afterwards take their bearing and distance from each other, according to the method before directed. But to approach nearer to the form of subterraneous surveying, it would be much better to do it at night, by the assistance of candle-light; many favourable evenings might be found for this mode of practising. Should the current of air be too strong for the naked flame of the candle, lanterns may be used.

To find the magnitude of angles.

(2.) Every circle, ABCD, is supposed to contain 360° (see theorem 2); each semicircle DAB and DCB contains 180°; and each quadrant AB, BC, CD, and DA, contains 90°. Draw the line ab; and if $\angle$ Aab contains 50° $\angle$ Dab must contain 90° − 50° = 40°, and $\angle$ baC must contain 180° − 50° = 130° (see theorem 5). Also if ab makes an angle of 50° with the line AC, and ad an angle of 30° with the same line, the semicircle ADC containing 180°, $\angle$ Aab = 50° + $\angle$ Cad = 30° = 80°, then 180° − 80°, leaves 100° = $\angle$ bad. Or thus, $\angle$ AaD = 90°; then

$90° - 50° \angle Aab = 40° \angle baD$; also $\angle DaC = 90°$;

FIG. 16.

then $90° - 30° \angle daC = 60°$
$\angle Dad$; consequently $\angle baD$
$= 40° + \angle Dad = 60° =$
$100° \angle bad$, as before. If ab
make an angle of $50°$ with aA,
and ac make another angle of
$75°$ with the same line aA,
then the $\angle cab = 75° - 50°$
$= 25°$; and if ab make an an-
gle of $50°$ with aA, and ac an
angle of $25°$ with the line ab,
then $50° + 25° = 75° \angle Aac$.
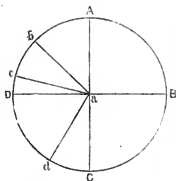
—(Euc. b. 1, p. 15.)

The manner of determining bearings, and also reducing angles into bearings.

(3.) The instrument used in subterraneous surveying is
the circumferentor, mentioned as before, whose effect
depends on the magnetic needle ; and the directions,

FIG 17

courses, or bearings, are
recorded according to
the angles these direc-
tions make with the
magnetic meridian. (The
magnetic meridian is the
north and south line, as
pointed out by the mag-
netic needle ; see theo-
rem 18.)

If we pass round from
the north N, to the east
E, and continue moving
from the east to the
south S, and from thence to the west W, and lastly from
the west to the north N, from whence we first of all set out,
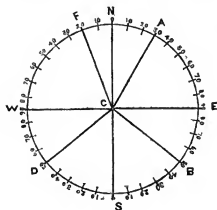
we shall have made a circuit NESWN of 360°, which all circles are supposed to contain (see theorem 2) ; and as there are four cardinal points (see theorem 16) in that circle, north, east, south, and west, dividing it into four equal parts, consequently from north N to east E subtends an angle of 90° ; from east E to south S subtends an angle of 90° ; from south S to west W subtends an angle of 90° ; and from west W to north N subtends an angle of 90°. Now let NE, or the distance between north and east,—also ES, or the distance between east and south,—also SW, or the distance between south and west,—and also WN, or the distance between west and north, be each divided into 90 equal parts or degrees, then a line in direction of CN may be called due north,—and another in direction of CS may be called due south,—another in direction of CE may be called due east, or north 90° east, or south 90° east,—and another in direction of CW may be called due west, or north 90° west, or south 90° west ; likewise the line CD passing between S and W, or between south and west, is called south 50° west, being 50° towards the west from south, or to the westward or right-hand (see theorem 17) of the south meridian line. The line CF passing between N and W, or between north and west, is called north 20° west, being 20° towards the west from north ; the line CA passing between N and E, or between north and east, is called north 30° east ; and the line CB passing between S and E, or between south and east, is called south 50° east ; for the bearing of any object from any point or place, taken by the circumferentor, is only the angle that object makes with the magnetic meridian of that point or place from which the bearing is taken : Therefore, if the bearing of B from C is required, it is nothing more than the direction and angle that B makes with the magnetic meridian of C ; CS is supposed the magnetic meridian of C, and BCS is the angle the object makes with that meridian.

Let WE, represent a circumferentor, and NS the magnetic
needle suspended on the pivot c as its centre of suspension
and centre of motion; AB are two horizontal arms fixed
opposite to each other on the instrument; on the extremity

FIG. 18.
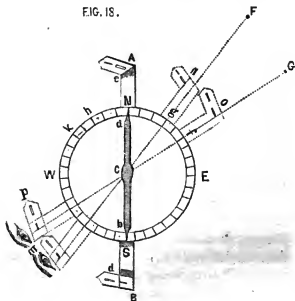
of each arm is the sight d and e perpendicular thereto,
through which is seen the object whose bearing is wanted :
The inner part of the circle to which the needle points is
divided into degrees, beginning at N, and numbered to 90
each way to W and E; and also beginning at S, and
numbered to 90 each way to the same points W and E.
The whole of the instrument is fixed on a stand, having
a ball and socket to allow of its being kept level and
turned freely round. This instrument is manufactured in
great perfection by Messrs. Elliott, Brothers, 30, Strand,
London.

To find the bearing of the line cF, let the centre of the
instrument be fixed at c; then turning it round so that the
eye of the observer may see F through the sights mn, the

needle always continuing in the same position, or preserving its parallelism, howsoever the instrument and sights are turned, the end N of the needle, which, before the sights were moved, pointed to north N, will, on the sight being moved in direction of c*F*, point to *h* 30°; for *h* will be brought to the situation of N ; then the angle N*cg* will be 30°, which is the bearing of F with the north magnetic meridian, and on being found to incline to the right,—therefore, from theorem 17, the bearing of F will be north 30° east, which is usually written N 30° E.

Again, suppose the bearing of G from *c* is wanted, turn the arms and sights *ed* in the situation of *po*, that is, in direction of *c*G, and the angle N*cf* will be 50°,—for the number of 50 at *k* will be opposite the end N of the needle; therefore, from theorem 17, the bearing will be found to be N 50° E.

To find what point of the compass an object bears on, when its direction, with respect to the magnetic meridian, is given.

(4.) RULE.—If the given angle that the object makes with the magnetic meridian is to the right of the north, the object will bear to the east of that meridian ; if to the left of that meridian, the object will bear to the west of it. Also, if the given angle that the object makes with the magnetic meridian is to the right of the south, the object will bear to the west of that meridian ; if to the left, it will bear to the east of it.—See theorem 17.

EXAMPLE I.—If I find an object makes an angle to the right of 25° with the magnetic meridian, when I face the north, what is the bearing of that object with that meridian ?

From the rule, the object will bear N 25° E.

EXAMPLE II.—If I find an object makes an angle to the left of 30° with the magnetic meridian, when I face the north, what is the bearing of that object with that meridian ?

The object will be N 30° W.

EXAMPLE III. — If I find an object makes an angle to the right of 30° with the magnetic meridian, when I face the south, what is the bearing of that object with that meridian?

The object will bear S 30° W.

EXAMPLE IV.—If I find an object makes an angle to the left of 25° with the magnetic meridian, when I face the south, what is the bearing of that object with that meridian?

The object will bear S 25° E.

EXAMPLE V.—If I find an object makes an angle to the right of 87° with the magnetic meridian, when I face the south, what is the bearing of that object with that meridian?

The object will bear S 87° W.

EXAMPLE VI.—If I find an object makes an angle of 86° to the right with the magnetic meridian, when I face the north, what is the bearing of that object with that meridian?

The object will bear N 86° E.

EXAMPLE VII.—If I find an object makes an angle of 89½° to the right with the magnetic meridian, when I face the north, what is the bearing of that object with that meridian?

The object will bear N 89½° E.

EXAMPLE VIII.—If I find an object makes an angle of 2° to the left with the magnetic meridian, when I face the south, what is the bearing of that object with that meridian?

The object will bear S 2° E.

EXAMPLE IX.—If I find an object makes no angle with the magnetic meridian, when I face the north, what is the bearing of that object with that meridian?

The object will bear due north, or will be in the direction of the magnetic meridian.

EXAMPLE X.—If I find an object makes an angle of

20° to the right of another object which makes an angle of 15° to the right with the magnetic meridian, when I face the north, what is the bearing of the first object with that meridian?

The object will bear (20 + 15 = 35) N 35° E.

EXAMPLE XI.—If I find a line makes an angle of 30° to the right of another line which forms an angle of 60° to the left with the magnetic meridian, when I face the north, what is the bearing of that object with that meridian?

The line will bear (60°−30°=30°) N 30° W.

The reversing of bearings.

(5.) If the bearing of N from S is found to be due north, the bearing of S from N will be due south, — just the reverse of the former; and if the bearing of B from S is found to be N 20° E, the bearing of S from B will be S 20° W,—the reverse; and so of any other.

FIG 19.

To reduce bearings into angles.

(6.) Suppose the line CD to bear N 50° E with the magnetic meridian NCS (north being represented by N, and south by S), then CD will make an angle of 50° NCD with the north magnetic meridian CN; and with the south magnetic meridian CS it will make an angle of 180° − 50° NCD = 130° SCD (see theorem 5): And if the line CF bear S 30° E with the magnetic meridian, it will make an angle of 30° SCF with the south magnetic

FIG. 20.
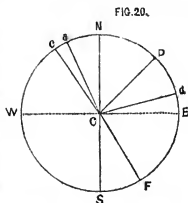
meridian CS ; and with the north magnetic meridian CN it
will make an angle of 180°− 30° SCF = 150° NCF: Also if
the line CE bear due east with the magnetic meridian, it will
make an angle of 90° NCE, or SCE, with that meridian ; for
east or west always forms an angle of 90° with the meridian
(see theorem 16): Or if the line CD bear N 50° E from the
point C, and that of C*d* N 80° E from the same point C,
then these two bearings being both of the same side of the
same meridian, will form an angle with each other of 80° −
50° = 30° ∠ DC*d*: Or if the line CD bear N 50° E from
the point C, and that. of CFS 30° E from the same point
C, then these two bearings, being both of the same side of
different meridians, will form an angle with each other of
180°− 50° + 30° =100°∠ DCF: Or if CD bear N 50° E
from the point C*a*N 25° W from the same point C, then
these two bearings, being of different sides of the same
meridian, will form an angle with each other of 50° + 25°
= 75° ∠ DC*a*: Or if C*a* bear N 25° W from the point C,
and CFS 30° E from the same point C, then these two
bearings, being of different sides of different meridians, will
form an angle with each other of 180°− 30° ∠ SCF + 25°
NC*a*= 175° ∠ *a*CF, or 30°− 25° = 5°; which difference
being taken from 180°, leaves 175° ∠ *a*CF, as before: Or if
C*e* bear N 30° W from the point C, and that of CFS
30° E from the same point C, then the one bearing as
much to the west side of the north meridian as the other
does to the east side of the south meridian, they will form
no angle at all, but a direct line, with each other, or 30°−
30°=0°; which taken from 180°, leaves 180°, which, as
before, shows they form a direct line. (See theorems 4
and 5.)

(7.) If the magnitude of the angles B and C is required,
which is formed by the bearing AB taken from A to B,
S 50° E; of the bearing BC taken from B to CS 45° W ;
and of the bearing CD taken from C to D, S 20° E; now
to render the two bearings which form the ∠ B to bearings

taken from that angular point, the bearing AB, which is the bearing of B from A, must be made the bearing of A from B, by reversing it (Art. 5): Then the

∠ B is the angle formed by the bearings N 50° W, and S 45° W; which bearings, being on the same side of different meridians, will form an angle of 180° − 50° + 45° = 85° ∠ B : And by reversing the bearing BCS 45° W, the ∠ C will be the angle formed by the bearing N 45° ECB, and S 20° ECD; which

FIG. 21.

bearings, being on the same side of different meridians, will form an angle of 180° − 45° + 20° = 115° ∠ C. In determining the magnitude of angles formed by bearings, those bearings which compose the angles must be supposed to be taken from the angular point.
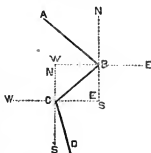
To find the number of degrees contained in the angle that any given bearing makes with the magnetic meridian.

(8.) RULE I.—The number of degrees of the bearing will be the magnitude of the angle that bearing forms with the meridian it is taken from ; and the same number of degrees, taken from 180°, leaves the number of degrees contained in the angle the same bearing makes with the contrary meridian.

To find the number of degrees contained in an angle formed by two given bearings taken from the same point, when they are both on the same side of the same meridian.

RULE II.—From the number of degrees contained in the one of the bearings, take the number of degrees contained in the other, and the difference will be the number of degrees contained in the angle formed by the two bearings.

To find the number of degrees contained in an angle formed by two given bearings taken from the same point, when they are both on the same side of different meridians.

RULE III.—Take the sum of the degrees contained in the bearings from 180°, and the remainder will be the number of degrees contained in the angle formed by the two bearings.

To find the number of degrees contained in an angle formed by two given bearings taken from the same point, when they are on different sides of the same meridian.

RULE IV.—The sum of the degrees contained in the bearings is the number of degrees contained in the angle formed by the two bearings.

To find the number of degrees contained in an angle formed by two given bearings taken from the same point, when they are on different sides of different meridians.

RULE V.—Take the difference of the number of degrees contained in the bearing from 180°, and the remainder will be the number of degrees contained in the angle formed by the two bearings.

To find the number of degrees contained in any angle which is formed by given bearings not taken from the angular point.

RULE VI.—Reduce the bearings which compose the angle required into bearings taken from that angular point (which is done by reversing one of them; Art. 5) then by the preceding rules find the number of degrees contained in the angle required.

EXAMPLE I.—In the bearing N 5° W, what is the magnitude of the angle formed with that bearing and the north magnetic meridian?

From rule 1, Art. 8, the bearing will form an angle of 5° with the north magnetic meridian.

EXAMPLE II. — In the bearing S 65° E, what is the

magnitude of the angle with that bearing and the south magnetic meridian?

The bearing will form an angle of 65° with the south magnetic meridian.

EXAMPLE III.— In the bearing S 20° W, what is the magnitude of the angle with that bearing and the north magnetic meridian?

From rule 1, Art. 8, from 180°−20°=160°, the magnitude of the angle formed with the north magnetic meridian.

EXAMPLE IV.— In the bearing N 80° E, what is the magnitude of the angle with that bearing and the south magnetic meridian?

From 180°− 80° = 100°, the magnitude of the angle formed with the south magnetic meridian.

EXAMPLE V.—In the bearing due east, what is the magnitude of the angle with that bearing and the south, and also north, magnetic meridian?

The bearing will form an angle of 90° with both the south and north magnetic meridians.   (See theorem 16.)

EXAMPLE VI.—In a bearing N 50° E, and another N 80° E, both taken from the same point, what is the magnitude of the angle formed by the two bearings with each other?

From rule 2, Art. 8, the bearings being on the same side of the same meridian 80°−50°= 30°, the magnitude of the angle formed by the two bearings.

EXAMPLE VII.—In a bearing S 60° E, and another S 10° E, both taken from the same point, what is the magnitude of the angle formed by the two bearings with each other?

60°−10°= 50°, the angle that the two bearings will form with each other.

EXAMPLE VIII. — In a bearing S 30° E, and another N 50° E, what is the magnitude of the angle formed by the two bearings with each other, when they are both taken from the same point?

From rule 3, Art. 8, the bearings being on the same side of different meridians, then $180° - 30° + 50° = 100°$, the magnitude of the angle formed by the two bearings.

EXAMPLE IX. — In a bearing N 80° W, and another S 85° W, what is the magnitude of the angle formed by the two bearings with each other, when they are both taken from the same point?

$180° - 80° + 85° = 15°$, the magnitude of the angle formed by the two bearings.

EXAMPLE X. — In a bearing N 50° E, and another N 40° W, what is the magnitude of the angle formed by the two bearings with each other, when both taken from the same point?

From rule 4, Art. 8, the bearings being on different sides of the same meridian, then $50° + 40° = 90°$, the magnitude of the angle formed by the two bearings.

EXAMPLE XI.—In a bearing S 10° W, and another S 5° E, both taken from the same point, what is the magnitude of the angle formed by the two bearings with each other?

$10° + 5° = 15°$, the angle formed by the two bearings.

EXAMPLE XII. — In a bearing N 50° E, and another S 30° W, both taken from the same point, what is the magnitude of the angle formed by the two bearings with each other?

From rule 5, Art. 8, the bearing being on different sides of different meridians, then $50° - 30° = 20°$, which taken from $180° = 160°$, the magnitude of the angle formed by the two bearings.

EXAMPLE XIII. — In a bearing S 60° W, and another N 86° E, both taken from the same point, what is the magnitude of the angle they form with each other?

$180° - 86° - 60° = 154°$, the magnitude of the angle formed by the two bearings.

EXAMPLE XIV. — In a bearing S 80° W, and another N 5° W, both taken from the same point, what is the magnitude of the angle formed with each other?

$180° - \overline{80° - 5°} = 105°$, the magnitude of the angle formed by the two bearings.

EXAMPLE XV. — In a bearing N 20° W, and another S 20° E, both taken from the same point, what is the magnitude of the angle formed with each other?

$180° - \overline{20° - 20°} = 180°$; therefore the two bearings form no angle, but a direct line, with each other.

EXAMPLE XVI. — Suppose the bearing ABS 50° E, fig. Art. 7, taken from A to B, and BCS 45° W, taken from B to C, required the magnitude of the angle B formed by those two bearings?

The two bearings which form the angle are not taken from the angular point B, the leg AB being taken from the point A: Therefore, from rule 6, Art. 8, by reversing the bearing ABS 50° E, to BAN 50° W, the angle B will then be formed of two bearings taken from the same angular point (viz.) BAN 50° W, and BCS 45° W; which bearing on the same side of different meridians, from rule 3, Art. 8, will be $180° - \overline{50° + 45°} = 85°$, the magnitude of the required angle.

EXAMPLE XVII. — In the bearing BCS 45° W, fig. Art. 7, taken from B to C, and CDS 20° E taken from C to D, required the magnitude of the angle C formed thereby?

The two bearings which form the angle are not taken from the angular point C; Therefore, from rule 6, by reversing BCS 45° W to N 45° E, the angle C will then be composed of two bearings taken from that angular point, N 45° E, and S 20° E; which bearing on the same side of different meridians, from rule 3, Art. 8, will be $180° - \overline{45° + 20°} = 115°$, the magnitude of the required angle.

The reducing of bearings and distances to their northing or southing, and easting or westing, from the point of departure.

(9.) Suppose it is required to know how far B is north-

ward of A. If SN represent the meridian, Aa will be the
northing of B from A, and aB, or Ab, will be its easting,
or what B is eastward of the meridian of the
point A.

FIG. 22
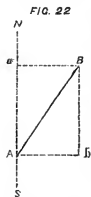
If we pass from any point A to B (fig. 23),
and from B to C, and from C to D, and
from thence return to the point A again, our
route will have as much southing as northing,
and easting as westing; that is, the southing
will be equal to the northing, and the easting
will be equal to the westing. Let SN repre-
sent the meridian of A, the point of depar-
ture; the northing of AB from that point
will be represented by Aa, the northing of
ABC by Ab, that of ABCD by Ac; and as the northing
of D from A is equal to Ac, the southing of A from D

FIG 23
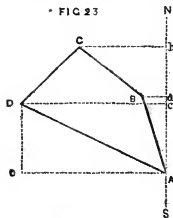
will be equal to De = cA;
therefore the southing will
be equal to the northing of
ABCDA: Also let the westing
of AB from the meridian of
A be represented by aB, that
of ABC by bC, that of ABCD
by cD; then as the westing of
D from the meridian of A is
equal to cD, the easting of A
from D will be equal to eA
= cD: Therefore the easting
will be equal to the westing

of ABCDA.

*To find the northing or southing, and also the easting or
westing, of any given bearing and distance.*

(10.) RULE.—Look in the traverse tables, under the
degree answering to that of the bearing: and to the right,
opposite the length of that bearing (in the column of dis-

tances), will be found the quantity of northing or southing, according as the bearing is north or south,—and also the easting or westing, according as the bearing is east or west.

Note.—When the given distance consists of chains and links, and the angles of degrees and minutes, the method of finding the northing or southing, and the easting or westing, is given in Art. 59.

EXAMPLE I.—What is the northing and easting of the bearing and distance N 40° E 10 chains?

Look in the traverse tables, under 40°, and opposite 10 chains, in the column of lengths, is found 7 chains 60 links of northing, and 6 chains 43 links of easting (the links are usually written after the chains as decimals, see next Example).

EXAMPLE II.—What is the northing and westing of N 10° W 6·50 chains from the point of commencement, or point of departure?

Its northing is 6·40 chains, and its westing is 1·13 chains.

EXAMPLE III.—What is the southing and westing of S 79° W 7·30 chains from the point of departure?

Its southing is 1·39 chains, and its westing 7·16 chains.

EXAMPLE IV.—What is the southing and westing of S 80° W 6 chains?

Its southing is 94 links, and its westing 5·36 chains.

EXAMPLE V.—What is the northing and westing of N 40° W 8·50 chains?

Its northing is 6·50 chains, and its westing is 5·46 chains.

EXAMPLE VI.—What is the southing and easting of S 5° E 6·52 chains?

Its southing is 6·49 chains, and its easting is 56 links.

EXAMPLE VII.—In the following successive bearings and distances taken from the pit A to the pit B, N 50° W 10 chains, N 20° E 5 chains, and S 40° W 7 chains, I wish to know what denomination of bearing the pit B will have from A; also the length of each?

PREPARATORY TABLE.

BEARINGS.	NORTHING.	SOUTHING.	EASTING.	WESTING.
	Chains.	Chains.	Chains.	Chains.
N 50° W 10 chains	6·43	...	...	7·66
N 20° E 5 ,,	4·70	...	1·71	...
S 40° W 7 ,,	...	5·36	...	4·50
	11·13			12·16
	5·36			1·71
	5·77			10·45

Now, as the northing is greater than the southing by 5·77 chains, and the westing greater than the easting by 10·45 chains, the pit will have 5·77 chains of northing, and 10·45 chains of westing from A.

EXAMPLE VIII.—What is the northing and westing of the pit D from C, under the following bearings, N 20° E 10 chains, and S 60° W 6 chains ?

BEARINGS.	NORTHING.	SOUTHING.	EASTING.	WESTING.
	Chains.	Chains.	Chains.	Chains.
N 20° E 10 chains	9·40	...	3·42	...
S 60° W 6 ,,	...	3·00	...	5·20
	9·40			3·42
	3·00			1·78
	6·40			

The southing being taken from the northing, and the easting from the westing, the pit D will have 6·40 chains of northing, and 1·78 chains of westing, from the pit C.

EXAMPLE IX.—What is the northing and easting of B from A under the following successive bearings, S 20° W 10 chains, N 5 chains, N 30° E 20 chains, and N 5° E 8 chains ?

The pit B will have 20·89 chains of northing, and 7·28 chains of easting, from A.

Surveying and recording bearings.

(11.) Suppose the bearing of ABC to be required. Set
the circumferentor on A (the north being represented by
N and the south by S): then turning that
part of the instrument having the *fleur-de-lis*
from you, or towards B, turn the instrument
until the object B is seen through, and cut by,
the hair in the sights; and the angle NAB
being the angle that the sights and line AB
make with the magnetic meridian NS, will be
the bearing of B from A,—suppose 30°; which
also being to the right side of the north
meridian, will be N 30° E (see theorem 17):
Then bring the instrument forward to B, and
fix it there, directing the same sight at B
towards C as was directed at A towards B;
then observe the angle that BC makes with the
magnetic meridian,—which suppose 25° NBC;
and being to the left of the meridian, will be N. 25° W.
In order to prove the work, and try the accuracy of the
instrument when it is standing at B, apply the eye to that
sight which was next B when it stood at A; then take the
bearing of A from B, which, if found to be the reverse of
B from A, shows the work so far is true. The bearing
of B being taken, in like manner, from C, will prove the
truth of the survey. Observe always to take the degrees
of each bearing by the same end of the needle.
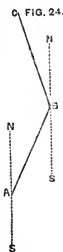
(12.) Suppose the bearing of B from A, C from B, and
D from C, to be required: Fix the instrument at A, with
the *fleur-de-lis* towards B (the north being represented by
N and the south by S); then take the bearing of B, as
before-described,—which suppose to make an angle of 30°
NAB to the right with the magnetic meridian, or N
30° E; remove the instrument to B, and take the bearing
of C,—which suppose equal to 30° NBC to the left,

c

or N 30° W; then remove the instrument to C, and

FIG. 25.

take the bearing of D,—which suppose equal to 65° SCD to the left, or S 65° E: See below in the survey-book.
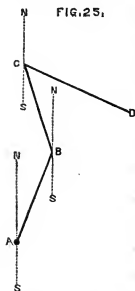
From A to B, N. 30° E.
   B to C, N. 30° W.
   C to D, S. 65° E.

Note.—This survey may be proved in the same manner as the preceding; and the methods of plotting and protracting subterraneous surveys, with the descriptions of the instruments used for the purpose, are given in Arts. 23, 24, 25 and 26, to which the student is referred, as it would greatly facilitate in these studies to lay down his work on paper, as soon after he has finished it as a proper opportunity presents itself; all the instruments required, in the first instance, being a scale of equal parts, a protractor, and a ⊤-square.

(13.) Suppose the subterraneous working ABCDA, to

FIG 26
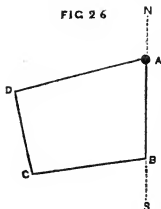
be surveyed, beginning at the pit A: Fix the instrument at the centre of the pit A; then let a person hold a lighted candle at B, being the utmost distance it can be seen through the sights of the instrument, the bearing of which being taken from A, suppose due south, or in the direction of the magnetic meridian of A,—and its distance from A suppose 6·57 chains; which place in the survey-book, as below:

Remove the instrument to B, where the candle stood, and direct the person to place the lighted candle at C; then take its bearing from B, which suppose to make

an angle CBS of 80° with the magnetic meridian, or to bear S 80° W; and its distance being found 7·10 chains, remove the instrument to C, the lighted candle being removed to D; then take its bearing and distance as before, which suppose N 10° W 5 chains; remove the instrument to D, and direct the lighted candle to be placed at the centre of the pit A, where the survey commenced; then take its bearing from D, which suppose N 70° E 8·35 chains,—and the survey will be finished.

A survey of a subterraneous working, commencing at the centre of the pit A.

AB, S.	.	.	.	.	6·57 chains.
BC, S. 80° W.	.	.	.	.	7·10 „
CD, N. 10° W.	.	.	.	.	5·00 „
DA, N. 70° E.	.	.	.	.	8·35 „

This survey, which is composed of four sides, may be proved by adding together the degrees contained in the interior angles, which, if they amount to 360, the work will be right.—(See theorem 11).

The proof.—The magnitude of the angle DAB is 70° (see rule 1, art. 8) in the reducing of bearings into angles; angle ABC is 180° − 80° ∠ CBS = 100°; angle BCD is 80° + 10° = 90° (see rule 4, art. 8); and angle CDA is 180° − 70° + 10° = 100° (see rule 3, art. 8).—

$$
\begin{aligned}
\text{Then } \angle \text{ DAB} &= 70° \\
\angle \text{ ABC} &= 100° \\
\angle \text{ BCD} &= 90° \\
\angle \text{ CDA} &= 100° \\
\hline
&360°
\end{aligned}
$$

Also the proof may be made by finding the northing, southing, easting, and westing of all bearings and distances. If the southings are equal to the northings, and the westings equal to the eastings, then the work will be right.—(See Art. 9.)

		Northing.	Southing.	Easting.	Westing.
	C. L.	Chains.	Chains.	Chains.	Chains.
Thus, S. . . . 6 57		...	6·57	...	6·98
S. 80° W. 7 10		...	1·23	...	6·98
N. 10° W. 5 0		4·93	...	...	0·87
N. 70° E. 8 35		2·87	...	7·85	...
		7·80	7·80	7·85	7·85

Therefore the northings and southings being equal, as also the eastings and westings equal, the work is right.

(14.) Suppose the bearing and distance of B from A, C from B, D from C, F from D, G from B, H from G, and I from H, are required. Fix the instrument at A, and take the bearing (as before described) of B from it, which suppose to be N 30° W, and the distance 5·50 chains; set it down in the following survey-book; also make a mark * with chalk at B, which must likewise be noted down, to return to. In order to take the bearings of C, D, and F, remove the instrument to B, and take the bearing of C from it, which suppose N 45° E, and distance 7 chains; the bearing of D from C suppose N 50° W, and the distance 5 chains; the bearing of F from D suppose N 85° E, and distance 7 chains: Then bring the instrument from D to the chalk mark at B, and take the bearing of G from B, which suppose S 65° W, and distance 6·50 chains; the bearing of H from G suppose N 10° W, and distance 6 chains; and lastly, the bearing of I from H suppose N. 60° E., and distance 4 chains.—See them properly arranged in the following survey-book (p. 29).

Suppose the bearings and distances of B from the pit A, C from B, D from C, F from D, G from F, H from G, P from H, and A from P,—also I from O, K from I, L from I, and M from L, are required, together with any remarkable circumstance that may be met with in the survey: Fix the instrument at A, directing a person to go with a lighted candle to B, and take the bearing and

SURVEY-BOOK.

Commencing at A.	Chains.	
N. 30° W. . .	5·50	to B.
At B is a chalk mark * to return to.		
N. 45° E. . .	7·00	to C.
N. 50° W. . .	5·00	to D.
N. 85°. W. . .	7·00	to F.
Returns to the chalk mark at B, and proceeds to G, &c.		
S. 65° W. . .	6·50	to G.
N. 10° W. . .	6·00	to H.
N. 60° E. . .	4·00	to I.

FIG. 27.
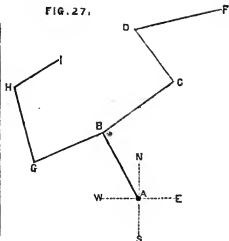
distance of B from it, which suppose S 36° E 7 chains; which insert in the survey-book. Also at *a*, 3 chains from A towards B, is the water-course from the pit R: Bring the instrument to B, and take the bearing and distance of the lighted candle at C, which suppose S 42° W 4 chain. At *b*, 3 chains from B towards C, is the water-course from the pit F: Remove the instrument to C, and take the bearing and distance of the light at D, which suppose S. 75°. W. 10 chains. At 4 chains from C towards D is a chalk * at O, to return to. Take the bearing and distance of F from D, which suppose N 42° W 7·50 chains,

FIG. 28.

to a pit; which note also down in the survey-book: Take the bearing and distance of G from F, which suppose N
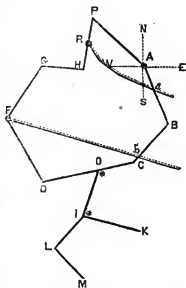
42° E 5 chains : Take the bearing and distance of H from
G, which suppose E 4 chains : Take the bearing and
distance of P from H, which suppose N 9° E 4 chains.
At 2 chains from H, towards P, is the pit R; which note
down in the survey-book. Take the bearing and distance
of A from P, which suppose S. 69° E. 5·56 chains. Now
return to the * mark at O, and fix the instrument there :
Take the bearing and distance of the candle placed at I,
which suppose S 10° W, 5 chains, and a chalk mark *
to return to : Take the bearing and distance of K from I,
which suppose S 80° E 6 chains. Return to the mark at
I, and fix the instrument, and take the bearing and distance
of L from it, which suppose S 40° W 4 chains : Take the
bearing and distance of M from L, which suppose S 45° E
4 chains,—and the survey will be finished.

See the bearings and distances arranged in form of a Survey-book.

		Chains.	
From A to B	S. 36° E.	7·00	
	At	3·00	from A is a, the water-course from the pit R.
B to C	S. 42° W.	4·00	
	At	3·00	from B is b, the water-course from the pit F.
C to D	S. 75° W.	10·00	
	At	4·00	from C is D, a chalk mark * to return to.
D to F	N. 42° W.	7·50	and pit F.
F to G	N. 42° E.	5·00	
G to H	E. . .	4·00	
H to P	N. 9° E.	4·00	
	At	2·00	from H is the pit R.
P to A	S. 69° E.	5·56	
			Return to the chalk mark * at O.
O to I	S. 10° W.	5·00	
			At I is a chalk mark * to return to.
I to K	S. 80° E.	6·00	
			Returned to the chalk mark * at L.
I to L	S. 40° W.	4·00	
L to M	S. 45° E.	4·00	

(15.) Suppose a survey of the subterraneous working ABCDFGHPA see last fig., is required, to commence at the pit A: Proceed as in the last, recording each bearing and its respective distance in the following manner, as in the survey-book :—

THE SURVEY COMMENCING AT THE PIT A.

		Chains.
From A to B	S. 36° E.	7·00
B to C	S. 42° W.	4·00
C to D	S. 75° W.	10·00
D to F	N. 42° W.	7·50
F to G	N. 42° E.	5·00
G to H	E. . . .	·4·00
H to P	N. 9° E.	4·00
P to A	S. 69° E.	5·56

To prove this survey by theorem 12: The number of sides which the survey contains is 8 ; then the amount of all the angles contained in the figure is equal to $\overline{8 \times 2} \times 90° - 4 \times 90° = 1080°$. Now from the rules of reducing bearings into angles (art. 8), $\angle$ B = 102°, $\angle$ C = 147°, $\angle$ D 117°, $\angle$ F = 96°, $\angle$ G 132°, $\angle$ H = 261°, $\angle$ P = 78°, and $\angle$ A = 147°; whose sum is equal to 1080°, as before: Therefore the survey is right.

Also the same may be proved by taking the northing, southing, easting, and westing of the bearings (art. 9); which, if the southings are found equal to the northings, and the westings equal to the eastings, the survey will be right.

Bearing and Distance.	Northing.	Southing.	Easting.	Westing.
Chains.	Chains.	Chains.	Chains.	Chains.
S. 36° E. 7·00	...	5·66	4·21	...
S. 42° W. 4·00	...	2·97	...	2·63
S. 75° W. 10·00	...	2·59	...	9·66
N. 42° W. 7·50	5·55	...	...	4·97
N. 42° E. 5·00	3·72	...	3·95	...
E.	...	...	4·00	...
N. 9° E. 4·00	3·95	...	0·63	...
S. 69° E. 5·56	...	2·00	5·21	...
	13·22	13·22	17·31	17·31

The northings and southings being equal, and the eastings and westings being also equal, the survey must be right.

(16.) Suppose the subterraneous bearings and distances of the workings ABCDF, are required, commencing at

FIG 29

the pit A ; and likewise the bearing and distance on the surface of a sinking pit G from the pit A : Fix the instrument at the centre of the pit A in the mine, and take the bearing and distance of B from it; also, of C from B, D from C, and F from D ; then the survey under-ground will be completed. Ascend to the surface, and fix the instrument at the mouth of the pit A ; and having previously placed a mark at the pit G, take its bearing and distance from A, which insert in the survey-book. (Observe to take the bearing of G from the same point of the pit A, on the surface, that the subterraneous survey commenced under the surface,—so that the proper situation of F, or any other part of the subterraneous working, may be shown with
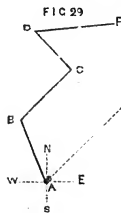
respect to the two pits.) If the bearing and distance of the pit G from that of A cannot be got at once, by the interposition of any building or other obstruction, it must be taken at two or three, or more, different bearings.

		Chains.
From A to B	N. 30° W.	5·50
B to C	N. 45° E.	7·00
C to D	N. 50° W.	5·00
D to F	N. 85° E.	7·00
	The bearing and distance of the sinking pit G from the pit A, taken on the surface.	
A to G	N. 45° E.	18·00

(17.) Suppose the subterraneous workings CDFGHI KBLMOP are required to be surveyed, beginning at the pit A: Fix the instrument at A, and take the bearing and distance of the headways AC (as before shown), which suppose S 10° E 3·10 chains. At 80 links is a bord 1 to the right and left, holed into the headways each way; at 1·60 chains is a bord 2 to the right and left, holed each way; at 2·40 chains is a bord 3 to the right, 1 chain to the face, and to the left holed into the headways. Take the bearing and distance of Aa, which suppose S 80° W 1·60 chains: At 1·30 chains is a headways R to the right and left, and a mark * to return to. Take the bearing and distance of aG, which suppose S. 70° W. 1·80 chains: At 80 links is a headways b to the right, and a mark * to return to; and at 1·20 chains is a headways V to the left, and a mark + to return to. Take the bearing and distance of the headways RD (by fixing the instrument at the mark at R), which suppose S 8° W 2·50 chains: At 70 links is a bord 4 to the right and left, and holed each way; at 1·50 chains is a bord 5 to the right and left, and holed each

way. Take the bearing and distance of the headways VF (by fixing the instrument at the mark at V), which suppose

FIC 30
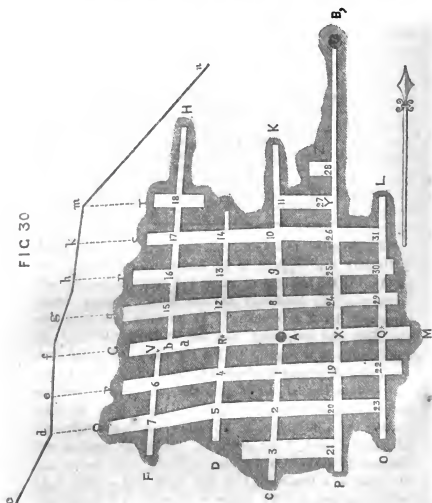
S 10° W 2·40 chains : At 80 links is a bord 6 to the right 1·30 chains to the face, and to the left holed into the headways ; at 1·60 chains is a bord 7 to the right 1 chain to the face, and to the left holed into the headways. Take the bearing and distance of the headways AK (by fixing the

instrument at A), which suppose N 10° W 4·20 chains : At 80 links is a bord 8 to the right and left, and holed into the headways each way ; at 1·70 chains is a bord 9 to the right and left, and holed into the headways each way ; at 2·50 chains is a bord 10 to the right and left, and holed into the headways each way ; at 3·30 chains is a bord 11 to the right, and holed into the headways,—and none to the left. Take the bearing and distance of the headways RI (by fixing the instrument at the mark at R), which suppose N 2° W 3 chains : At 80 links is a bord 12 to the right and left, and holed into the headways each way ; at 1·60 chains is a bord 13 to the right and left, and holed into the headways each way ; at 2·40 chains is a bord 14 to the right and left, and holed into the headways each way. Take the bearing and distance of the headways bH (by fixing the instrument at the mark at b), which suppose N 1° W 5 chains : At 80 links is a bord 15 holed into the headways to the right, and to the left 90 links to the face ; at 1·70 chains is a bord 16 holed into the headways to the right, and to the left 60 links to the face ; at 2·55 chains is a bord 17 holed into the headways to the right, and to the left 60 links to the face ; at 3·40 chains is a bord 18 to the right 50 links to the face, and to the left 55 links to the face. Take the bearing and distance of AM (by fixing the instrument at A), which suppose N 85° E 2·80 chains : At 1·30 chains is a headways X to the right and to the left, and a mark + to return to ; at 2·50 chains is a headways Q to the right and to the left, and a mark * to return to. Take the bearing and distance of the headways XP (by fixing the instrument at the mark X), which suppose S 5° E 3·10 chains : At 75 links is a bord 19 to the right and left, and holed into the headways each way ; at 1·60 chains is a bord 20 to the right and left, and holed into the headways each way ; at 2·40 chains is a bord 21 to the right, and holed into the headways,—and none to the left. Take the bearing and distance of the headways

QO (by fixing the instrument at the mark Q), which suppose
S 4° E 2·30 chains: At 80 links is a bord 22 to the right,
and holed into the headways, and to the left 40 links to the
face; at 1·60 chains is a bord 23 to the right, holed into the
headways,—and none to the left.   Take the bearing and
distance of the headways XYZB (by fixing the instrument
at the mark X), which suppose from X to Y N 2° W 2·80
chains: At 90 links is a bord 24 to the right and left, and
holed into the headways each way; at 1·70 chains is a bord
25 to the right and left, and holed into the headways each
way; at 2·60 chains is a bord 26 to the right and left, and
holed into the headways each.   Take the bearing and dis-
tance of YZ (by fixing the instrument at Y), which suppose
N 5° W 2 chains: At 60 links is a bord 27 to the left,
holed into the headways,—and none to the right; at 1·50
chains is a bord 28 to the left 30 links, and none to the
right.   Take the bearing and distance of ZB (by fixing the
instrument at Z), which suppose N 3° W 2·30 chains, to
a pit B.   Lastly, take the bearing and distance of the head-
ways QL (by fixing the instrument at the mark Q), which
suppose N 2° W 3·60 chains: At 80 links is a bord 29
to the left, holed into the headways, and to the right 30
links to the face; at 1 link is a bord 30 to the left, holed
into the headways, and to the right 20 links to the face; at
2·60 chains is a bord 31 to the left, holed into the headways,
and none to the right.—See the survey-book, where
the whole is recorded :—

SURVEY-BOOK.

A SURVEY OF A PIT'S WORKINGS, COMMENCING AT THE PIT A.

Bearings.	Remarks to Left.	Dist.	Remarks to Right.	
		Chains.		
S. 10° E.	. . . .	3·10	. . . .	AC
	Bord holed . .	0·80	Bord holed	
	Bord holed . .	1·60	Bord holed	
	Bord holed . .	2·40	Bord 1 chain from the headways	
S. 80° W.	. . . .	1·60	. . . .	Aa
	Headways . .	1·30	Headways	
	And a chalk mark * at R to return to			
S. 70° W.	. . . .	1·80	. . . .	aG
		0·80	A headways b, and a chalk mark * to return to	
	Headways V, and a chalk mark * to return to	1·20		
S. 8° W.	. . . .	2·50	. . . .	RD
	Bord holed . .	0·70	Bord holed	
	Bord holed . .	0·50	Bord holed	
	Returned to the mark * at V			
S. 10° W.	. . . .	2·40	. . . .	VF
	Bord holed . .	0·80	Bord 1·30 chain from the headways	
	Bord holed . .	1·60	Bord 1 chain from the headways	
	Returned to the pit A			
N. 10° W.	. . . .	4·20	. . . .	AK
	Bord holed . .	0·80	Bord holed	
	Bord holed . .	1·70	Bord holed	
	Bord holed . .	2·50	Bord holed	
	None . . .	3·30	Bord holed	
	Returned to the mark * at R			
N. 2° W.	. . . .	3·00	. . . .	RI
	Bord holed . .	0·80	Bord holed	
	Bord holed . .	1·60	Bord holed	
	Bord holed . .	2·40	Bord holed	
	Returned to the mark * at b			
N. 1° W.	. . . .	5·00	. . . .	bH
	Bord 90 links from the headways	0·80	Bord holed	
	Bord 60 links from the headways	1·70	Bord holed	

Bearings.	Remarks to Left.	Dist.	Remarks to Right.	
		Chains.		
	Bord 60 links from the headways	2·55	Bord holed	
	Bord 55 links from the headways	3·40	Bord 50 links from the headways	
	Returned to the pit A			
N. 85° E.	Headways	2·80		AM
	And a chalk mark * at X to return to	1·30	Headways	
	Headways	2·50	Headways	
	And a chalk mark * at Q to return to			
	Returned to the mark * at X			
S. 5° E.		3·10		XP
	Bord holed	0·75	Bord holed	
	Bord holed	1·60	Bord holed	
	None	2·40	Bord holed	
	Returned to the mark * at Q			
S. 4° E.		2·30		QO
	Bord 40 links from the headways	0·80	Bord holed	
	None	1·60	Bord holed	
	Returned to the mark * at X			
N. 2° W.		2·80		XY
	Bord holed	0·90	Bord holed	
	Bord holed	1·70	Bord holed	
	Bord holed	2·00	Bord holed	
N. 5° W.		2·00		YZ
	Bord holed	0·60	None	
	Bord 30 links from the headways	1·50	None	
N. 3° W.		2·30	To pit B	ZB
	Returned to the mark * at Q			
N. 2° W.		3·60		QL
	Bord holed	0·80	Bord 30 links from the headways	
	Bord holed	1·70	Bord 20 links from the headways	
	Bord holed	2·60	None	

Note.—When marks are made to be returned to in the survey, observe that they are returned to, otherwise the survey will be defective; and when the new method of taking the angles, given in Arts. 20 and 21, is adopted, the angles, thus taken, must be inserted instead of the bearings, the column being headed "angles" instead of "bearings."

The Back-Sight.

(18.) Suppose the bearing and distance of B from the pit A is required: Fix the instrument at B, instead of A (keeping the same sight foremost, and pointing towards b, when it is placed in the situation of B, as if it had been placed in the situation of A, for the purpose of taking the bearing of B); then apply the eye at the sight furthest distant from A, turning the same until the light at the pit A is cut by the perpendicular hair in the other; observe then the bearing of A from B, which, suppose S 30° E, on being reversed (see p. 17), will become N 30° W, for the bearing of B from A,—the distance, being measured, is found to be 3 chains; making the bearing and distance of B from A N 30° W 3 chains.

FIG 31

Bearings taken in this way are taken in a direction contrary to the order of the survey, and the eye is applied at the contrary sight to that which it would be applied when direct bearings are taken.

FIG 32

(19.) Suppose the bearing of ABCDFG and H is required, making use of the back-sight throughout the survey: Fix the instrument at B, instead of A, directing that sight towards A which, in the situation of A, would have been hindmost,
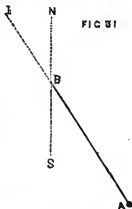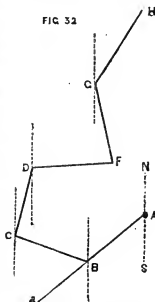
in the manner before directed; then the bearing A from B being found to be N 45° E, on being reversed makes S 45° W, the bearing of B from A, which enter into the survey-book. The instrument standing at B, turn that sight towards C which pointed to *a*, and take the bearing of C from B, which being found N 75° W, enter the same into the survey-book, without reversing, as it is not a backsight. Remove the instrument from B to D, and direct the sight back to C from D, in the same manner as from B to A: The bearing then of C from D being found S 10° W, which, being reversed, will be N 10° E, the bearing of D from C,—which enter into the survey-book. Then take the bearing of F from D, which being found N 80° E, enter the same into the survey-book, without reversing. Lastly, remove the instrument to G; then take the back-sight from G to F, which being found S 15° E, on being reversed will be N 15° W, the bearing of G from F,—which being entered into the survey-book, then take the bearing of H from G; which suppose N 30° E,—which enter also into the survey-book, without reversing, and the survey is finished.—By this mode of taking bearings, the instrument is only removed half the number of times it would otherwise be, were the back-sights not taken.

<div align="center">SURVEY-BOOK.</div>

The bearing of B from A, S. 45° W.
,,   C from B, N. 75° W.
,,   D from C, N. 10° E.
,,   F from D, N. 80° E.
,,   G from F, N. 15° W.
,,   H from G, N. 30° E.

PART II.

ON SURVEYING SUBTERRANEOUS EXCAVATIONS WITHOUT THE GENERAL USE OF THE NEEDLE.

IT has long been found that the conducting of subterraneous surveys requires strict attention in guarding against the presence of ferruginous substances, which exist in almost all mines, and which, it is well known, affect the magnetic needle, so as to cause it to give erroneous indications. On this account Mr. Fenwick was induced, as long ago as 1822 (when the second edition of his work was published), to suggest to the surveyor of mines the following new method, in which the needle has no control except in the first departure.

The use of the instrument.*

Suppose the subterraneous excavation ABCDEF to be surveyed begining at the pit A, and terminating at the pit F.

(20.) Place the instrument at B, and turning it until the vanes at zero cut the lighted candle at the centre of the pit A, which suppose N 65° E; and suppose AB to be 3 chains, the fixed sight at 0° still remaining as before; screw the instrument fast, and turn the moveable sights so as to cut a candle placed at C, taking care that the instru-

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* The improved Circumferentor, by Elliott Brothers, 30, Strand, London, which is still much used, especially in secondary mining surveys; but the modern improved theodolite is much to be preferred. See *Heather's Treatise on Mathematical Instruments, Weale's Series.*

ment has remained immovable. If so, read off the angle, which the index makes with the moveable circle, which sup-

FIG. 33.
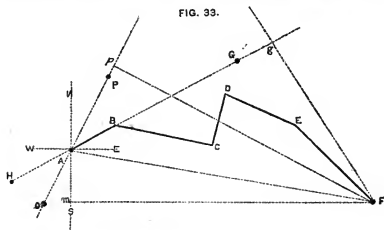
pose 120°; then the angle ABC is 120°, that is, the excavations BC and AB make an angle of 120°. Removing the instrument to C, turn the sights and index so as to cut the candle at B, keeping the instrument immovable; then turn the sights to the candle at D, reading off the angle BCD, which suppose 80°; and measure CB, which call 5 chains. Remove the instrument next to D, measuring the distance CD, which call 3 chains; and turn the sights and index to the candle at C, the instrument, as before, being kept immovable; turn the sights to the candle E, observe the angle CDE, which suppose 70°, and let the distance DE be 4 chains. Remove the instrument to E, and turn the sight and index to the candle at D, keeping the instrument immovable; turn the sight to the candle at E, and observing the angle DEF = 160°; lastly, measure the distance EF, which call 6 chains, and the survey is completed.

The following method of conducting subterraneous survey entirely without the use of the magnetic needle, was suggested by Mr. T. Baker (who has now made the present

additions and improvements to the new edition of Mr. Fenwick's "Subterraneous Surveying"), at least 35 years ago; but it was ridiculed by the then colliery surveyors; yet is now recommended and adopted by several scientific mining surveyors; among whom I may name Mr. H. Mackworth; who has given more elaborate details for conducting these surveys than those in the preceding article: Mr. M.'s improvements on Mr. Baker's suggestion are given in the following article.

(21.) To commence a survey without the magnetic needle, where there is only one shaft to the mine, the following plan should be adopted. Two thin copper wires, carrying heavy weights, must be suspended from a strong straight edge, at the surface of the shaft, and as near the edges of the shaft as not to touch them, the weights reaching nearly to the bottom of the shaft; while the weights must be immersed in buckets of water, or what would be still better, in vessels filled with mercury, to diminish oscillation, which will still continue, if the shaft is deep; but in the latter case, for only a very short time. The observer standing behind the wires must next send a candle along the heading, as far as it can be seen, and have it fixed in a line with the wires. He should repeat the operation in the opposite direction, by placing a candle against one of the wires, that the whole may be checked by seeing that the three candles are exactly in a line. This line being the basis of the whole underground survey, must be permanently marked by four or more pegs driven into the roof, with nails in them, or by marks on cross timbers or masonry. Returning to the surface, permanent pegs should be placed at some chains' distance, on each side of the shaft, in a line with the wires, as G and H (see last fig.) We then obtain a line on the surface exactly corresponding with the base line of our operation underground. The same process may be adopted, if there is more than one shaft to a mine; but it is not generally desirable to repeat it at more than one

shaft. A few hours' labour in getting the fundamental lines permanently fixed and connected, before commencing the survey, is afterwards well repaid.

The angular instrument used for this purpose ought to be the modern improved theodolite (see the foot-note to last article). Three tripods should be provided, and two lamps on stands, fitting on the tripod, of such a height that, when the lamp is replaced by the theodolite, the fulcrum of the axis of the telescope must be of the same height as the top of the wick in the lamp, a tripod with a lamp being placed under the centre of the shaft, at some well-marked station; the second tripod is fixed with the theodolite upon it, as far along the base-line as the light at the bottom of the shaft can be seen. The theodolite is clamped to zero. The third tripod with the other lamp on it, is sent as far forward as the light can be seen from the theodolite. The depth of the top of the wick in the first lamp below the top of the shaft having been ascertained, we carry on a series of levelling with the vertical arc of the theodolite all through the mine, at the same time as the horizontal angles and the measurement of the lines are taken. The telescope of the theodolite being directed to the top of the wick of the first lamp, the angle of elevation or depression is read. The lower limb being then clamped, and the upper relaxed, the horizontal angle is then read to the second lamp, and at the same time its angle of elevation or depression is read. The distance having been carefully measured, the first tripod is taken up, and carried forward beyond the third tripod, a lamp is placed on the second tripod, and the theodolite on the third tripod, when the observation of the angles are repeated as before.

(22.) The leading feature of Mr. A. Beauland's plan (see "Mining Surveys, Institute of Mining Engineers, Newcastle-upon-Tyne") consists in a method of fixing a bearing, or meridian line at the bottom of the pit, the direction of which is determined, either with reference to

the true meridian, or with respect to some line arbitrarily fixed on the surface, as PQ, fig. to Art. 20. By this means the underground survey can be commenced, and carried forward to any extent, by means of the theodolite, and is properly connected with the surface, the whole process being effected without the aid of the magnetic compass.

This method is Mr. B.'s own invention, or, at least, he is not aware that the idea has ever been carried out before, or has ever occurred to any one else, though of course it is quite possible that he may not be the first person who has thought of such a plan.

The process is effected by means of a powerful transit instrument, mounted in the line of the shaft, either at the top or bottom as may be most convenient. For simplicity, suppose the instrument to be at the top of the shaft. It is fixed and properly adjusted on a very firm support, which must be so arranged as not to interrupt the view of the telescope, when pointed vertically down the shaft.

Two marks are then fixed at the bottom of the pit, as nearly as may be in the same vertical plane as the transit, so that each of them can be seen through the telescope, and appear in the centre of the field of view. These marks are rendered visible by the light of a strong lamp reflected upwards, and are likewise so arranged that both can be seen by a theodolite placed at the bottom in a horizontal line with them. They are made as small as will allow of their being observed by the transit at the top, and are of such form that they can be bisected by the wires with great precision, the marks being as far apart as possible.

If now, on pointing the instrument downwards, each of the marks is exactly bisected by the middle wire, it is evident that the horizontal line, in which the marks are placed, coincides with the vertical plane of the instrument, and is, therefore, parallel to the position of the telescope when pointed horizontally. In this case, therefore, we have two lines, one at the top of the shaft, represented by

the optical axis of the telescope when pointed horizontally the other the line joining the centres of the two illuminated marks at the bottom, and the bearing of the instrument being determined, either with respect to the meridian, or to some determinate line, which can be connected with the surface survey, that of the line of direction of the marks below is ascertained at the same time.

This, however, is on the supposition, that each of the marks is seen precisely in the centre of the telescope. If this condition is not exactly fulfilled, the marks being a little out of the centre of the field of view, the apparent distance of each mark from the middle wire is accurately measured by a micrometer, or some other means, and from these distances, the angular deviation of the line of the marks from the plane of the instrument is determined by calculation. Having found the amount of this deviation, the bearing of the line of marks is at once deduced from that of the instrument, and the connection between the surface and underground survey, made as in the former case.

It is necessary, in order to complete the process, that permanent marks should be fixed above and below, the marks above ground being set out in some given direction, with respect to the plane of the telescope ; those below, with respect to the illuminated marks, which, as well as the instrument, must be removed from their places in the line of the shaft, before the colliery can resume working.

Wherever the nature of the ground, or erections on the surface, admit of it, marks may be placed at once in the direction of the instrument above being set out in any convenient positions, coinciding with the middle wire of the telescope. These permanent marks should of course be placed so that one of them can be seen from the other, it is also desirable to have them conveniently placed for the commencement of the surface survey.

Where, however, it is not practicable to set out a line in the direction of the transit, owing to obstructions, some

other direction must be taken, one mark being fixed in the line of the instrument, and the other at any point at a convenient distance, and visible from the first. The direction of the permanent line will, of course, be determined with respect to that of the transit, by setting up the theodolite at the nearer station, and measuring the angle between the direction of the transit and that of the further station.

The permanent marks fixed at the bottom of the pit are fixed in like manner, and their direction determined from that of the illuminated marks, by the aid of the theodolite, which is placed at some point near the shaft, in the line of the illuminated marks, and from which a more distant point can be seen. A permanent mark is then fixed at the place occupied by the theodolite, and another at the more distant point referred to, which may be chosen convenient for the commencement of the underground survey.

Mr. A. B. has thus endeavoured to explain, somewhat briefly, but he trusts with sufficient distinctness, the method by which the underground survey may be connected with the surface. It will scarcely be necessary for him to observe, that the whole process is one requiring great care, and an intimate acquaintance with the use and manipulation of the instruments, such as can scarcely be acquired without considerable expense. With proper management, however, and a transit of sufficient size and power, he believes the bearing may generally be fixed at the bottom of the pit without any error exceeding one minute of an arc, a degree of precision amply sufficient for all practical purposes.

On plotting subterraneous surveys.

(23.) Plotting may be divided into two kinds: *The first kind*, the communicating of bearings and distances of a subterraneous survey to paper, for the purpose of planning the same ; *the second kind*, the manner of running on the surface of the earth the different bearings or angles and distances, in the same order as they were taken under-

ground in the survey. In the first mode, the protractor, for setting off the angles contained in each bearing, and a scale of chains and links, for transferring the distances, are requisite; and in the second mode, the circumferentor or theodolite, and Gunter's chain. Observe, in running off the bearings on the surface, that the same instrument be made use of as in the subterraneous survey; and also let the same end of the needle, when used, determine the angles of the bearings as determined them under-ground. This last precaution is not necessary when the magnetic needle is not used.

(24.) Let ABCD represent a protractor, which is a circular rim of brass, and E its centre, of about 9 inches

FIG. 34.
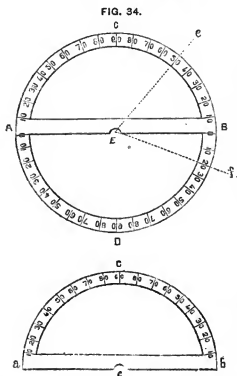
diameter, divided into degrees, and each degree in quarters of a degree, commencing from the north and south points A and B and numbered up to 90° at C and D. Also *abc* represents a semicircular protractor, which for many purposes, is more commodious than the circular one, *ab* representing the meridian, and *e* its centre. These instruments are manufactured by Messrs. Elliott Brothers, 30, Strand, London.

In using this instrument in plotting bearings, the meridian line AB or *ab*,

must be applied to the assumed meridian line drawn on paper; and if a line E*e* is drawn from the centre E, through the 50th degree or division from B to C, supposing AB the meridian, A the north, and B the south; then E*e* will be N 50° W (see theorem 17), and the line E*f* passing through the 20th degree or division, will be N 20° E.

(25.) Suppose the following bearings and distances to be plotted on paper—

AB, N. 45° W.	. . .	10 chains.
BC, N. 10° E.	. . .	7 ,,
CD, S. 50° E.	. . .	6 ,,

Proceed thus:—

Draw the meridian line NS on the paper where the work has to be plotted, N for north, and S for south; then fix on any place on that meridian line for the commencement of the work, as at the pit A; apply the meridian line AB of the protractor on the assumed meridian, with its centre E on A; let *nesw* represent the protractor, *n* corresponding with N the north, and *s* with S the south,—*e* will represent the east, and *w* the west; then draw the line AB from the centre of the protractor at A through the 45th degree from *n* towards *w*, or west, and it will represent N 45° W: Also from the scale of chains take 10 with the compasses, and setting the same from A to B, and AB will represent the first bearing and distance N 45° W, 10 chains: by the assistance of a parallel ruler, or any other method, draw the second meridian line *ns*, through B, parallel to that drawn through A; apply the protractor

FIG. 55.

D
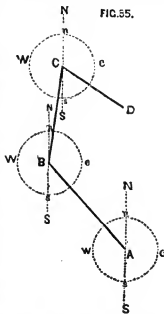
as before directed, with its centre on the point B; draw
the line BC from the centre of the protractor at B,
through the 10th degree from *n* towards *e*, and it will
represent N 10° E: Then from the scale of chains take 7
with the compasses, setting the same from B to C, and BC
will represent the second bearing and distance; then draw
the third parallel line *ns* through C; apply the protractor
as before, with its centre on C; draw the line CD through
the 50th degree from *s* towards *e*, and it will represent
S 50° E: Then take 6 chains from the scale, setting the
same from C to D, and CD will represent the third bearing
and distance;—and the whole will be plotted.

Note.—The student ought now to lay down on paper the several surveys,
commencing at Art. 12, not only by the old method of bearings, taken by
the magnetic needle, but also by the modern and more accurate methods,
given in Arts. 20, 21, and 22 (the methods given in the several articles
not differing materially except at the commencement of the surveys), that
he may thus acquire a skilful and ready method of performing this impor-
tant part of his profession. See the following article.

(25a.) Let the following angles and distances, taken in a
coal-mine, be laid down on paper (see fig. to Art. 20).

Let NS be the true meridian, obtained by making proper
allowance for the magnetic *variation*; and let the following
distances be measured, and angles be taken in a coal-mine
as below :—

DISTANCES.		ANGLES.	
AB =	3·12 chains.	NAB =	64° 39′
BC =	4·96 ,,	ABC =	118° 19′
CD =	2·89 ,,	BCD =	79° 15′
DE =	4·17 ,,	CDE =	61° 5′
EF =	6·02 ,,	DEF =	158° 57′

Draw the meridian line NS, N representing the north
point, and let A in the line NS be the pit where the work
is to commence; lay off from the meridian line NS by the
protractor, the angle NAB = 64° 39′, in the manner already
directed; and from a scale of equal parts, lay off the dis-

tance AB = 3·12 chains, and extend the line, if necessary; next apply the line AB of the protractor on the line AB on the plan, the centre E of the protractor being applied to the angular point B: then lay off the angle ABC = 118° 19'; and the distance BC = 4·96 chains; apply the protractor to the line BC, as before directed, lay off the angle BCD = 79° 15', and the distance CD = 2·89 chains: lay off successively the angles CDE = 61° 5' and DEF = 158° 57', and the distances DE = 4·17 and EF = 6·02 chains; and the work will be completed, being a correct representation of the survey made in the mine.

Next plot the surveys, given in Arts. 17, 18, and 19, by laying off the successive angles, as directed in Arts. 20 and 21, the bearings being previously reduced to the angles, which every two successive distances make with one another by Art. 6.

Note.—In the second column of the survey-book to Art. 17, the angles NAB, ABC, &c., must be entered, as shown in this article.

Suppose the following subterraneous survey is to be plotted by the application of the T square:—

N. 54° W. . . . 10 chains.
S. 42° W. . . . 7   ,,
N. 30° W. . . . 6   ,,

(26.) On the drawing-board, or table ABCD, fix the paper *abcd*, on which the survey is to be plotted, and let SN represent the T square applied thereon, which also represents the magnetic meridian (N the north and S the south). Fix upon the point *f* for the commencement of the work; apply the straight edge of the semicircular protractor *sn* against the arm of the T square NS, with its centre on the point *f*; then draw the line *fg* through the 54th degree of the protractor from north to west, setting off the distance 10 chains from *f* to *g*: Then *fg* is the first

bearing and distance N 54° W 10 chains. Remove the T
square along the line AC until its arm SN meets the point
g, where it represents the magnetic meridian; then apply

FIG 36

the protractor as before-
directed, with its centre
on *g*; draw the line *gh*
through the 42nd degree
from south to west, setting
off the distance 7 chains
from *g* to *h* : and *gh* is the
second bearing and distance
S 42° W, 7 chains. Re-
move again the T square
until its arm SN meets
the point *h*, representing
there the magnetic meridian; then apply the protractor
with its centre on *h*; draw the line *hk* through the
30th degree from north to west, setting off the distance
6 chains from *h* to *k* : And *hk* is the third and last bearing
and distance N 30° W, 6 chains. The work being finished,
take the paper off the board.

(27.) In the following subterranean survey *fghk* (see
Fig. to last Article), I wish to know, by one single bearing
and distance, the situation of *k* from *f*?

fg,	N. 54° W.	.	10 chains.
gh,	S. 42° W.	.	7 „
hk,	N. 30° W.	.	6 „

Protract the survey on the paper fixed to the drawing-
board, as before-directed; then draw a line from *f* to *k* ;
move the arm of the T square until it touches *f*, forming
therewith the magnetic meridian; then apply the protractor
with its centre at *f*, observing what division or degree the
line *fk* cuts which will be found to be the 71st nearly,
which is the magnitude of the angle N*fk* : Measure the
distance to *k* from *f* by the same scale as the work was

plotted from, which distance is found to be 16·70 chains; then from rule, Art. 4, the bearing of k from f will be found to be N 71° W, and its distance 16·70 chains.

(28.) In the following survey of the subterraneous working ABCDF (see Fig. to Art. 16), driven from the pit A towards G, I wish to know the bearing that the workmen must proceed in from F to hit the pit G, and likewise the distance between F. and G ?

Plot the survey from the given data in Art. 16, by the use of the T square; also by laying off the several angles, as directed in Arts. 20 and 21, which will verify the survey.

Then the bearing of the pit G from F, from rule, Art. 4, will be S 65° 30′ E. Measure the length of the line FG by the same scale of equal parts as the work was protracted from—which is found to be 8·60 chains; hence the bearing and distance of the subterraneous working from F, to hit the pit G, must be S 65° 30′ E 8·60 chains.

ANOTHER METHOD.

Which may be thought more eligible than the preceding ; for if any error is made in this method of plotting, it only affects the particular part where it occurs, and is not carried throughout the remaining part of the work, as in the other methods already described.

(29.) Suppose the following survey to be plotted according to this method :—

		Chains.
AB, S. 36° E.	. . .	7·00
BC, S. 42° W.	. . .	4·00
CD, S. 75° W.	. . .	10·00
DF, N. 42° W.	. . .	7·50

Prepare the survey by taking the northing, southing, easting and westing of all the bearings therein (see Art 10, ex. vii.), placing each separately in its respective column, in the following preparatory table : Thus the bearing and

distance AB, S 36° E, 7 chains, will, from the traverse
tables, contain 5·66 chains of southing, and 4·12 chains of
easting ;—and so of all the rest.

The next thing is to determine the northing and south-
ing of the bearings conjointly, from A the point of com-
mencement of the survey: Thus let NS represent the
magnetic meridian of A, the southing of the bearing AB
S 36° E, 7 chains is 5·66 chains A*a* ; which place in the 6th
column of the preparatory table. The southing of the bear-
ing BC, S 42° W, 4 chains is 2·97 chains *ab*, which, being
added to 5·66 chains, makes 8·63 chains A*b* for the south-
ing of the bearings ABC; which place in the 6th column:
The southing of the bearing CD S 75° W, 10 chains is 2·59

FIG 37
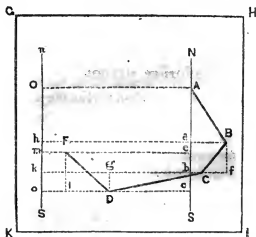
chains *bc*, which, being added to 8·63 chains, makes 11·22
chains A*c* for the southing of the bearings ABCD; which
place in the 6th column: The next, DF, N 42° W 7·50
chains, will produce 5·55 chains of northing *ce* from D, which,
being subtracted from 11·22 chains, leaves 5·67 chains A*e*,
the southing of the bearings ABCDF from the commence-
ment A : Then determine the easting and westing distance of

the end of each bearing from the assumed meridian of the point A, or point of commencement. The easting of the bearing AB, which is S 36° E, 7 chains from NS, the assumed meridian, will be found by the traverse tables to be 4·12 chains aB; which place in the 7th column of the following table: The westing of the bearing S 42° W, 4 chains from B will be found to be 2·68 chains fC, which, taken from the easting aB or bf 4·12 chains, leaves 1·44 chains, bC for the easting of the bearings ABC from NS, the assumed meridian of A: The westing of the bearing S 75° W, 10 chains from C will be found to be 9·66 chains Cg, from which take 1·44 chains of easting bC, leaves bg or cD 8·22 chains for the westing of the bearings ABCD from NS: The westing of the bearing N 42° W, 7·50 chains from D will be found to be 4·97 chains Dl, which, being added to 8·22 chains cD, makes cl or eF 13·19 chains for the westing of the bearings ABCDF from NS. Now, to prepare the survey for plotting, the next thing is to assume another meridian, which shall be to the west of the westmost bearing of the survey from NS; and from this second meridian find the easting of the end of each bearing from it (see the 8th column of the table). The greatest westing of the bearing from NS is eF, or cl 13·19 chains: Suppose, then, this second assumed meridian line to be ns 14 chains AO west of the first meridian line NS, place the 14 chains at the top of the 8th column of the following table, which is the distance that the point A is eastward of ns: Then 14 chains ha + 4·12 chains aB = 18·12 chains hB, the distance that B is east of ns; which place in the 8th column: Then 14 chains + 1·44 chains bC = 15·44 chains kC, the easting of C from ns: Then 14 chains — 8·22 chains cD = 5·78 chains oD, the easting of D from ns: Lastly, 14 chains — 13·19 chains eF = 81 links mF, the easting of F from ns; which, being all entered in the 8th column of the following table, the survey will be prepared for plotting.

PREPARATORY TABLE.

	1.	2.	3.	4.	5.	6.	7.	8.
	Bearings and Distances.	Northing.	Southing.	Easting.	Westing.	Northing and southing distance from A.	Easting and westing distance from the meridian of A.	Easting distance of each bearing from the second meridian az.
	Chains.	Chains.	Chains.	Chains.	Chains.	Chains.	Chains.	Chains.
AB	S. 36° E. 7·00	...	Aa 5·66	aB 4·12	...	Aa 5·66 S.	aB 4·12 E.	OA 14·00 E. AB 18·12 E.
BC	S. 42° W. 4·00	...	ab 2·97	...	fC 2·68	Ab 8·63 S.	bC 1·44 E.	KC 15·44 E.
CD	S. 75° W. 10·00	...	bc 2·59	...	Cg 9·66	Ac 11·22 S.	cD 8·22 W.	oD 5·78 E.
DF	N. 42° W. 7·50	ee 5·55	...	...	Dι 4·97	Ae 5·67 S.	eF 13·19 W.	mF 0·81 E.

N.B. The seventh column of the table is only preparatory to the eighth.

In order to plot the survey, fix the paper on the drawing-board or table G H I K ; then draw the meridian line *ns* by the application of the T square, *n* representing the north and *s* the south ; let O be the point for the commencement of the work, and from the 6th column of the table set off the different southings ; 1st, 5·66 chains A*a* from O to *h*, being the southing of the bearing AB ; 2dly, 8·63 chains A*b* from O to *k*, the southing of the bearings and distances AB and BC ; 3rdly, 11·22 chains A*c* from O to *o*, the southing of the bearings and distances AB, BC, and CD ; and 4thly, 5·67 chains A*e* from O to *m*, the southing of the bearing and distances AB, BC, CD, and DF. This being done, apply the T square to the side G K, its arm crossing the meridian line *ns* at right angles ; then from the 8th column of the table set off 14 chains of easting from O to A, and A denotes the place of commencement of the survey, or point of departure : Move the T square down the side G K until its arm comes to *h* : then set off 18·12 chains of easting from *h* to B, draw the line AB, and it represents the first bearing and distance ; move the T square until the arm comes to *k*, then setting off 15·44 chains of easting from *k* to C, draw the line BC, and it represents the second bearing and distance ; move the T square to *o*, then setting off 5·78 chains of easting from *o* to D, draw the line CD, and it represents the third bearing and distance ; move the T square to *m*, then setting off 81 links of easting from *m* to F, draw the line DF, and it represents the fourth and last bearing and distance. Then the whole survey will be plotted.

Next plot this survey from the given data by laying off the several angles as directed in Arts. 20 and 21, the bearings being previously reduced to the angles which the successive distances make with one another by Art. 6 ; also plot the surveys, given in Arts. 30 and 31, in the same manner.

(30.) Suppose the following subterraneous survey to be plotted, beginning at the pit A :—

FIG. 38.
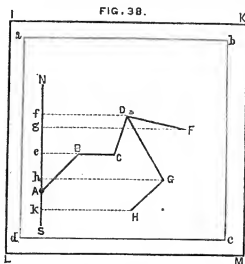
	Chains.
AB, N. 42° E.	5·00
BC, E.	4·00
CD, N. 9° E.	4·00
At 4 chains is a mark	
* to return to.	
DF, S. 69° E.	5·66
Returned to mark *.	
DG, S. 36° E.	7·00
GH, S. 42° W.	4·00

Prepare the survey for plotting, by taking the northing, southing, easting, and westing of each bearing from the traverse tables.

The northing and easting of the first bearing and distance N 42° E, 5 chains, will be northing 3·72 chains, and easting 3·35 chains (which see in the following preparatory table, together with the northing, southing, easting, and westing of all the others). Then find the northing and southing of the bearings conjointly from the commencement of the survey at the pit A, — which is had from the 2nd and 3rd column of the table : The northing of the first bearing and distance will be found to be 3·72 chains ; which place in the 6th column of the table : That of the second bearing and distance will be also 3·72 chains ; that of the third, 3·72 chains + 3·95 = 7·67 chains ; and so of all the rest.   Also take the easting and westing of each bearing and distance from the meridian of the pit A, — which is had from the 4th and 5th column of the table : The easting of the first bearing and distance will be found 3·35 chains ; which place in the 7th column of the table : That of the second will be 3·35 + 4 chains = 7·35 chains of easting ; and so of all the

PREPARATORY TABLE.

	1. Bearings and Distances.	2. Northing.	3. Southing.	4. Easting.	5. Westing.	6. Northing and southing distance from A.	7. Easting and westing distance from the meridian of A.	8. Easting distance of each bearing from the meridian of A.
		Chains.	Chains.	Chains.	Chains.	Chains.	Chains.	Chains. mark *
AB	N. 42° E. 5·00	3·72	...	3·35	...	3·72 N.	3·35 E.	3·35 E.
BC	E. 4·00	...	...	4·00	...	3·72 N.	7·35 E.	7·35 E.
CD	N. 9° E. 4·00	3·95	...	0·63	...	7·67 N.	7·98 E.	7·98 E.
DF	S. 69° E. 5·66	...	2·00	5·21	...	5·67 N.	13·19 E.	13·19 E.
	Returned to the mark +							
DG	S. 36° E. 7·00	...	5·66	4·12	...	0·01 N.	13·31 E.	17·31 E.
GH	S. 42° W. 4·00	...	2·97	...	2·68	2·96 S.	14·63 E.	14·63 E.

rest: As from the 8th column of the table the end of each
bearing in the survey will be east of the meridian NS of A;
therefore no other need be assumed.

Fix the paper *abcd* on the drawing-board or table IKLM;
draw a meridian line NS by the application of the T square,
and mark A for the pit, and commencement of the work;
then make a mark with the compasses at *e*, on the meridian
line NS, 3·72 chains to the north of A (from the 6th column
of the table),—which is the northing of the first and second
bearing and distance: Make another at *f*, 7·67 chains from
A to the north; another at *g*, 5·67 chains; another at *h*, 1
link to the north of A; and another at *k*, 2·96 chains to the
south of A: This being done, apply the T square to the
side LI, its arm crossing the meridian NS at right angles,
and corresponding with *e*; then set off from *e* to B, 3·35
chains of easting to the right (from the 8th column of the
table), which is the easting of the first bearing and distance:
Draw a line from A to B, and AB represents the first bearing
and distance: Also set off from *e* to C, 7·35 chains to the right,
and draw the line BC: Remove the arm of the T square to
f, and set off from *f* to D 7·98 chains to the right, and draw
the line CD; there make a mark * to return to: Remove
the T square to *g*, and set off from *g* to F 13·19 chains to
the right, and draw the line DF: Remove the T square to
h, and set off from *h* to G 17·31 chains to the right, and
draw the line DG from the mark at D: Remove the T
square to *k*, and set off from *k* to H 14·63 chains to the
right, and draw the line GH;—and ABCDFGH will repre-
sent the survey protracted.

(31.) An example showing that an error, committed
during the time of plotting the survey after this method,
is not communicated to the following part of the work:—

Suppose the subterranean survey ABCDF is required
to be plotted.

FIG 59

	Chains.
AB, S. 36° E. . .	7·00
BC, S. 42° W.. .	4·00
CD, S. 75° W.. .	10·00
DF, N. 42° W.. .	7·50
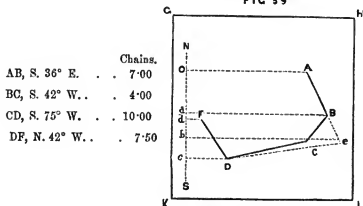
(For Preparatory Table see next page.)

Fix the paper on the drawing-board GHIK, and draw the
assumed meridian NS 14 chains west of the meridian of A,
which exceeds the greatest westing in the 6th column; let
O be the point thereon for the commencement of the work:
Set off, from the 6th column of the table, the different
southings from O to *a b c,* and *d* respectively; and from the
8th column of the same table set off the different eastings
from O to A, from *a* to B, from *b* to C, from *c* to D, and
from *d* to F; and ABCDF will represent the survey truly
plotted. Now, suppose the plotter, in laying down the
eastings in the 8th column of the table, commits an error,
by setting off from the assumed meridian 25·44 chains *be,*
instead of 15·44 chains *b*C, then the point C will be
removed to *e,* and BC will be represented by B*e,* and CD
by *e*D; therefore it appears, from inspecting the figure,
that the error will cease at D, and the following bearings,
be there ever so many, will be each in the same situation as
if no such error had ever existed; which is a peculiar advan-
tage in this mode of plotting.

PREPARATORY TABLE.

	1.	2.	3.	4.	5.	6.	7.	8.
	Bearings and Distances.	Northing.	Southing.	Easting.	Westing.	Northing and southing distance from A.	Easting and westing distance from the meridian of A.	Easting distance of each bearing from the assumed meridian NS.
	Chains.	Chains.	Chains.	Chains.	Chains.	Chains.	Chains.	Chains.
A								14·00 E.
AB	S. 36° E. 7·00	...	5·66	4·12	...	5·66 S.	4·12 E.	18·12 E.
BC	S. 42° W. 4·00	...	2·97	...	2·68	8·63 S.	1·44 E.	15·44 E.
CD	S. 75° W. 10·00	...	2·59	...	9·66	11·22 S.	8·22 W.	5·78 E.
DF	N. 42° W. 7·50	5·55	...	...	4·97	5·67 S.	13·19 W.	0·81 E.

*The manner of reducing any number of bearings and distances
into one bearing and distance.*

(32.) The practical miner will frequently find it necessary to have recourse to this mode of reduction in the plotting of subterraneous surveys on the surface, for the purpose of determining their extent. As when the circumferentor is the only instrument used in such works, which in windy weather is both troublesome and fallacious, therefore, if the whole survey can be reduced to one bearing and distance, or to such a number as may be thought necessary, the labour of protracting will be proportionally reduced, and the work more to be depended on.

Suppose the following subterraneous survey ABCDF, to be reduced to one single bearing and distance from A to F:—
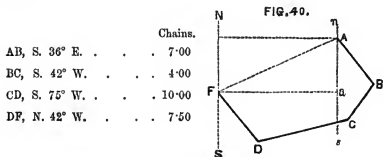
FIG. 40.

	Chains.
AB, S. 36° E. . . .	7·00
BC, S. 42° W. . . .	4·00
CD, S. 75° W. . . .	10·00
DF, N. 42° W. . . .	7·50

THE PREPARATORY TABLE.

		Northing.	Southing.	Easting.	Westing.
	Chains.	Chains.	Chains.	Chains.	Chains.
AB, S. 36° E.	7·00	...	5·66	4·12	...
BC, S. 42° W.	4·00	...	2·97	...	2·68
CD, S. 75° W.	10·00	...	2·59	...	9·66
DF, N. 42° W.	7·50	5·55	...	...	4·97
		5·55	11·22	4·12	17·31
			5·55		4·12
		NF or		NA or	
		Aa	5·67	Fa	13·19

By taking the northings from the southings, leaves 5·67 chains of southing of F from A; and by taking the eastings from the westings, leaves 13·19 chains of westing of F from the meridian of A, which form the triangle NAF; of which NA 13·19 chains, NF 5·67 chains, and the right ∠ N, are given, to find the side AF and ∠ NAF, which is done by trigonometry, as follows :—

As NA 13·19	1·120245
Is to radius	10·000000
So is NF 5·67	·753583
To tang. ∠ NAF 23° 15′ . .	9·633338
And as sine ∠ A 23° 15′ . .	9·596315
Is to NF 5·67	·753583
So is radius	10·000000
To AF 14·36	1·157268

Or AF may be found thus :—Euclid, b. 1, p. 47,

$$\sqrt{\overline{13·19}^2 + \overline{5·67}^2} = 14·36 \text{ chains} = \text{AF}.$$

Then 90° — 23° 15′ = 66° 45′ ∠ FAs. Therefore the bearing and distance of F from A is S 66° 45′ W, 14·36 chains.

Or the bearing and distance may be found instrumentally, if protracted on paper, by applying the protractor to the meridian line *ns*, with its centre on the angular point A, observing the magnitude of the ∠ FAs, which will be found 66° 45′; and, from theorem 17, the line AF will bear S 66° 45′ W. The distance may be measured by the scale and compasses.

(33.) In a subterraneous survey ABCDF, commencing at the pit A, I wish to have the direct bearing and distance on the surface of F from A ?
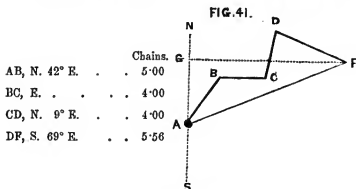
FIG. 41.

AB, N. 42° E.	.	.	.	5·00
BC, E.	.	.	.	4·00
CD, N. 9° E.	.	.	.	4·00
DF, S. 69° E.	.	.	5·56

PREPARATORY TABLE.

	Northing.	Southing.	Easting.	Westing.
	Chains.	Chains.	Chains.	Chains.
N. 42° E. 5·00	3·72	...	3·35	...
E. 4·00	...	...	4·00	...
N. 9° E. 4·00	3·95	...	0·63	...
S. 69° E. 5·56	...	2·00	5·21	...
	7·67	2·00	13·19	
	2·00			
	5·67			

Now the point F contains 5 chains 67 links of northing AG, and 13·19 chains of easting GF, from the commencement A of the survey: Therefore construct the triangle AGF, the line NS representing the meridian, N the north, and S the south; AG being given 5·67, and also GF 13·19, and the right ∠ G, to determine AF and the ∠ NAF.

$\sqrt{\overline{13·19}^2 + \overline{5·67}^2}$ = 14·36 AF, or the distance of F from A.

As AG 5·67	.	.	.	.	·753583
Is to radius	.	.	.	10·000000
So is GF 13·19	.	.	.	1·120245
To tang. ∠ A 66° 45′ .	.	.	10·366662

Therefore the bearing and distance of F from A is N 66° 45′ E, 14·36 chains; and if that bearing and distance is

run off by a circumferentor and chain, on the surface from A, it will determine the point thereon immediately vertical to the point F in the subterraneous excavation.

Also, if the different bearings and distances ABCDF are protracted on paper, on which the triangle AGF is constructed, beginning at the point A, and making the side AG the meridian, the end of the last bearing and distance DF will coincide with the angular point F of the triangle, if the survey is rightly protracted.

(34.) In the subterraneous survey ABCDFGH, commencing at the pit A, I wish to know the direct bearing and distance of the point D from A, and also the direct bearing and distance of the point H from A, so that a pit may be put down from the surface on each of those points?

FIG. 42

	Chains.
AB, N. 42° E.	5·00
BC, E.	4·00
CD, N. 9° E.	4·00
DF, S. 69° E.	5·56
FG, S. 36° E.	7·00
GH, S. 42° W.	4·00

(See Preparatory Table opposite.)
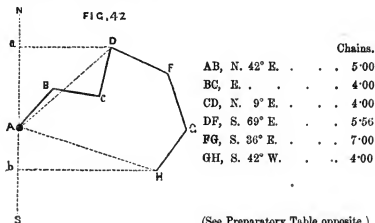
The point D has from A 7·67 chains of northing Aa, and 7·98 chains of easting aD; and the point H has from A 2·96 chains of southing Ab, and 14·63 chains of easting bH.

Construct the triangle AaD, and let Aa represent 7·67 chains of northing, and aD 7·98 chains of easting; also construct the triangle AbH, and let Ab represent 2·96 chains of southing, and bH 14·63 chains of easting: The side AD

PREPARATORY TABLE.

				Northing.	Southing.	Easting.	Westing.
		· Chains.		Chains.	Chains.	Chains.	Chains.
N.	42°	E.	5·00	3·72	...	3·35	...
R.	.	.	4·00	...	...	4·00	...
N.	9°	E.	4·00	3·95	...	0·63	...
				7·67		7·98	
S.	69°	E.	5·56	...	2·00	5·21	...
S.	36°	E.	7·00	...	5·66	4·12	2·68
S.	42°	W.	4·00	...	2·97	...	...
				7·67	10·63	17·31	2·68
					7·67	2·68	
					2·96	14·63	

and ∠ NAD is required in the former triangle, and the side AH and ∠ SAH in the latter.

Then, as A*a* 7·67 .	.	·834795
Is to radius	.	10·000000
So is *a*D 7·98	.	·902003
To tang. ∠ A 46° 8′	.	10·017208

$$\overline{2} \quad \overline{2}$$

And √ 7·67 + 7·98 = 11·06 AD.

Therefore the bearing and distance of a pit from A on the surface, to hit the point D under-ground, will be N 46° 8′ E, 11·06 chains.

Also, as A*b* 2·96 .	.	·471292
Is to radius	.	10·000000
So is *b*H 14·63	.	1·165244
To tang. ∠ A 78° 33′	.	10·693952

$$\overline{2} \quad \overline{2}$$

And √ 14·63 + 2·96 = 14·92 AH.

Consequently the bearing and distance of a pit from A

on the surface, to hit the point H under-ground, will be S 78° 33′ E, 14·92 chains.

(34a.) In the subterraneous survey ABCDEF, commencing at the pit A, it is required to find the direct bearing and distance of the point F from A, so that a pit may be sunk from the surface to the point F (see Fig. to Art. 20), the required bearing being taken both from the meridian NS, and also from a well defined line GH, passing through the fixed marks G and H and the shaft A, and corresponding to a line in the headway AB, determined in the manner pointed out in Articles 21 and 22.

Let the distances be measured, and the angles be taken by the theodolite as below :—

Distances.		Angles.	
AB	= 3·12 chains.		
BC	= 4·96 ,,	ABC	= 118° 34′
CD	= 2·89 ,,	BCD	= 79° 15′
DE	= 4·17 ,,	CDE	= 61° 5′
EF	= 6·02 ,,	DEF	= 158° 57′

Reduce the angles at B, C, D and E to their bearings from GH by Art. 3; then find the northing or southing and the easting or westing from the Traverse Table by Art. 59; then proceed as in Art. 34 to find Ag and Fg; whence by trigonometry, as shown in the last-named Article, the bearing of F from the fixed line GH, and the distance AF, will be readily found.

Next reduce the angles A, B, C, D and F to their bearing from NS, then find the northing or southing and easting or westing from the Traverse Table, and proceed as in Art. 34 to find Am and Fm; whence by trigonometry, as already shown, the bearing of F from the meridian NS and the distance AF will be found.

Or the bearings and distance in both cases may be found from the plan by measuring the angles GAF and NAF with the protractor, and the distance AF by the same scale

of equal parts as that with which the plan was laid down.
By doing the work by all these methods its accuracy may
be further verified.

It would conduce much to the improvement of the
student to plot the surveys in the following Articles 35 and
36, by reducing the given bearings to the angles made by
every two successive lines in each example, as practice of
this kind will impart great facility in the exercise of his
profession; and besides, enable him to reason for himself
and not on every slight occasion to have recourse to
authors.

(35.) In the following subterraneous working ABCDF,
beginning at the pit A, I wish to know the bearing and
distance of the pit G from F, the bearing and distance of
G from A being given:—

FIG. 43.

AB, S. 30° W.	. .	4·00
BC, N. 50° W.	. .	8·00
CD, N. 50° E.	. .	9·00
DF, N. 53° W.	. .	8·00
AG, N. 20° E.	. .	24·00
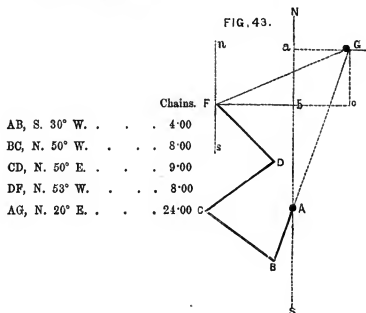
PREPARATORY TABLE.

	Chains.	Northing. Chains.	Southing. Chains.	Easting. Chains.	Westing. Chains.	
S. 30° W.	4·00	...	3·46	...	...	
N. 50° W.	8·00	5·14	...	...	6·13	
N. 50° E.	9·00	5·79	...	6·89	...	
N. 53° W.	8·00	4·81	...	...	6·39	
		15·74	3·46	6·89	14·52	
		3·46			6·89	
		12·28	Ab		7·63	bF
N. 20° E.	24·00	22·55	Aa	8·21	aG or bc	
		10·27				

Then Aa 22·55 chains — Ab 12·28 chains = 10·27 chains ba or cG, and Fb 7·63 chains + aG or bc 8·21 chains = 15·84 chains Fc.

The $\angle$ nFG, or bearing of the line FG from the magnetic meridian ns, and the length of FG are both wanted; and the sides Fc, cG, and the right $\angle$ c are given to find them.

$$
\begin{array}{lll}
\text{As F}c\ 15·84 & . \quad . \quad . & 1·1997552 \\
\text{Is to radius} & . \quad . \quad . & 10·0000000 \\
\text{So is G}c\ 10·27 & . \quad . \quad . & 1·0115704 \\
\text{To co-tang.}\ \angle\ \text{F } 57°\ 3' & .\ \underline{\quad\quad} & 9·8118152
\end{array}
$$

Which will be N 57° 3' E with the magnetic meridian ns.

Also $\sqrt{\overline{15·84}^2 + \overline{10·27}^2} = 18·87$ FG.

Therefore the bearing of the pit G from F will be N 57° 3' E, and the distance 18·87 chains.

Plotting on the surface by the circumferentor, or theodolite.

(36.) In this mode of plotting the bearings and distances are run off on the surface of the earth in the same order as taken in the subterraneous survey. Great care must be taken in running the length of each bearing as nearly horizontal as can be, where the surface is uneven and declining.

—The first two examples show the different modes of commencing the plotting of a survey on the surface, by assuming a point to begin at; and the others following show the manner of avoiding an obstacle, as a house, a lake, or any other thing that interferes with the line of survey.

Let the following subterraneous survey be plotted on the surface, commencing at the centre of the pit A:—

	Chains.
S. 45° W. . . .	6·00
S. 80° W. . . .	6·00
N. . . .	5·00
N. 70° E. . . .	4·00
N. 20° E. . . .	10·00

FIG. 44.
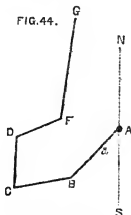
Fix the instrument as near the pit A as convenience will allow; (observe to keep the same end of the instrument first in the plotting of the survey as was first in making it under-ground; likewise the same end of the needle must determine the bearings in the plotting as determined them under-ground). Suppose *a* the place where the instrument is fixed, which is such a situation that, when the fore-sight is put in the direction of the first bearing, S 45° W, you may, by looking backward from *a*, cut exactly the centre of the pit A, the commencement of the survey,—otherwise the instrument is not placed in a proper situation. (This first point A is obtained by shifting the instrument either to the right or left, until it is in the situation before-mentioned.)— After the proper situation of the commencement of the survey is found, let the assistant take the chain, and running 6 chains from the centre of the pit A, which

suppose to extend to B, then AB is the first bearing and distance plotted. Remove the instrument to B, and put the fore-sight in direction of S 80° W, measuring the distance from B to C 6 chains; then BC is the second bearing and distance. Remove again the instrument to C, and put the foresight in direction of due north, measuring the distance from C to D 5 chains; then CD is the third bearing and distance. Remove again the instrument to D, and put the fore-sight in direction of N 70° E, measuring from D to F 4 chains; then DF is the fourth bearing and distance. Lastly, remove the instrument to F, and putting the fore-sight in direction of N 20° E, measure 10 chains from F to G; then FG is the fifth and last bearing and distance. If marks are made at B, C, D, F and G, they will represent on the surface the excavation with all its windings.

(37.) Suppose the following subterraneous survey ABCDF, to be plotted on the surface, commencing at the centre of the pit A :—

FIG. 45.
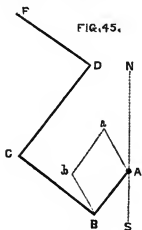
	Chains.
S. 30° W.	4·00
N. 50° W.	8·00
N. 50° E.	9·00
N. 53° W.	8·00

Instead of following the same mode of commencement, as shown in the former example, make any place on the surface the point of commencement, as *a* (the same not being far distant from the pit A), and run off from that assumed point *a* the first bearing and distance, in the same

manner as if a was the centre of the pit A; which first bearing and distance S 30° W 4 chains suppose to be represented by ab. Before the instrument is removed, from a take the bearing and distance of the centre of the pit A from a, which suppose S 30° E 3 chains aA, and insert it in the column of remarks in the survey-book (for fear it should be forgot), as a deflection from the line of the subterraneous survey; which deflection must be accounted for before the whole of the survey is plotted. Now remove the instrument to b, and there turn the sights in the direction of S 30° E, running off 3 chains, which let bB represent; then the line AB represents the first bearing and distance as if taken from the centre of the pit A (the line of deflection Aa is now repaid). Remove the instrument from b to B, and proceed to run off the second bearing and distance N 50° W 8 chains BC, according to the method described in the last example. Remove the instrument to C, and run off the third bearing and distance N 50° E 9 chains CD. Lastly remove the instrument to D, and run off the fourth bearing and distance N 53° W 8 chains DF. And if marks are put up at BCD and E, they will represent the course of the subterraneous excavation on the surface.

Note.—This survey ought also to be plotted by the new methods, given in Arts 20 and 21, in the manner directed in Art. 34a.

To show the manner how to avoid an obstacle that interferes with the line of survey when plotting it on the surface of the earth.

(38.) Suppose the following survey ABCD is to be plotted on the surface, commencing at the centre of the pit A;—

E

FIG 46.

	Chains.
S. 30° W.	4·00
N. 50° W.	8·00
N. 50° E.	9·00

Fix the instrument at the point a, as the assumed centre of the pit A, and run off the first bearing and distance from thence, which suppose to extend to b; then take the bearing and distance of A from a for the deflection, which note down in the column of remarks in the survey-book: suppose it to be S 30° E 3 chains : Then remove the instrument to b, and from thence run off S 30° E 3 chains bB, and the line AB will be the first bearing and distance as run off from A. Remove the instrument to B, and proceed to plot the remaining part of the survey. Now the next bearing, N 50° W, will be found to run over the lake e; therefore, to avoid this obstruction, let the plotter extend the line Bc to such a distance that, in running the second bearing from c, he may avoid the obstruction. Suppose this line Bc to be due west 6 chains, which being noted down in the survey-book, remove the instrument to c, and from thence let the bearing N 50° W 8 chains be run ; which suppose it to extend to d; then from d run off due east 6 chains (being the reverse of Bc), which suppose to extend to D ; then BC will be the second bearing and distance. Remove the instrument to C, and run off the third bearing and distance, which suppose to extend to D ; then CD will represent N 50° E 9 chains, and the whole is plotted.

The obstruction at e may be more easily avoided by

laying down the survey on paper, and drawing on it the lines AC AD, which must be measured, and their bearings from NS found; thus the position of the points C and D may be determined; also various other similar methods will readily suggest themselves to the student when the obstructions are even more formidable than that at e.

In plotting a survey, either on paper or on the surface of the earth, it matters not whether we begin with the first or last bearing, the ending will be the same.

(39.) Thus, suppose the subterraneous bearings and distances are required to be plotted, in order to determine on the surface the situation of the end D from the commencement A :—

FIG. 47.

	Chains.
1st, N. 10° W.	5·00
2nd, N. 40° E.	7·00
3rd, N. 45° W.	6·00
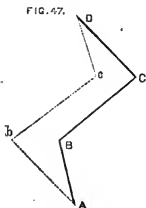
Suppose A the point or place of commencement, and run off from thence the first bearing and distance to B, then AB will represent N 10° W 5 chains; and from B run off the second bearing and distance to C, then BC will represent N 40° E 7 chains; and from C run off the third bearing and distance to D, then CD will represent N 45° W 6 chains,—and the whole is plotted in the order of the survey. Now, to plot the same in a manner contrary to the order of the survey, begin at the point A, and run off

N 2

the third bearing and distance N 45° W 6 chains,—which let A*b* represent; run off from *b* the second bearing and distance N 40° E 7 chains *bc*; also run off from *c* the first bearing and distance N 10° W 5 chains *c*D; which termination will correspond with the point D in the former method, if the work be right.

(40.) In the following subterraneous survey ABCDF, beginning at the pit A, I wish to have the same plotted on the surface, in order to determine the bearing and distance of F from A:—

FIG. 48
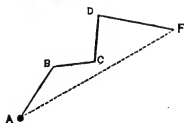
	Chains.
AB, N. 42° E. . .	5·00
BC, E. . .	4·00
CD, N. 9° E. . .	4·00
DF, S. 69° E. . .	5·56

Commence the plotting on the surface according as directed in the former examples; and running off the bearing and distance AB N 42° E 5 chains, remove the instrument to B, and run off the bearing and distance BC due east 4 chains; remove the instrument to C, and run off the bearing and distance CD N 9° E 4 chains; lastly, remove the instrument to D, and run off the bearing and distance DF S 69° E 5·56 chains, and there make a mark; then return with the instrument to the pit A, and take the bearing of the mark at F, which suppose N 64° 44′ E; then measure the distance, which suppose 14·40 chains, which are the bearing and distance required. Or the circumferentor may be fixed at F instead of A, and the bearing of A taken from it; which being reversed (see Art. 5), will become the bearing of F from A, the same as before.

Note.—In many cases, where the surveyor is desirous of plotting the subterraneous survey on the surface, it will be best to make choice of a

level piece of ground, sufficiently large to contain the whole, and plot the same thereon, assuming a point of commencement in the most advantageous place.

(41.) In the following survey of the subterraneous working ABCDF, driven from the pit A, I wish to know by what bearing the miner must be conducted from F, the extreme point of the excavation, just to hit the centre of the pit G; and also what is the distance of G from F?

	Chains.
AB, N. 30° W.	5·50
BC, N. 45° E.	7·00
CD, N. 50° W.	5·00
DF, N. 65° E.	7·00
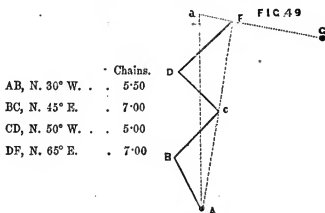
Commence the plotting at the pit A on the surface, as before directed, running off the distances in direction of their respective bearings: When the whole is run off to F, fix the instrument there, and take the bearing of the pit G from it, which suppose S 68° 30′ E; then measure, by the chain, the distance of G from F, which suppose 8·60 chains, the direction and distance required to hit the pit G.

In the foregoing subterraneous survey, commencing at the pit A, I wish to know the bearing and distance on the surface of F from A, without plotting the same?

(42.) Reduce the bearings and distances of the survey to their northing or southing, and easting or westing (see Art. 10, Ex. VII.), in order to obtain the denomination of bearing of F from the pit A. Thus:—

PREPARATORY TABLE.

		Northing.	Southing.	Easting.	Westing.
	Chains.	Chains.	Chains.	Chains.	Chains.
N. 30° W.	5·50	4·76	...	...	2·75
N. 45° E.	7·00	4·95	...	4·95	...
N. 50° W.	5·00	3·21	...	...	3·81
N. 65° R.	7·00	2·96	...	6·34	...
		15·88	Aa	11·29	6·56
				6·56	
				4·73	aF

The denomination of bearing of the extreme part of the excavation F from the pit A is 15·88 chains of northing, and 4·73 chains of easting. Therefore,

$$\text{As } Aa\ 15\cdot88 \quad \cdot \quad \cdot \quad \cdot \quad \cdot \quad 1\cdot2008505$$
$$\text{Is to radius} \quad \cdot \quad \cdot \quad \cdot \quad 10\cdot0000000$$
$$\text{So is } aF\ 4\cdot73 \quad \cdot \quad \cdot \quad \cdot \quad \cdot \quad \cdot6748611$$

$$\text{To tang. } \angle\ aAF\ 16°\ 35' \quad \cdot \quad 9\cdot4740106$$

$$\text{And } \sqrt{15\cdot88 + 4\cdot73} = 16\cdot56 = AF.$$

Now fix the instrument at the pit A, and run off from thence the bearing and distance N 16° 35′ E 16·56 chains, and the situation of F, with respect to the pit A, will be had on the surface.

(43.) In the workings of the pit A, see fig. 30 to Art. 17, I wish to know how far each bord or excavation opGqrst is distant from the boundary cdfgmn?

To obtain what is required, fix the circumferentor at the pit A, and survey in direction of AaG, VF, and bH, which are the excavations next the boundary,—measuring the distance that each bord opGqrst is driven towards the boundary from the headways VF and bH, entering them, according to the following form, in the survey-book.

SURVEY-BOOK.

Bearings.	Remarks to Left.	Distance.	Remarks to Right.	
		Chains.		
S. 80° W.	. . .	1·60	. . .	A a
S. 70° W.	. . .	1·80	. . .	a G
	. . .	0·80	A headways b, and a chalk mark + to return to.	
	A headways V, and a chalk mark + to return to.	1·20		
	Returned to .		mark + at V.	
S. 10° W.	. . .	2·40	. . .	V F
	. . .	0·80	Bord p, 1·30 chains towards the boundary.	
		1·60	Bord o, 1 chain towards ditto.	
	Returned to .	...	mark + at b.	
N. 1° W.	. . .	5·00	. . .	b H
	Bord q, 90 links towards the boundary	0·80		
	Bord r, 60 links towards the boundary	1·70		
	Bord s, 60 links towards the boundary	2·55		
	Bord t, 55 links towards the boundary	3·40		

Note.—The student must recollect to enter in this and all other survey-books in the first column the angles which every two successive lines in the survey make with one another when the new method, given in Arts. 20 and 21, are used; besides, not only this survey, but also the following one, ought to be done without the use of the magnet.

Now the survey underground being finished, fix the instrument at the pit A, on the surface, and run off the bearing and distance therefrom, in the order as taken underground,—the first S 80° W. 1·60 chains A a: Remove the instrument to a, and run off the next bearing and distance S 70° W 1·80 chains a G ; at 80 links make a mark on the surface, as represented by b ; also at 1·20 chains make another, as represented by V; and at G make another: Then with the chain measure the distance G f, which suppose 1·30 chains, which is the distance the excavation G is

short of the boundary,—which must be recorded in the miner's book of memorandums. Return with the instrument to the mark made on the surface at V, and run off S 10° W 2·40 chains VF; at 80 links, in direction from V to F, run off the bord p 1·30 chains to the right, perpendicular to the headways VF, and there make a mark at p : Then measure the distance pe, which suppose 1 chain, which is the distance of the bord p from the boundary,—which must be recorded. Also at 1·60 chains run off the bord o 1 chain to the right, similar to the former, and make a mark at o : Then measure the distance od, which suppose 70 links, which is the distance of the bord o from the boundary,—which must also be recorded. Return with the instrument to the mark made on the surface at b, and run off N 1° W 5 chains bH, and there make a mark : Then measure the distance Hn, which suppose 80 links, which is the distance of the headways bH from the boundary. At 80 links, in the direction from b to H, run off the bord q 90 links to the left, perpendicular to the headways bH, and there make a mark at q : Then measure the distance qg, which suppose 70 links, which is the distance of the bord q from the boundary. From 1·70 chains run off the bord r 60 links to the left, and make a mark at r : Then measure the distance rh, which suppose 1·10 chains, which will be the distance of the bord r from the boundary. From 2·55 chains run off the bord s 60 links to the left, and make a mark at s : Then measure the distance sk, which suppose 1·50 chains, which will be the distance of the bord s from the boundary. From 3·40 chains run off the bord t 55 links to the left, and make a mark at t : Then measure the distance tm, which suppose 1·80 chains, which will be the distance of the bord t from the boundary,—and the whole will be finished.

(44.) In the following subterraneous survey ABCDF, commencing at the pit A, I wish to know the bearing and distance of F from A :—

FIG. 50
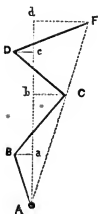
		Chains.
N. 30° W.	. .	5·50
N. 45° E.	. .	7·00
N. 50° W.	. .	5·00
N. 65° E.	. .	7·00

PREPARATORY TABLE.

1.	2.	3.	4.	5.	6.	7.
Bearings and Distances.	Northing.	Southing.	Easting.	Westing.	Northing and southing distance from A.	Easting and westing distance from the meridian of A.
	Chains.	Chains.	Chains.	Chains.	Chains.	Chains.
N. 30° W. 5·50	4·76	...	...	2·75	4·76 N.	2·75 W.
N. 45° E. 7·00	4·95	...	4·95	...	9·71 N.	2·20 E.
N. 50° W. 5·00	3·21	...	...	3·81	12·92 N.	1·61 W.
N. 65° E. 7·00	2·96	...	6·34	...	15·88 N.	4·73 E.

Fix the instrument at A, and run off the line Ad 15 chains 88 links on the magnetic meridian of A (from the 6th column of the table), for the northing of F from A; and also 4 chains 73 links dF (from the 7th column of the table), for the casting of F from the magnetic meridian of A: Then at F fix up a mark, and take its bearing and distance from A, which suppose N 16° 35′ E 16·56 chains,—which is the bearing and distance required.

This mode of plotting will be-tedious, and liable to error, particularly where the surface is uneven.

The manner of making a survey where the subterraneous excavation declines from the horizon.

(45.) In making surveys where the distances measured are not horizontal, but rising or falling, or both, it will be necessary for the surveyor to reduce all his measurements to horizontal distances, which may be obtained by taking the angle that each separate distance makes with the horizon, noting the same down opposite its respective bearing, in a column made for that purpose in the survey-book.

FIG 51
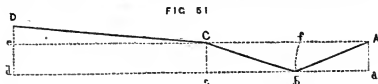
Suppose Ae and ad to be lines parallel to the horizon, and AbCD is the undulating excavation which is to be surveyed, commencing at A; let the bearing and distance taken in such a situation as that of Ab to be N 10° W 5 chains, and the angle fAb which such excavation makes with the horizon to be 30°; and another in such a situation as that of bC N 20° W 6 chains, and the angle Cbc which it makes with the horizon to be 20°; also another in the situation of CD N 20° E 12 chains, and the angle DCe which it makes with the horizon to be 10°;—which bearings,

distances, &c., must be inserted in the following survey book :—Thus, the first column containing the bearings and declining distances, the second column the magnitude of the angle that each bearing forms with the horizon, and the third the declining distance of each bearing reduced by the traverse tables to horizontal distance. This third column may be made at the surveyor's leisure, but previous to its being plotted.

SURVEY-BOOK.

1.	2.	3.
Rising and falling distances.	Angle that each bearing forms with the horizon.	The horizontal distance of each bearing.
Chains.		Chains.
N. 10° W. 5·00	30°	4·33 A f or a b
N. 20° W. 6·00	20°	5·64 b c x C f
N. 20° E. 12·00	10°	11·82 C or c d

I shall protract the survey first without reducing the declining measurements to horizontal distances, from the first column of the foregoing survey-book ; and, secondly, by the same, reduced to horizontal distances, taken from the third column, —in order to show the error arising from the protracting of declining or hypothenusal distances.

Without reducing the declining distances.—Let A b represent N 10° W 5 chains, b C N 20° W 6 chains, and CD N 20° E 12 chains ; then A b CD will represent the survey protracted according to the first column of the survey-book.

Where the declining lengths of each bearing are reduced to horizontal dis-

FIG 52
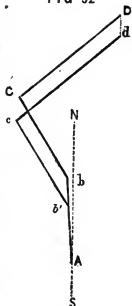
tance.—Let A*b′* represent N 10° W 4·33 chains (from the 3rd column of the survey-book), *b′c* N 20° W 5·64 chains, and *cd* N 20° E 11·82 chains; then A*b′cd* will represent the true protraction, and A*b*CD the false one,—and *d*D will be the amount of the error.

As it is common among practical miners, when plotting their surveys, to add a number of bearings and distances together, taking the mean sum of the degrees contained in the bearings so added for the common bearing of the whole, when they are all on the same side of the same meridian,— and the sum of the lengths of all the bearings for the length of the whole, — I shall therefore show the errors which result from such practices.

(46.) Suppose A B N 30° W 10 chains, and B C N 50° W 20 chains to be plotted.

FIG. 53.
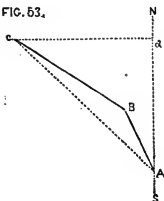
By the false method.

N. 30° W. . . 10 chains.

N. 50° W. . . 20 ,,

2) 80°

N. 40° W. . . 30 chains.

Now it appears that N 40° W 30 chains will be the bearing and distance equal to both, by this method.

By the true method.

	Chains.	Northing. Chains.	Westing. Chains.	
N. 30° W. .	. 10·00	8·66	5·00	
N. 50° W. .	. 20·00	12·86	15·32	
Aa		21·52	20·32	aC

$$
\begin{array}{llll}
\text{As } 21\cdot52 & . & . & 1\cdot3328420 \\
\text{Is to radius} & . & . & 10\cdot0000000 \\
\text{So is } 20\cdot32 & . & . & 1\cdot3079240 \\
\text{To tang. } \angle \ a\mathrm{AC} \ 43° \ 21' & & & 9\cdot9750820
\end{array}
$$

And $\sqrt{21\cdot52^{2} + 20\cdot32^{2}} = 29\cdot59$ chains = AC.

Then N 43° 21' W 29·59 chains is the true bearing and distance of C from A, instead of N 40° W 30 chains;—and the magnitude of the error will be their difference, *i. e.* 30—29·59 =41 links; it is hence presumed that no surveyor will use the false method.

A promiscuous collection of practical questions.

(47.) EXAMPLE I.—I wish to drive a drift or subterraneous excavation from the point A to hit the pit C, which is on the other side of a river; now I run a line AB by the river side, N 85° E 20 chains long, which from the point A, I found C to bear N 42° E, and also from the point B, I found C to bear N 30° W; I therefore desire to know what will be the length of the excavation or drift AC?

FIG. 54.
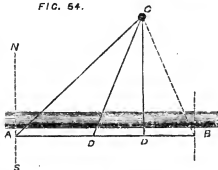
From the rules for reducing bearings into angles, $\angle$ A =43°, $\angle$ B=65°, and $\angle$ C=72°; therefore, by trigonometry, the excavation AC will be 19·05 chains in length.

EXAMPLE II.—There is a pit C (see last fig.), on the other side of a river, to which I wish to drive a drift from a given point; I took the bearing of the pit C from A, which was N 42° E, and after running a line AB by the river side in direction of N 85° E 20 chains, I also took its bearing again from B, which I found to be N 30° W; now I demand to know under what bearing I must set off a drift from a point D, 8 chains from A, along the line AB, so that I may hit C,—and also what will be the length of the drift DC?

$\angle$ A=43°, $\angle$ B=65°. The line DC, which is the direction of the drift or excavation, will be found to form an angle with the line DB of 65° 33′, and the line DB forms an angle of 85° to the left of the north magnetic meridian; therefore, from the rule for reducing angles into bearings (Art. 3), the drift DC will bear N 19° 27′ E, and its length will be 14·29 chains.

EXAMPLE III.—There is an inaccessible point C (see fig. to Ex. I.), to which a drift is to be driven underground; now the angle A is found to be 43°, the angle B=65°, and the length of the drift AB=20 chains: how far from A must a drift be set off to arrive at C by the shortest distance possible?

The shortest distance between AB and the point C is a line perpendicular to AB, let fall from the point C.

The point, from which the drift DC must be driven, by the shortest distance possible, will be 13·94 chains from A, as required.

EXAMPLE IV.—I made a survey along the side of a hill from A to B, under the following bearings and distances viz., Aa N 75° E 20 chains, ab S 80° E 19 chains, bc N 73° E 15·60 chains, and cB S 71° E 18·65 chains; now I wish to make a straight tunnel from A to B; therefore I demand to

know under what bearing it must be conducted, and what will be its length?

FIG. 53.
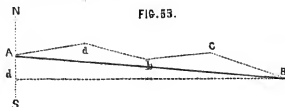
From the traverse tables, the point B will have 7·63 chains of southing Ad, and 65·17 chains of easting dB from A; and the angle SAB = 83° 43′, which is the angle that the line AB makes with the south meridian,—and AB being the direction of the tunnel, therefore it must be conducted from A to B under the bearing of S 83° 43′ E, and its length will be 65·61 chains.

EXAMPLE V.—There is a vein of lead ore AB, which I find forms an angle CAB of 82° with the horizon; now I wish to know how deep my shaft DB must be sunk before I cut the vein, if I set it off at the distance of 30 yards from A to D at the surface?

FIG. 56.

Ans. DB = 213·4 yds.

EXAMPLE VI.—There is a vein of lead ore AB (see last fig.), which forms an angle CAB of 70° with the horizon, on which I wish to sink a shaft DB; I demand to know what distance AD the shaft must be set off from the vein at the surface, just to cut it at the depth of 141 yards?

The distance AD that the shaft must be set off at the surface from the vein AB, just to cut it at the depth of 141 yards, will be 51·3 yards.
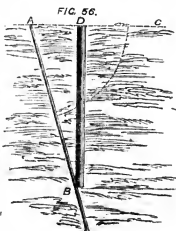
EXAMPLE VII.—I have to set a drift BC from the bottom of a pit AB, which is to be driven truly level; now I wish

FIG. 58.
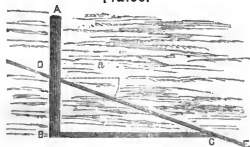
to know at what distance from the pit B it will cut the stratum of coal DE, which dips so as to form an angle aDE of $20°$ with the horizon, the drift BC being set from the bottom of the pit at B, 40 yards perpendicularly below the seam D, and driven in direction of the dip of the stratum?

Ans. BC = 109·9 *yds.*

EXAMPLE VIII.—I set off a drift at the side of a hill A,

FIG. 59.
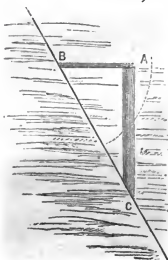
which was driven truly level, and cut a vein of lead ore at B, 100 yards distant from A, which vein I found to make an angle of 65° ABC with the horizon; now I wish to know what depth a shaft at A must be sunk just to cut the vein at C?

Ans. AC = 214·4 *yds.*

EXAMPLE IX.—In the subterranean survey ABCD, in the form of a trapezium, are two shafts F and E, joined by a fifth straight drift FE. Now this survey was made with a magnetic needle, which was afterwards found to be defective in its indications, on account of the presence of ferruginous substances both in the mine and on the surface; therefore, how is the work to be plotted, since the angles

cannot be relied upon; and only the lengths of five drifts, and the segments of the drifts AB and CD made by the drift EF, are given; moreover, the tops of the shafts F and E range with the sun at 1½ P.M. on the 18th of October, 1860?

FIG. 57.
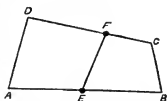
Note.—The solution of this question will require a knowledge of the application of algebra to geometry and of spherical trigonometry to astronomy.

EXAMPLE X.—There is a vein of lead ore AC, which forms an angle *aAe* of 80° with the horizon A*c* ; now I have sunk a shaft AB on the vein at the surface, to the depth of 120 yards perpendicular; I desire to know what distance the bottom of the shaft B will be from the vein?

FIG. 60.

Ans. BC=21·1 *yds.*

EXAMPLE XI.—I made a survey of a subterranous excavation ABCDFG (see the following bearings and distances), commencing at the pit A; now I wish to know, on the surface, by one single bearing and distance, to be taken from the pit A, where I must sink a pit perpendicularly upon G, the extreme end of the excavation?

FIG. 61
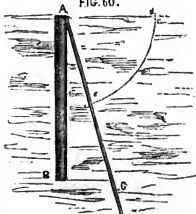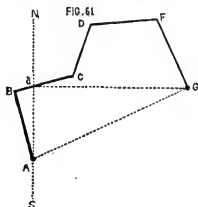
			Chains.
AB, N. 20° W.	.	.	15·50
BC, N. 60° E.	.	.	12·00
CD, N. 15° E.	.	.	10·50
DF, N. 85° E.	.	.	15·00
FG, S. 25° E.	.	.	16·60

The extreme point G of the excavation will have 16·98 chains of northing Aa, and 29·76 chains of easting aG, from A; therefore the line AG will be found to bear N 60° 17′ E with SN, the magnetic meridian of A, and its length will be 34·26 chains,—the bearing and distance required.

Note.—This Example ought also to be solved by taking the angles from the direction of the drift AB (the position of which is assumed to be fixed on the surface), by the method given in Art. 21.

EXAMPLE XII.—I have to drive an excavation from B towards A, which is to rise 1 inch in every 60 feet of its

FIG. 62.
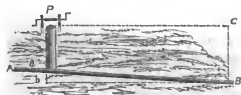
length; now I wish to put down an air-shaft P thereon, just 1600 yards from its mouth B; what will be the depth of the shaft from the surface to the sole of the drift or excavation, when the surface at P, the place where it has to be sunk, is 350 feet above the level of B, the mouth of the excavation?

Ans. 343½ *feet.*

EXAMPLE XIII.—A headway is driven into a coal-stratum

from the foot of a hill; the straight portions of the headway, commencing at A, are AB = 5·63 chains, BC = 5·18, CD = 3·80, DE = 4·71, and EF = 7·02; the angles are ABC = 121° 16', BCD = 228° 5', CDE = 164° 52', and DEF = 168° 29', all the angles being taken by the theodolite on the right side of the lines in the headway. A shaft is required to be sunk on the hill to the coal-stratum, at the levelled or horizontal distance of 37·50 chains from the entrance of the headway, from which the top of the proposed shaft bears 37°42' to the right of the direction of the first straight portion of the headway AB. Now the coal-stratum rises uniformly at the rate of 1¾ inches in a chain; it is required to find the direction and length of the additional headway from F to the bottom of the proposed shaft, also its depth, the angle of elevation of the top of the shaft from the entrance A of the headway being 12° 8'.

PART III.

This part of the work treats of those subjects which are particularly necessary to be attended to, because of the great number of existing surveys, which have been made by the help of the magnetic needle; and the consequent necessity of attending to the magnetic variation at the different periods of time, at which those surveys were made; of showing the method of finding the true meridian, and of determining the variation of different magnetic needles at different times, and of the manner of reducing bearings taken with the magnetic meridian to those formed with the true meridian. Various other subjects interesting to miners are here discussed, concluding with a Traverse Table, and the method of estimating the produce of seams of coal.

AXIOMS AND OBSERVATIONS.

(48.) 1.—Two magnetic needles seldom have exactly the same variation.

2.—The magnetic variation not being stationary, the variation of the needle of all instruments depending thereon will change accordingly.

3.—If a subterraneous survey is made by one instrument, and plotted on the surface by another, the needles of each having different magnetic variation, the plotting will be erroneous if the bearings to be plotted are not previously reduced to bearings with that magnetic needle by which it is to be plotted.

4.—If a subterraneous survey is made by one instru-

ment, and plotted on the surface by another, the needles of both having the same magnetic variation, the survey will be truly plotted.

5.—If a survey is plotted on the surface immediately after it has been taken under ground (by the same instrument), no material error can result.

6.—If a survey is plotted on the surface by the same instrument it was made with, but at some distant time after, the plotting will be erroneous, inasmuch as the magnetic variation has changed in the time between the survey being taken underground and its being plotted on the surface.

7.— All bearings of subterraneous excavations which are added, from time to time, on any plan kept for that purpose, must be reduced to bearings with the delineated meridian of that plan, previous to their being plotted thereon, otherwise the plotting will be erroneous.

8.— All surveys of subterraneous excavations which are recorded for future purposes must be recorded with the variation of the needle by which they have been taken, or otherwise they must be reduced to bearings with the true meridian, and so recorded, notifying the same.

9.—All the preceding axioms and observations will be unnecessary in new surveys, which are made without the use of the needle, and which are unconnected with old surveys.

Of the magnetic variation of the needle.

(49.) Since nearly all subterraneous surveys have been made by, or have reference to, the magnetic needle, each bearing (as shown in the first part of this work) is taken by the angle it makes with the magnetic meridian; and that magnetic meridian has been continually changing at the rate of about 9 minutes annually, for 230 years, from north towards the west, up to 1793; but its annual declination was afterwards not so great, for the north end of the needle was little more than 24 degrees westward of the true meridian

of London in 1803: At Paris it was somewhat less, still
continuing to increase or decrease at a slow rate; while in
some parts of the world the north end of the needle was
even eastward of the true meridian at the last-named date.
As the magnetic meridian is always changing, it must neces-
sarily follow, that the same line which formed an angle with
it, of a certain magnitude, on any particular day, will not
(we have strong reasons to suppose) form the same angle
that day twelve months with the then magnetic meridian:
Hence follows the great necessity of reducing every bear-
ing to the angle it will form with the true or invariable
meridian; the manner of doing it will be shown hereafter:
Also the records of subterraneous surveys noted down for
future purposes, where the surveyor has neglected to insert
from what kind of meridian the bearings thereof are formed;
by such neglect those records will not only cease to be of
use, but will tend to mislead.

I shall insert a table, showing the different degrees of
magnetic variation at different times from the year 1575 to
1858, which is nearly to the present time:

VARIATION AT LONDON.

Year.	Variation.		Year.	Variation.	
1576	11° 15′		1745	16° 53′	
1580	11° 11		1750	17° 54′	
1612	6° 10′	E.	1760	19° 12′	
1622	6° 0′		1765	20° 0′	
1633	4° 5′		1770	20° 35′	
1657	0° 0′		1775	21° 28′	
1666	1° 35′		1777	21° 57′	
1672	2° 30′		1779	22° 4′	
1683	4° 30′		1780	22° 26′	W.
1692	6° 0′		1786	23° 19′	
1700	8° 0′	W.	1789	23° 36′	
1717	10° 42′		1793	23° 51′	
1724	11° 45′		1797	24° 2′	
1730	13° 0′		1800	24° 6′	
1735	14° 16′		1803	24° 9′	
1740	15° 40′		1806	24° 15′	

VARIATION AT LONDON.—*Continued.*

Year.	Variation.		Year.	Variation.	
1809	24° 22′		1835	23° 32′	
1812	24° 28′		1838	23° 19′	
1815	24° 35′		1841	23° 6′	
1818	24° 41′		1844	22° 52′	
1820	24° 32′	W.	1847	22° 41′	W.
1823	24° 20′		1850	22° 30′	
1826	24° 8′		1853	22° 19′	
1829	23° 56′		1856	22° 8′	
1832	23° 44′		1858	22° 2′	

Note.—By the variation being east or west, is meant that the north end of the magnetic needle is on the east or west side of the true meridian; and where the variation is called east or west in the following part of this work, it is to be understood that the north end of the magnetic needle has east or west variation accordingly, except it is particularly mentioned to the contrary.

From the table it appears the magnetic needle had east variation in the year 1576; that is, its north end was 11° 15′ on the east side of the true meridian of London; and in 1657 the needle was in direction of the true meridian; and since that time it has been veering about to the west, until it has got upwards of 24° to the westward thereof. Besides this annual variation just mentioned, it has a daily variation.

I shall insert a table, showing the diurnal variation taken at different hours of the 27th day of June, 1759, by Mr. Canton.—(*Phil. Trans.*, vol. 51.)

	Hrs.	Min.	Declination west.	Degrees of Fahrenheit's thermom.
Morning	0	18	18° 2′	62°
	6	4	18° 58′	62°
	8	30	18° 55′	65°
	9	2	18° 54′	67°
	10	20	18° 57′	69°
	11	40	19° 4′	68¼°
Afternoon	0	50	19° 9′	70°
	1	38	19° 8′	70°
	3	10	19° 9′	68°
	7	20	18° 59′	61°
	9	12	19° 6′	59°
	11	40	18° 51′	57¼°

The mean variation of each month of the year.—

January	.	.	7' 8"	July .	. .	13' 14"
February	.	.	8' 58"	August .	. .	12' 19"
March	.	.	11' 17"	September .	. .	11' 43"
April	.	.	12' 26"	October .	. .	10' 36"
May	.	.	13' 0"	November .	. .	8' 9"
June	.	.	13' 21"	December .	. .	6' 58"

To find the true meridian.

(50.) I shall lay down an easy and comprehensive rule to find the true meridian, which is preparatory to the determining of the magnetic variation of the needle. It is well known that the sun, at 12 o'clock at noon, is due south in all northern latitudes ; and if a pole is set up perpendicular to the horizon, its shadow at that hour will bear exactly north, or in direction of the true meridian ;—also the shadow of the pole will be shortest at that precise time.

Let ABC be a board perfectly plain and clear of twistings, and of a triangular form, each side about 30 inches long, having a number of concentric circles *cde* about 1½ inch asunder, drawn on its surface from a centre *a*.   Now let this board be placed horizontal by means of a spirit level, with its angular point C towards the south ; and at *a*, the centre of the concentric circles, let there be fixed an upright pin about 10 inches long, exactly perpendicular to the board, and also perpendicular to the horizon. All this being done on a clear day, and before the sun arrives on the meridian of the place of observation, which I shall say about 11 o'clock, then observe carefully the first concentric circle that the end of the shadow of the pin fixed at *a* touches, which suppose to be at *f*, and there make a mark : Then observe again carefully when the end of the same shadow touches on the same concentric circle, which will be about 1 o'clock,—suppose it to be at *g* ; there make another mark : Then with a pair of compasses divide the distance *fg*, and

the point in the middle between which, suppose h, will be the direction of the shadow of the pin at 12 o'clock: Consequently ah is the direction of the true meridian. Then by placing an upright sight E, with a slit kk in it, on the table, the centre of which coinciding with the point h, the pin at a having an opening in it similar to bb, with a perpendicular hair in direction of the opening; and by looking through the sight E, together with the hair in the centre of the opening in the pin placed at a, the meridian may be extended to any distance S on the surface; in the direction of which line it will be proper to place two permanent marks, as represented by NS, whose distance may be from 100 to 300 yards, for the purpose of determining at all times the magnetic variation of the needle of the different instruments, made use of in surveying: Such a line every director of mines ought to have marked out in the situation of the mine he directs.
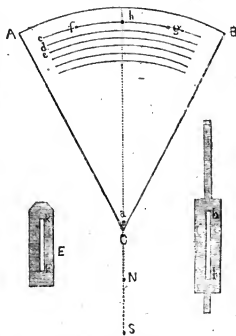
(50*a*.) If the student be acquainted with the application of spherical trigonometry to astronomy, he will find the following method of finding the true meridian to be greatly preferable to that just given. Let S represent the place of the sun's centre, P the north pole, and Z the zenith; these

F

three points being the angles of a spherical triangle SPZ (the student can readily draw the figure for himself), in which SZ represents the co-altitude of the sun, when he comes into the direction of the required bearing of the drift in the mine; SP the sun's co-declination on the day of observation (which will be found in the Nautical Almanack for the year in which the observation is made); and PZ the co-latitude of the place of the mine (which is usually well known). From the given spherical triangle SPZ the angle Z may be readily found, which is the azimuth or bearing of the sun from the north at the time of observation, and also the bearing of the drift; whence also the true meridian may be readily deduced for the following purpose.

To determine the magnetic variation of the needle of any instrument.

(51.) Suppose N and S to be marks representing the true meridian, S the south and N the north; place the instrument (whose magnetic variation you would wish to know) at S, and turn the sights in direction of SN until N is seen through them; at the same time observe the bearing of the needle of the instrument, and whatever N is found to bear from due north, as much will the magnetic meridian differ from the true meridian. Suppose the north end of the needle to stand in direction of Sd, then the true meridian SN will be to the east of the magnetic as much as the angle dSN, which suppose 23°; then SN will bear N 23° E with the magnetic meridian: Consequently the needle of the instrument may be said to have 23° of west variation, as the north end thereof is 23° to the west or left of the true meridian SN. Or if the north end of the needle stand in direction of Se, then the true meri-

FIG. 54.

dian SN will be to the west of the magnetic as much as the angle *e*SN, which, if equal to 23°, then SN will bear N 23° W : Then the needle may be said to have 23° of east variation, the north end thereof being 23° to the east or right of the true meridian SN.

The manner of reducing bearings from a magnetic to a true meridian.

(52.) Let NS represent the true meridian, N the north and S the south, and *ns* a magnetic needle suspended on a centre *c*, representing the magnetic meridian, *n* the north and *s* the south ; then the arch *na* will be the variation of the magnetic meridian from the true meridian, which may

be called west va-
riation, the north
end of the needle
being to the west
side of the true
meridian : And if
the angle *nca* is
equal to 23°, then
the needle will
have 23° of west
variation, and the
south end *s* will
have 23° of east
variation ; for *s*

FIG. 65.

will be to the east
of the true south
meridian line as
much as the north
end *n* is to the west of the true north meridian line.—
(See theorem 3.)
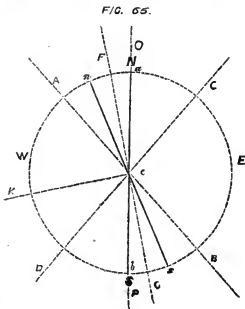
1st.—Suppose the circle WE to represent a circum-
ferentor, and that the bearing of the object O with the true
meridian is required ; if *ns* is the needle representing the

y 2

magnetic meridian, and the object O is found to form an angle *nca* with it of 23°, which (from the manner of determining bearings, Art. 2) may be called N 23° E, and, as before, the magnetic variation of the needle being 23° to the west of the true meridian, then 23° — 23° = 0; therefore the bearing of O with the true meridian S*c*N will be due north, for the needle ought to have stood in direction *ab*.

2d.—Suppose again the bearing of the object A with the true meridian is required; the bearing of A with the magnetic meridian will be equal to the angle *nc*A, which call N 10° W; but as the magnetic meridian has 23° of west variation, the bearing of A with the true meridian will be N 23° + 10° = 33° W; for angle *ac*A is equal to 33°, which is the angle that *c*A makes with the true meridian S*c*N.

3d.—Suppose again the bearing of the object C with the true meridian is required; the bearing of C with the magnetic meridian will be equal to the angle *nc*C, which call N 53° E; but the variation of the needle being 23° to the west of true north, and ought to have stood in the direction of *ab*, consequently the bearing of C from *c* with the true meridian will be N 53° — 23° = 30° E; for angle *ac*C is equal to 30°, which is the angle that the line *c*C makes with the true meridian line S*c*N.

4th.—Suppose the bearing of the object D with the true meridian is required; the bearing of D with the south magnetic meridian will be equal to the angle *sc*D, which call S 56° W; but the south end of the needle having 23° of east variation, and ought to have stood in direction of *ab* the true meridian, consequently the bearing of D from *c* with the true meridian will be S 56° — 23° = 33° W; for angle *bc*D is equal to 33°, which is the angle that the line *c*D makes with the true meridian line N*c*S.

5th.—Suppose again the bearing of the object B with the true meridian is required; the bearing of B with the magnetic meridian will be equal to the angle *sc*B, which call S 15° E; but the south end of the needle having 23° of east

variation, consequently the true bearing of B will be S 15° + 23° = 38° E ; for augle bcB is equal to 38°, which is the angle that the line cB makes with the true meridian line NcS.

6th.—Suppose again the bearing of the object F with the true meridian is required ; the bearing of F with the magnetic meridian will be equal to the angle ncF, which call N 13° E ; but the magnetic meridian has 28° of west variation, consequently the bearing of F with the true meridian will be N 23° − 13° = 10° W ; for angle acF is equal to 10°, which is the angle that the line cF makes to the left with the true meridian ScN.

7th.—Suppose again the bearing of the object G with the true meridian is required ; the bearing of G with the magnetic meridian will be equal to the angle scG, which call S 13° W ; but the south magnetic meridian has 23° of east variation, consequently the bearing of G with the true meridian will be S 23° − 13° = 10° E ; for angle bcG is equal to 10°, which is the angle that the line cG makes to the right with the true meridian NcS.

8th.—Suppose again the bearing of the object K with the true meridian is required ; the bearing of K with the magnetic meridian will be equal to the angle ncK, which call N 80° W ; the magnetic meridian having 23° of west variation, the angle that cK will make with the true north meridian cN will be 80° + 23° = 103°, acK ; but as it exceeds 90°, therefore 180° − 103° = 77°, angle bcK ; then the bearing of K with the true meridian will be S 77° W ; for angle bcK is equal to 77°, which is the anglo that the line cK makes with the true south meridian line NcS.

N.B.—The true bearing of any object is nothing more than the angle that the object makes with the true meridian, instead of the angle it forms with the magnetic meridian ; therefore, by the several cases of Art. 52, the method of solving the following examples will be readily seen :

EXAMPLE I.—If the following bearings, N 20° W, N 60°

E, N 70° W, and N 13 E are taken by an instrument whose magnetic needle has 23° west variation, what will be their bearings with the true meridian?

The first bearing N 20° W will form a bearing of N 20° + 23° = 43° W with the true meridian.

The second bearing, N 60° E, will form a bearing of N 60 − 23° = 37° E with the true meridian.

The third bearing, N 70° W, will form a bearing of 180° − 70° + 23° = 87°, which will be S 87° W with the true meridian.

The fourth bearing, N 13° E, will form a bearing of N 23° − 13° = 10° W with the true meridian.

With the magnetic meridian.	With the true meridian.
Thus, N. 20° W.	N. 43° W.
N. 60° E.	N. 37° E.
N. 70° W.	S. 87° W.
N. 13° E.	N. 10° W.

EXAMPLE II.—If the following bearings are taken by a meridian having 23° of west variation—S 10° W, N 10° E, N 50° E, and N 20° W—what will be their bearings with the true meridian?

With the magnetic meridian.	With the true meridian.
S. 10° W.	S. 13° E.
N. 10° E.	N. 13° W.
N. 50° E.	N. 27° E.
N. 20° W.	N. 43° W.

EXAMPLE III.—If the following bearings are taken by a meridian having 10° of west variation—N 50° W, N 70° E, S 5° E, and S 60° W—what will be their bearings with the true meridian?

With the magnetic meridian.	With the true meridian.
N. 50° W.	N. 60° W.
N. 70° E.	N. 60° E.
S. 5° E.	S. 15° E.
S. 60° W.	S. 50° W.

EXAMPLE IV.—If the bearings in the last example be taken by a meridian having 6° of east variation, what will be their bearings with the true meridian?

With the magnetic meridian.	With the true meridian.
N. 50° W.	N. 44° W.
N. 70° E.	N. 76° E.
S. 5° E.	S. 1° W.
S. 60° W.	S. 66° W.

The manner of reducing a bearing from one magnetic meridian to its bearing with any other magnetic meridian of different variation.

(53.) 1st.—Suppose the bearing of the object P from C is taken by a circumferentor whose needle has 10° of west variation $n's'$, which bearing is to be reduced to the bearing it will form with another magnetic meridian ns, having 23° of west variation: Let NS represent the true

FIG. 66.
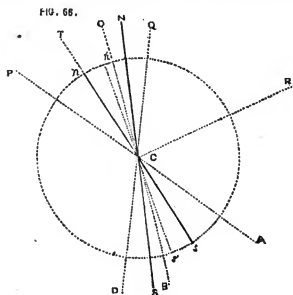
meridian, and the bearing of CP therewith (from the man-

ner of reducing bearings, &c., Art. 52) equal to the angle
PCN 45°, or N 45° W; also the magnetic meridian to which
the bearing PC is to be reduced equal to the angle nCN
23°, or having 23° of west variation; the object P and the
magnetic variation of the meridian to which its bearing is
to be reduced are both on the *west side* of the true meridian
NS; therefore ∠ PCN 45° − ∠ nCN 23° = ∠ PCn 22°;
and as the angle PCN exceeds the angle nCN, the object P
from C must bear N 22° W with the magnetic meridian ns.

2d.—Suppose the bearing of the object O from C is
taken by an instrument whose needle has 10° of west
variation $n's'$, which is to be reduced to the bearing it
will form with another magnetic meridian ns, having 23° of
west variation: Let the bearing of CO with the true meridian
be found equal to the angle OCN 8°, or N 8° W; and the
magnetic meridian to which the bearing CO is to be re-
duced equal to the angle nCN 23°, or having 23° of west
variation; the object O and the magnetic variation of the
meridian to which its bearing is to be reduced are both on
the *west side* of the true meridian NS; therefore ∠ nCN
23° − ∠ OCN 8° = ∠ OCn 15°; and as the angle OCN is
less than the anlge nCN, the bearing of O from C will be N
15° E with the magnetic meridian ns.

3d.—Suppose the bearing of the object T from C is
taken by a magnetic needle having 10° of west variation
$n's'$, which bearing is to be reduced to the bearing it will
form with another magnetic meridian ns, having 23° of west
variation: Let the bearing of TC with the true meridian
be found equal to the angle TCN 23°, or N 23° W; and the
magnetic meridian to which the bearing TC is to be reduced
equal to the angle nCN 23°, or having 23° of west variation;
then ∠ TCN 23° − ∠ nCN 23° = 0°; therefore the bearing
of T from C will be in the direction of the magnetic meridian
ns, or due north.

4th.—Suppose the bearing of the object Q from C is
taken by a magnetic needle having 10° of west variation $n's'$,

which bearing is to be reduced to the bearing it will form with another magnetic meridian, ns, having 23° of west variation: Let the bearing QC with the true meridian NS be found equal to the angle QCN 15°, or N 15° E; and the magnetic meridian to which the bearing QC is to be reduced equal to the angle nCN 23°, or having 23° of west variation; now the object Q and the magnetic variation of the meridian to which its bearing is to be reduced are on *contrary sides* of the true meridian NS; therefore ∠ QCN 15° + ∠ nCN 23° = ∠ QCn 38°; and also the bearing of Q will be on the *contrary side* of that magnetic meridian ns that its variation is on; and as ns has west variation, therefore the bearing of Q from C will be N 38° E with the meridian ns.

5th.—Suppose the bearing of the object A from C is taken by the meridian $n's'$, having 10° of west variation, which is to be reduced to the bearing it will form with another magnetic meridian ns, having 23° of west variation: Let the bearing of CA with the true meridian NS be found equal to the angle ACS 45°, or S 45° E; and the south magnetic meridian to which the bearing AC is to be reduced equal to the angle sCS 23°, or having 23° of east variation (see theorem 3, Art. 48); the bearing of the object A and the magnetic variation of the meridian to which its bearing is to be reduced are both on the *east side* of the true meridian; therefore ∠ ACS 45°− ∠ sCS 23° = ∠ ACs 22°; the angle ACS exceeding the angle sCS, the bearing of A with the magnetic meridian ns will be S 22° E.

6th.—Suppose the bearing of the object B from C is taken by a needle $n's'$, having 10° of west variation, which is to be reduced to its bearing with another magnetic meridian ns, having 23° of west variation: Let the bearing of CB with the true meridian NS be found equal to the angle BCS 8°, or S 8° E; and the south magnetic meridian to which the bearing BC is to be reduced equal to the angle sCS 23°, or having 23° of east variation (see theorem 3,

Art. 48); the bearing of the object B and the magnetic variation of the meridian to which its bearing is to be reduced are both on the *east side* of the true meridian; therefore ∠ *s*CS 23°— ∠ BCS 8°= ∠ BC*s* 15°; and as the angle BCS is less than the angle *s*CS, the bearing of B from C will be S 15° W with the magnetic meridian *ns*.

7th.—Suppose the bearing of the object D from C is taken by a needle *n's'*, having 10° of west variation, which is to be reduced to its bearing with another magnetic meridian *ns*, having 23° of west variation: Let the bearing of CD with the true meridian NS be found equal to the angle DCS 15°, or S 15° W; and also the south magnetic meridian to which the bearing DC is to be reduced equal to the angle *s*CS 23°, or having 23° of east variation (see theorem 3, Art. 48); and as the bearing of the object D and the magnetic variation of the meridian to which its bearing is to be reduced are on *contrary sides* of the true meridian NS, therefore ∠ DCS 15°+*s*CS 23°= ∠ DC*s* 88°; and also the bearing of D will be on the *contrary side* of the magnetic meridian *ns* that its variation is on; and as the south meridian *ns* has east variation, therefore the bearing of D from C will be S 38° W.

8th.—Suppose the bearing of the object R from C is taken by the meridian *n's'*, having 10° of west variation, which is to be reduced to the bearing it will form with another magnetic meridian *ns*, having 23° of west variation: Let the bearing RC with the true meridian be found equal to the angle RCN 77°, or N 77° E; and the magnetic meridian to which the bearing RC is to be reduced equal to the angle *n*CN 23°, or having 23° of west variation; the bearing of the object R and the magnetic variation of the meridian to which it is to be reduced are on *contrary sides* of the true meridian NS; therefore ∠ RCN 77° + ∠ *n*CN 23°= ∠ RC*n* 100°; but as the angle that the object R makes with the north magnetic meridian *ns* exceeds 90°, its bearing in that case must be with the *south or contrary*

meridian; then $180° - 100° = 80°$ / RCs; consequently the bearing of the object R with the magnetic meridian ns will be S 80° E.

Note.—From the several cases of Art. 53, the student will have no difficulty in solving the following examples, with respect to two different magnetic variations.

EXAMPLE I.—If the following bearings are taken by a meridian having 10° of west variation,—N 50° W, N 70° E, S 5° E, and S 80° E; what will be the bearing of each with a meridian having 23° of west variation?

With a meridian of 10° of variation.	With a meridian of 23° of variation.
N. 50° W.	N. 37° W.
N. 70° E.	N. 83° E.
S. 5° E.	S. 8° W.
S. 80° E.	S. 67° E.

EXAMPLE II.—If the following bearings are taken by a meridian having 10° of east variation,—S 60° W, S 10 E, N 80° E, and N 10° W; what will be the bearing of each with a meridian having 20° of west variation?

With a meridian of 10° of east variation.	With a meridian of 20° of west variation.
S. 60° W.	Due west.
S. 10° E.	S. 20° W.
N. 80° E.	S. 70° E.
N. 10° W.	N. 20° E.

EXAMPLE III.—The following bearings are taken by a meridian having 20° of west variation,—S 60° W, N 5° W, N 30° W, and N 50° E; what bearing will each form with a meridian having 10° of east variation?

With a meridian of 20° of west variation.	With a meridian of 10° of east variation.
S. 60° W.	S. 30° W.
N. 5° W.	N. 35° W.
N. 30° W.	N. 60° W.
N. 50° E.	N. 20° E.

EXAMPLE IV.—If the following bearings are taken by
the true meridian,—S 60° W, N 5° W, N 30° W, and
N 50 E; what bearing will each form with a meridian
having 23° of west variation?

With the true meridian.	*With a meridian of 23° of west variation.*
S. 60° W.	S. 83° W.
N. 5° W.	N. 18° E.
N. 30° W.	N. 7° W.
N. 50° E.	N. 73° E.

EXAMPLE V.—I have to plot a survey on the surface of
the following bearings and distances,—N 25° W 5 chains,
N 63° W 10 chains, N 20° E 3 chains, N 70° E 6 chains,
and S 84° E 9 chains, which has been taken by a circum-
ferentor having 20° of west variation; now I find the
circumferentor by which I have to plot the same has 23°
of west variation, I demand to know the bearings under
which the survey must be plotted, so that the same may
be accurately done?

With a meridian of 20° of west variation.		*The bearings under which the survey must be plotted to be accurately done, by a needle having 23° of west variation.*	
	Chains.		Chains.
N. 25° W.	. . 5	N. 22° W.	. . 5
N. 63° W.	. . 10	N. 60° W.	. . 10
N. 20° E.	. . 3	N. 23° E.	. . 3
N. 70° E.	. . 6	N. 73° E.	. . 6
S. 84° E.	. . 9	S. 81° E.	. . 9

EXAMPLE VI.—In a subterraneous survey of the fol-
lowing bearings and distances, viz. N 20° W 10 chains,
N 60° W 3 chains, S 12° W 5 chains, N 87° W 4 chains,
and S 15° E 7 chains, surveyed by an instrument having
22° of west variation, which is to be plotted on a plan
whose meridian has 12° of west variation, I wish to know

under what bearing each must be plotted on the plan, so that it may be accurately done?

The bearings by a meridian having 22° of west variation.		The bearings with the plan's meridian having 12° of west variation.	
	Chains.		Chains.
N. 20° W.	. . 10	N. 30° W.	. . 10
N. 66° W.	. . 3	N. 70° W.	. . 3
S. 12° W.	. . 5	S. 2° W.	. . 5
N. 87° W.	. . 4	S. 83° W.	. . 4
S. 15° E.	. . 7	N. 25° E.	. . 7

To find what kind of a meridian a plan has been constructed by.

(54.) Where subterraneous excavations are to be added to some previously delineated on a plan, it will be necessary, first of all, to find what kind of meridian the plan has been constructed by, in order that the bearings to be plotted may previously be reduced thereto (see theorem 4, Art. 48).

1. Suppose $N'S'$ to be the meridian of a plan whose magnetic variation is required to be known ; let the bearing of the pit B from the pit A be taken on the plan with the meridian thereon, equal to the angle BAN' 40°, or N 40° W; and let the bearing of the same two pits be taken on the surface by a circumferentor placed at A, whose needle is known to have 23° of west variation ns, and found to form an angle BAn = 27°, or N 27° W; then, if $N'S'$ represent the true meridian, the line AB will form an angle therewith of 27° + 23° = 50° BAN, or N 50° W: From ∠ BAN 50

FIG 67
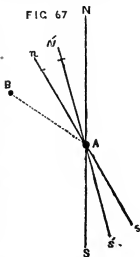
BAN' 40°, leaves ∠ N'AN = 10°, which is the angle
that the plan's meridian makes with the true meridian;
and as the angle BAN', which is the bearing of the
object with the plan's meridian, *is to the left* thereof, and
less than the ∠ BAN, which is the bearing of the same
object, as taken by the circumferentor on the surface, with
the true meridian, and *to the left* thereof also, it follows
that ∠ N'AN, the variation of the plan's meridian, must
be *to the left* of the true meridian; therefore S'N' must have
10° of west variation.

2. Suppose N'S' to be the meridian of a plan whose
magnetic variation is required to be known; let the bearing
of the pit B from A be taken on the plan with the meridian
thereon, equal to the angle BAN' 60°, or N 60° W; and
let the bearing of the same two pits be taken on the surface
by a circumferentor placed at A, whose needle is known
to have 23° of west variation *us*, and found to form an

FIG. 68

angle BA*n* = 27°, or N 27° W; then if
NS represent the true meridian, the
line AB will form an angle therewith
of 27° + 23° = 50° BAN, or N 50°
W: Then from ∠ BAN' 60° − ∠
BAN 50°, leaves ∠ N'AN = 10°, the
variation of the plan's meridian; but
as the ∠ BAN', which the bearing of
the object makes *to the left* with the
plan's meridian, is greater than the ∠
BAN, which is the angle that the same
object, as taken by the circumferentor
on the surface, makes *to the left* with
the true meridian, the ∠ N'AN must be
to the right of the true meridian; there-
fore S'N' must have 10° of west variation.

3. Suppose N'S' to be the meridian of a plan whose
magnetic variation is required to be known; let the bearing
of the pit B from the pit A be taken on the plan with the

meridian thereon, equal to the angle BAN' 5°, or N 5° E; and let the bearing of the same two pits be taken on the surface by a circumferentor placed at A, whose needle has 23° of west variation ns, be found to form an angle BAn = 18°, or N 18° E; then if NS represent the true meridian, the line AB will form an angle therewith of 23° − 18° = 5° ∠ BAN, or N 5° W: Then ∠ BAN' 5° + ∠ BAN 5° = ∠ N'AN 10°, the variation of the plan's meridian; and as AB bears on different sides of the two meridians $N'S'$ and NS, and ∠ BAN being *to the left* of the true meridian NS, ∠ NAN' must be *to the left* thereof also; consequently the plan's meridian $N'S'$ must have 10° of west variation.

FIG. 69.
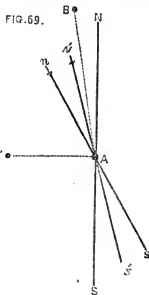
4. Suppose $N'S'$ (see last fig.), is the meridian of a plan whose magnetic variation is required to be known; let the bearing of the pit B' from the pit A be taken on the plan with its meridian, equal to the angle N'AB' 83°, or N 83° W; and let the bearing of the same two pits be taken on the surface by a circumferentor placed at A, whose needle has 23° of west variation ns, be found to form an angle nAB' = 70°, or N 70° W; then if NS represent the true meridian, the line AB' will form an angle therewith of 87° ∠ B'AS S 87° W (see Art. 52): Now ∠ N'AB' 83° + ∠ B'AS 87° = ∠ N'AS 170°, then 180° − 170° = 10° ∠ NAN', the variation of the plan's meridian; and as ∠ NAN' 10° is what ∠ SAN' falls short of 180°, reckoning from the south meridian S, therefore it must be *to the left or west* of the north meridian N; consequently the plan's meridian $N'S'$ must have 10° of west variation.

5. Suppose $N'S'$ to be the meridian of a plan whose magnetic variation is required; let the bearing of the pit B from the pit A be taken on the plan with its meridian

FIG 70
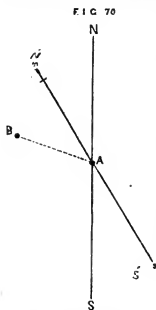
thereon, equal to the angle $N'AB$ 45°, or N 45° W; and let the bearing of the same two objects, taken on the surface by an instrument placed at A, whose needle has 23° of west variation ns, be found to be equal to the same angle nAB 45°, or N 45° W, as before; then if NS represent the true meridian, the line AB will form an angle therewith of 45° + 23° = 68° ∠ NAB, or N 68° W: Then ∠ NAB 68° − ∠ N'AB 45° = ∠ NAN' 23°, the variation of the plan's meridian; but as ∠ N'AB is *to the left* of the plan's meridian, and is less than ∠ NAB, the ∠ NAN' must be *to the left* of the true meridian SN; therefore the plan's meridian, will have 23° of west variation.—When the bearing of two objects, taken on a plan by its delineated meridian, agrees with the bearing of the same two objects taken on the surface by an instrument, the variation of the plan's meridian will be the same as the magnetic variation of the needle of that instrument.

6. Suppose $N'S'$ to be the meridian of a plan whose magnetic variation is required to be known; let the bearing of the pit B from that of A be taken on the plan by its meridian thereon, equal to the angle NAB 68°, or N 68° W: and let the bearing of the same two objects be taken by an instrument on the surface placed at A, whose needle has 23° of west variation ns, equal to the angle nAB 45°, or N 45° W; then the object will form an angle with the true

meridian of $45° + 23° = 68°$, or N $68°$ W: Now, as the bearing of the two objects on the plan with its meridian, agrees with the bearing of the same two objects taken on the surface when reduced to the true meridian, therefore the plan's meridian must be the true meridian.

From the several cases in the last Article, where six examples are solved, the method of solving the following unsolved examples will be readily seen.

EXAMPLE I.—I wish to know the variation of a plan's meridian, when the bearing of two objects thereon with its meridian is N $30°$ W, and the bearing of the same two objects with each other on the surface is found, by an instrument whose needle has $20°$ of west variation, to be N $19°$ W?

The objects on the surface will form a bearing with each other of N $39°$ W by the true meridian.

Then $39° − 30° = 9°$; therefore the plan's meridian has $9°$ of west variation.

EXAMPLE II.—I wish to know the variation of a plan's meridian, when the bearing of two objects thereon with its meridian is N $16°$ E, and the bearing of the same two objects with each other on the surface is found, by an instrument whose needle has $23°$ of west variation, to be N $10°$ E?

The objects on the surface will form a bearing with each other of N $13°$ W by the true meridian.

The $16° + 13° = 29°$; therefore the plan's meridian has $29°$ of west variation.

EXAMPLE III.—I have a plan which I wish to know by what kind of meridian it has been delineated: Now the bearing of two objects thereon with each other by its meridian is found to be N $80°$ W, and the bearing of the same two objects, taken on the surface by an instrument whose needle has $21°$ of west variation, is N $74°$ W?

The bearing of the two objects on the surface with the true meridian will be S $85°$ W.

Then $180° - \overline{80° + 85°} = 15°$; therefore the plan has been delineated by a meridian having 15° of west variation.

EXAMPLE IV.—I wish to know the variation of a plan's meridian, when the bearing of two objects taken thereon by its meridian is found to be N 40° E, and the bearing of the same two objects, taken on the surface by an instrument whose needle has 20° of west variation, is also N 40 E?

Then the meridian of the plan will have the same magnetic variation as the needle by which the bearing of the objects was taken on the surface; therefore the plan's meridian will have 20° of west variation.

EXAMPLE V.—I wish to know by what kind of meridian a plan has been constructed, when two objects thereon by its meridian form a bearing with each other of N 32° W, and the bearing of the same two objects, as taken on the surface by an instrument whose needle has 22° of west variation, forms a bearing with each other of N 10° W?

The two objects on the surface will form a bearing with each other of N 32° W by the true meridian.

Then the meridian of the plan will be the true meridian.

EXAMPLE VI.—I wish to know the variation of a plan's meridian, when the bearing of two objects thereon with its meridian is S 16° W, and the bearing of the same two objects with each other on the surface, taken by an instrument whose needle has 23° of west variation, is found to be S 10° W?

The plan's meridian will have 29° of west variation.

EXAMPLE VII.—I wish to know the variation of a plan's meridian, when the bearing of two objects thereon with its meridian is S 40° W, and the bearing of the same two objects with each other on the surface, taken by an instrument whose needle has 20° of west variation, is found to be S 23° W?

The plan's meridian will have 6° of east variation.

EXAMPLE VIII.—I wish to know the variation of a plan's meridian, when the bearing of two objects thereon

with its meridian is N 65° W, and the bearing of the same two objects with each other on the surface, taken by an instrument whose needle has 23° of west variation, is found to be N 20° W?

The plan's meridian will have 22° of east variation.

EXAMPLE IX.—I have a plan of a colliery workings, on which I took the bearing of two pits with each other by its meridian, which was N 5° W; I also took the bearing of the same two pits on the surface by an instrument whose needle had 23° of west variation, which was N 5° E; now I wish to know the variation of the plan's meridian by which it has been delineated?

The plan's meridian will have 13° of west variation.

EXAMPLE X.—I wish to know by what kind of meridian a plan of a colliery working has been constructed, when the bearing of two pits thereon with each other by its delineated meridian is found to be N 5° E, and the bearing of the same two pits on the surface with the true meridian is found to be N 14° W?

The plan has been constructed by a meridian having 19° of west variation.

How to plan surveys, and also the manner of determining an error arising in plotting, through inattention to the magnetic variation of the needle.

(55.) It has been shown, in Art. 49, that the magnetic meridian is always changing; therefore the bearings of the same objects, taken by such a meridian at different times, must also vary from each other, except reduced to bearings with the true meridian.

Let NS represent the meridian of a plan, which is also supposed to be the true meridian; and if a subterraneous excavation is to be plotted thereon from the pit A, which excavation is found to form a bearing of N 10° W 10 chains by an instrument whose needle had 20° of west variation;

now if the excavation N 10° W 10 chains is plotted on the plan by its meridian NS, which is the true meridian, it will

FIG. 7¹.

be represented by AB; but the bearing being taken by a needle having 20° of west variation, therefore (according to the manner of reducing bearings from one magnetic meridian to their bearings with any other, Art. 53) it should form a bearing of N 30° W with the meridian NS, as represented by A*b*; then A*b* will be the true direction of the excavation from the pit A, and *b*B will be the magnitude of the error (see theorem 8, Art. 48): Or, instead of reducing the excavation to its bearing with the true meridian NS, it will be equally as true if *ns* is drawn on the plan, and made to represent the magnetic meridian of the needle by which the bearing was taken, with which A*b* will form a bearing of N 10° W.

I shall insert a few examples, illustrative of the error arising from plotting a subterraneous survey on a plan without attending to the variation of the magnetic meridian, and also how its magnitude can be ascertained.

EXAMPLE I.—The following is a subterraneous survey, commencing at a pit called the B pit, N 30° W 6 chains, N 70° E 10 chains, N 30° E 5 chains, and N 25° W 8 chains, which was surveyed by an instrument whose needle had 24° of west variation; under what bearings must the survey be plotted on a plan whose delineated meridian has 15° of west variation?

Reduce the bearings, as taken by a meridian having 24° of west variation; to bearings with a meridian having 15° of west variation: Thus,—

Bearings with a meridian of 24° *of west variation.*		*Bearings with a meridian of 15° of west variation.*	
	Chains.		Chains.
N. 30° W.	. . 6	N. 39° W.	. . 6
N. 70° E.	. . 10	N. 61° E.	. . 10
N. 30° E.	. . 5	N. 21° E.	. . 5
N. 25° W.	. . 8	N. 34° W.	. . 8

The survey must be plotted under bearings with a magnetic meridian having 15° of west variation, as above, commencing at the B pit.

EXAMPLE II.—If the following subterraneous survey, N 9°.W 8 chains, N. 30° E 7 chains, and N 21° W 8 chains, is made by an instrument whose needle has 23° of west variation, and plotted on a plan by a meridian having 5°

of west magnetic variation, without being reduced thereto,—what will be the magnitude of the error resulting by such neglect?
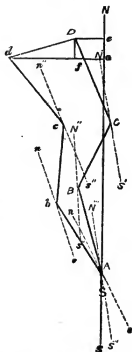
Suppose A, the point of commencement of the survey on the plan, and let the meridian of the plan here presented be $N^m S^m$, having 5° of west variation with the true meridian NS; then the first bearing, N 9° W 8 chains, will be represented by AB, — the second, N 30° E 7 chains, by BC,—and the third bearing, N 21° W 8 chains, by CD; then ABCD will represent the survey plotted without attending to the magnetic variation: But as the survey was made by an instrument whose needle had 23° of west variation, therefore each bearing, when truly plotted, must be set off from a meridian of that variation, which let *ns* represent;

FIG. 72.

then N 9° W 8 chains will be represented by A*b*, N 30° E
7 chains by *bc*, and N 21° W 8 chains by *cd*; then A*bcd*
will represent the survey truly plotted, and *d*D will be the
magnitude of the error.

Or the survey may be plotted by reducing the bearings,
as taken by a meridian of 23° of west variation, to bearings,
with a meridian of 5° of variation, as represented by *N'S'*,
and plotted from it accordingly, — which will exactly
coincide with A*bcd*, as before.

To discover, by calculation, the magnitude of the error,
reduce the bearings of the survey, as taken by a magnetic
meridian having 23° of west variation, to bearings with the
true meridian, — and also the same bearings, as if taken by
a meridian having 5° of west variation, to bearings with the
true meridian; then determine the northing and easting of
D from *d*: Thus, —

With a meridian of 23° of west variation.	With the true meridian.	With a meridian of 5° of west variation.	With the true meridian.
Chns.	Chns.	Chns.	Chns.
N. 9° W. 8	N. 32° W. 8	N. 9° W. 8	N. 14° W. 8
N. 30° E. 7	N. 7° E. 7	N. 30° E. 7	N. 25° E. 7
N. 21° W. 8	N. 44° W. 8	N. 21° W. 8	N. 26° W. 8

		Northing.	Southing.	Easting.	Westing.
	Chns.	Chains.	Chains.	Chains.	Chains.
N. 32° W. 8		6·78	...	...	4·23
N. 7° E. 7		6·94	...	0·85	...
N. 44° W. 8		5·75	...	...	5·55
		19·47	A*a*		9·73
					0·85
					8·93 *ad*

	Chns.	Northing. Chains.	Southing. Chains.	Easting. Chains.	Westing. Chains.	
N. 14° W.	8	7·76	...	...	1·93	
N. 25° E.	7	6·34	...	2·95	...	
N. 26° W.	8	7·19	...	...	3·50	
		21·29	A*e*		5·43	
					2·95	
					2·43	*c*D or *af*

ad 8·93 chains — *af* 2·48 chains = *fd* 6·45 chains.

A*e* 21·29 chains — A*a* 19·47 chains = *ae* or *f*D 1·82 chains.

$$
\begin{array}{llr}
\text{Then, as } fd \ 6\cdot45 & . \quad . \quad . & \cdot8095595 \\
\text{Is to radius} & . \quad . \quad . & 10\cdot0000000 \\
\text{So is } fD \ 1\cdot82 & . \quad . \quad . & \cdot2600714 \\
\text{To tang. } \angle\, d \ 15^\circ\ 45' & . \quad . & 9\cdot4505117
\end{array}
$$

From $90^\circ \overline{ - 15^\circ\ 45'} = 74^\circ\ 15'$, $\angle\, adD$.

And $\sqrt{6\cdot45 + 1\cdot82} = 6\cdot7\ dD$, or 6·70 chains.

Therefore the magnitude of the error, or the bearing and distance of D from *d*, will (from Art. 3) be N 74° 15′ E 6·70 chains with the true meridian.

EXAMPLE III.—If the following subterraneous survey S 30° W 4 chains, N 50° W 8 chains, N 50° E 9 chains, and N 53° W 8 chains, is surveyed by an instrument having 23° of west variation, and plotted on a plan by the true meridian, without being reduced thereto,—what will be magnitude of the error thereby?

Suppose A to be the point of commencement on the plan, and NS the true meridian thereon; then ABCDF will be the erroneous representation of the bearings and distances, as plotted from that meridian,—AB forming an angle of 30° therewith, BC an angle of 50° therewith, CD an angle of 50° therewith, and DF an angle of 53° therewith.

To plot the survey accurately, draw on the plan a meridian line *ns*, having 23° of west variation; each bearing and distance being then plotted from it, and *Abcdf* will represent the survey accurately done, and *f*F will be the magnitude of the error: Or, otherwise, if each bearing in the survey is reduced from the angle it formed with the magnetic meridian it was taken by, to the angle of bearing it will form with the plan's meridian, which is the true meridian, and plotted accordingly, the result will be the same : Thus,—
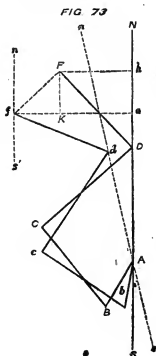
FIG 73

With a meridian having 23° of west variation.		With the true meridian.	
	Chains.		Chains.
S. 30° W.	4	S. 7° W.	4
N. 50° W.	8	N. 73° W.	8
N. 50° E.	9	N. 27° E.	9
N. 53° W.	8	N. 76° W.	8

Then A*b* will represent S 7° W 4 chains, *bc* N 73° W 8 chains, *cd* N 27° E 9 chains, and *df*, N 76° W 8 chains, the same as before.

	Chns.	Northing.	Southing.	Easting.	Westing.	
		Chains.	Chains.	Chains.	Chains.	
S. 30° W.	4	...	...	...	2·00	
N. 50° W.	8	5·14	...	...	6·13	
N. 50° E.	9	5·79	...	6·89	...	
N. 53° W.	8	4·81	...	...	6·39	
		15·74			14·52	
		3·46			6·89	
		12·28	Ah		7·63	hF or ak

	Chns.	Northing.	Southing.	Easting.	Westing.	
		Chains.	Chains.	Chains.	Chains.	
S. 7° W.	4	...	3·97	...	0·48	
N. 73° W.	8	2·33	...	...	7·65	
N. 27° E.	9	8·01	...	4·08	...	
N. 76° W.	8	1·93	...	...	7·76	
		12·27			15·89	
		3·97			4·08	
		8·30	Aa		11·81	af

From af 11·81 — ak 7·63 = kf 4·18.

Ah 12·28 — Aa 8·30 = ah or kF 3·98.

Then, as kf 4·18 . . . . . ·6211763

Is to radius . . . 10·0000000

So is kF 3·98 5998831

To tang. ∠ f 43° 35′ . . 9·9787068

From 90° — 43° 35′ = 46° 25′ ∠ nF.

And $\sqrt{4·18 + 3·98}$ = 5·77 fF chains.

Therefore the bearing of F from f with the true meridian will be N 46° 25′ E, and the distance will be 5·77 chains; which is the magnitude of the error.

EXAMPLE IV.—If the following subterraneous survey,

G

commencing at the pit A, S 30° W 4 chains, S 70° W 10 chains, and S 50° E 5 chains, was surveyed by an instru-

FIG. 74.
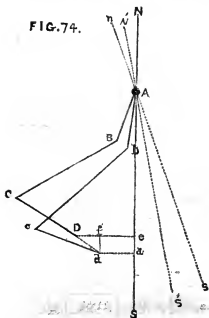
ment whose needle had 23° of west variation, and is plotted on a plan by a meridian having only 10° of variation to the west, without reduc-ing the bearings there-to ; what will be magni-tude of the error ?

If NS represent the true meridian,—*ns* the meridian, having 23° of west variation, by which the survey was taken,— and *N'S'* the meridian of the plan, having 10° of variation, by which the survey is to be plot-ted ; the ABCD will be the erroneous representation of the survey, as plotted by the meridian *N'S'* without reducing the bearings thereto. To plot the same truly,

With a meridian of 23° of west variation.			*With a meridian of 10° of west variation.*	
	Chains.			Chains.
S. 30° W.	. . 4		S. 17° W.	. . 4
S. 70° W.	. . 10		S. 57° W.	. . 10
S. 50° E.	. . 5		S. 63° E.	. . 5

Now make A*b* form an angle to the west with the meri-dian *N'S'* of 17°, *bc* an angle to the west of 57°, and *cd* an angle to the east of 63° ; then A*bcd* will represent the survey truly plotted, and the distance between D and *d* will be the magnitude of the error.

TO FIND THE MAGNITUDE OF THE ERROR.

With a meridian of 23° of west variation.	With the true meridian.	With a meridian of 10° of west variation.	With the true meridian.
Chns.	Chns.	Chns.	Chns.
S. 30° W. 4	S. 7° W. 4	S. 30° W. 4	S. 20° W. 4
S. 70° W. 10	S. 47° W. 10	S. 70° W. 10	S. 60° W. 10
S. 50° E. 5	S. 73° E. 5	S. 50° E. 5	S. 60° E. 5

	Northing.	Southing.	Easting.	Westing.	
Chns.	Chains.	Chains.	Chains.	Chains.	
S. 7° W. 4	...	3·79	...	0·49	
S. 47° W. 10	...	6·82	...	7·31	
S. 73° E. 5	...	1·46	4·78	...	
		12·25	Aa	7·80	
				4·78	
				3·02	ad

	Northing.	Southing.	Easting.	Westing.	
Chns.	Chains.	Chains.	Chains.	Chains.	
S. 20° W. 4	...	3·75	...	1·37	
S. 60° W. 10	...	5·00	...	8·66	
S. 60° E. 5	...	2·50	4·33	...	
		11·25	Ae	10·03	
				4·33	
				5·70	eD

Then Aa 12·25 — Ae 11·25 = ae or fd 1.

And eD 5·70 — ad 3·02 = fD 2·68.

$$\text{As } fD \text{ 2·68 .} \quad . \quad . \quad . \quad \cdot 4281348$$
$$\text{Is to radius .} \quad . \quad . \quad . \quad 10\cdot0000000$$
$$\text{So is } fd \text{ 1 .} \quad . \quad . \quad . \quad .$$
$$\text{To tang. } \angle \text{ D, 20° 27′} \quad . \quad 9\cdot5718652$$

From 90° — 20° 27′ = 69° 33′, $\angle fd$D.

And $\sqrt{2\cdot68 + 1} = 2\cdot86 = D$d.

a 2

Therefore the bearing of D from *d* with the true meridian will be N 69° 33′ W, and the distance will be 2·86 chains; which is the magnitude of the error.

EXAMPLE V.—The following subterraneous survey,— S 20° W 5 chains, S 70° W 10 chains, N 50° W 5 chains, and N 3° W 8 chains, was taken by an instrument having 23° of west variation, which I have to plot on a plan, the magnetic variation of the meridian by which it has been constructed is unknown; I therefore wish to know how the survey must be plotted, so that it may be accurately done?

In order to find by what kind of meridian the plan has been constructed, I took the bearing of two pits thereon by the delineated meridian, which I found to bear with each other N 25° W,—and the same two pits on the surface I found to bear N 22° W by an instrument whose needle had 23° of west variation; therefore the plan's meridian will have 20° of west variation, and the bearings of the survey must be reduced from a meridian of 23° of west variation to bearings with a meridian of 20° of the same variation, and plotted on the plan accordingly; Thus,—

Bearings with a meridian of 23° of west variation.		*Bearings with the plan's meridian of 20° of west variation.*	
	Chains.		Chains.
S. 20° W.	. . 5	S. 17° W.	. . 5
S. 70° W.	. . 10	S. 67° W.	. . 10
N. 50° W.	. . 5	N. 53° W.	. . 5
N. 3° W.	. . 8	N. 6° W.	. . 8

How to run bearings on the surface by a circumferentor, without error.

(56.) It frequently happens that the practical miner has to re-traverse on the surface the survey of a subterraneous excavation from bearings taken at some former time : Now, when that is the case, if the miner does it without attending to the change that has taken place with the magnetic meridian, between the taking of the survey and the re-

traversing it, an error must inevitably be the result; but where surveys are recorded without mentioning by what kind of meridian they were originally made, such surveys cannot be re-traversed with any degree of accuracy.

Suppose the bearing of a subterraneous excavation AB, is found to be N 20° W, which is taken by the needle of an instrument placed at the pit A, whose magnetic meridian is represented by NS; now, if the bearing of this excavation is run off on the surface from the pit A, immediately after it has been surveyed under-ground, and by the same instrument also, the excavation AB will be truly represented on the surface (see theorem 6, Art. 48); but if it should be necessary, at any future time, to have the same excavation represented on the surface by the same survey already made, and in that interval of time between the survey being made and its second plotting on the surface, the magnetic meridian NS has changed its situation to *ns*, the same excavation, N 20° W, run off from the then magnetic meridian *ns*, will be represented by A*b*, which will be erroneous: Therefore, to do the work truly, the bearing of AB, as originally taken by the meridian NS, must be reduced to its bearing with the meridian *ns*, and plotted on the surface from it accordingly (see theorem 7, Art. 48).

I shall insert a few examples relative to plotting bearings on the surface by different meridians.

EXAMPLE I.—The subterraneous excavation commencing at the pit A, N 20° W 5 chains AB, N 20° E 8 chains BC, N 70° E 5 chains CD, and S 70° E 5 chains DF, was surveyed by an instrument whose needle had 10° of west variation *ns*, and is to be plotted on the surface by another instrument whose needle has a different magnetic variation; how must it be plotted with accuracy?

First, find the magnetic variation of the needle of the
instrument by which the survey is to be plotted (see
Art. 51), which suppose it to have 23° of west variation
N S; then reduce the bearings, as taken by a meridian of
10° of west variation *ns*, to bearings with a meridian of 23°
of west variation N S.

EXAMPLE II.—If the following survey of a subterraneous
excavation, commencing at the pit A (see Fig. to Ex. IV.
Art. 55), S 30° W 4 chains, S 70° W 10 chains, and S 50°
E 5 chains, was surveyed by an instrument which had 10° of
west variation; what will be the magnitude of the error, if
the survey is plotted on the surface by another instrument
having 23° of west variation?

Let N'S' represent the magnetic meridian of the needle
of the instrument by which the survey was made, having
10° of west variation, and let ABCD represent the survey
as plotted on the surface thereby,—also let *ns* represent the
meridian of the instrument whose needle has 23° of west
variation, and A*bcd* the excavation as plotted according to
that meridian; then ABCD will be the survey plotted
truly, and A*bcd* the same plotted erroneously: Therefore,
from the manner of determining the magnitude of an error,
arising from plotting a survey by a different meridian than
that by which it was made (Art. 55), the error will be
2·86 chains,—which is the distance of *d* from D.

EXAMPLE III.—I have the survey of a subterraneous
excavation, commencing at a pit called the A pit; the
bearings are recorded to be taken by the true meridian,
viz., N 30° W 5 chains, due north 8 chains, N 80° E 5
chains, N 45½° W 10 chains, and N 23½° W 4 chains; how
is the survey to be truly delineated by an instrument on the
surface, so that a pit may be sunk on the extreme point of
the last bearing?

The first thing to be done, the surveyor must ascertain
the magnetic variation of the needle of the instrument by
which he intends delineating the survey (see Art. 49)

which suppose to be 23° 30′ to the west, and reduce the bearings of the survey thereto : Thus,—

Bearings with the true meridian.		Bearings with a meridian of 25° 30′ of west variation.	
	Chains.		Chains.
N. 30° W.	5	N. 6½° W.	5
N.	8	N. 23½° E.	8
N. 80° E.	5	N. 76½° E.	5
N. 45½° W.	10	N. 22° W.	10
N. 23½° W.	4	N.	4

Then fix the instrument at the A pit, and run off the first bearing and distance N 6½° W 5 chains, and the other following ones in regular order, and the end of the last N 4 chains, will be the place on the surface where the pit must be sunk, to hit the extreme point of the excavation.

To find the antiquity of a plan by its delineated meridian.

(57.) As the magnetic meridian has, for a great number of years past, been veering about to the west, hence plans constructed at different times must have their magnetic meridians of different variation ; those that are of the most ancient construction will have their meridians more easterly than those of a more modern date. Should a plan be found to have been constructed by a meridian having 11° 15′ of east variation, it will be reasonable to suppose it has been made about the year 1576 ; for at that time the magnetic meridian had 11° 15′ of east variation (see Table, Art. 49) : Or, if its meridian is found to have 20° of west variation, from the same principle it may be supposed to have been made about the year 1765.

EXAMPLE I.—If a plan is found to have a magnetic meridian of 18° of west variation, in what year has it been constructed ?

By looking in the table, Art. 49, it will appear to have been made about the year 1750.

EXAMPLE II.—I have a plan on which is a delineated meridian; I therefore wish to know in what year it has been made?

First find the magnetic variation of the meridian on the plan according to the rules for finding the same, Art. 54, which suppose to be 6° of east variation; then, by the table, Art. 49, it will appear to have been made about the year 1622.

The manner of recording subterraneous surveys.

(58.) As the necessity of recording surveys of subterraneous workings frequently occurs, I shall therefore show how the same ought to be recorded, so that they may answer the intended design: Thus,—

A recorded survey of a subterraneous excavation, taken June 10th, 1800, beginning at the centre of the A pit, in Blackburn colliery.

Each bearing being reduced to the true meridian.

		Chains.
N. 10° W.	. . . . .	5·50
N. 20° E.	. . . . .	4·20
N. 75° E.	. . . . .	10·10
E.	. . . . .	4·40
S. 71° E.	. . . . .	6·30
N. 50° E.	. . . . .	5·90

A recorded survey of a subterraneous working, taken November 21st, 1801, beginning at the centre of the Venture Pit, in Tanfield colliery.

Each bearing was taken by a needle having 23° of west variation, and recorded accordingly.

		Chains.
S. 50° W.	. . . . .	5·24
S. 30° W.	. . . . .	2·20
S. 86° W.	. . . . .	5·70
N. 40° W.	. . . . .	12·60

Now, either of these recorded surveys may be truly re-traversed on the surface of the earth, at any future time

with accuracy, by an instrument whose magnetic needle may have any known variation whatever, by referring to Art. 56.

The nature and use of the Traverse Tables.

(59.) Thus, if it is required to know the northing and easting of N 18° E 56 links,—look in the tables under the degree answering to the bearing, and to the right, opposite 56 in the column of bearing lengths, will be found 53 links and 26 hundred parts of a link of northing, and 17 links and 30 hundred parts of a link of easting. As the bearing length is links, the northing and easting must be links and parts of a link ; for in whatever denomination the bearing length is, in the same denomination must the integral part of the northing or southing and easting or westing be.

Also, if it is required to know the northing and easting of N 18° E 5·65 chains,—look in the table under the degree answering to the bearing, and opposite 5 chains in the bearing lengths will be found 4·76 chains of northing and 1·55 chains of easting ; then, for the remaining 65 links, look opposite 65 in the same column of bearing lengths, and there will be found 61·82 links of northing, and 20·09 links of easting,—which, added to the former northing and easting, will make 5·3782, or nearly 5·38 chains of northing, for the whole northing,—and 1·7509 chains, or 1·75 chains nearly, for the whole easting.

Suppose, again, the southing and westing of S 86° W 98·20 chains is required,—look in the tables under the degree of the bearing, and the southing and westing will be thus :—

Chains.	Chains.		Chains.	
For 98·00 there is	6·84	of southing and	97·76	of westing.
For 00·20	0· 1·40	of ditto	0·19·95	of ditto.
98·20	6·85·40	of southing and	97·95·95	of westing.
	or, 6·85⅜	of southing and	97·96	of westing nearly.

If the southing and easting of S 18½° E 20 chains is required,—take the southing and easting of the bearing length under 18°, and also under 19°, in manner before shewn, and half their sum will be the southing and easting required; thus:—

	Chains.	Chains.	Chains.
S. 18° E. 20 will have	19·02 of southing	6·18 of easting.	
S. 19° E. 20 will have	18·91 of ditto.	6·51 of ditto.	
	2)37·93	12·69	
	18·96 of southing	6·34 of easting.	

Therefore S 18½° E 20 chains will have 18·96 chains of southing and 6·34 chains of easting.

Again, if the northing and westing of N 75½° W 10·35 chains is required,—

	Chains.	Chains.	Chains.
N. 75° W. 10·35 will have	2·68·06 of northing	9·99·81 westing.	
N. 76° W. 10·35 will have	2·50·47 of ditto.	10·08·96 ditto.	
	2)5·18·53	20·08·77	
N. 75½° W. 10·35 will have	2·59·26 of northing	10·04·38 westing,	
or nearly	2·59¼ of northing	10·04⅜ westing.	

If the northing and easting of N 14° 37′ E 18 chains be required, take the northing and easting of the bearing length under 14° and the same under 15°; take the difference of each, multiply the respective differences by the number of minutes, i. e. 37′, and divide the products by 60 (the number of minutes in a degree), subtract the first quotient from the northing, and add the second to the easting; and the sum and difference will be the northing and easting required; thus—

N. 14° E. 18 chains will have 17·47 of northing, and 4·35 of easting.

N. 15° E.   „   „   17·39 of ditto,   „   4·66 of ditto.

·08 diff.		·31 diff.	
37		37	
60)29·6		60)114·7	
5 nearly.		19 nearly.	
14·47		4·35	

N. 14° 37′ E. 18 ch. will have 14·42 of northing, and 4·54 of easting.

The use of the Traverse Tables in reducing hypothenusal or inclined distances to horizontal distances.—(See Art. 45.)

(60.) When the table is used for the before-mentioned purpose, the column called bearing lengths represents the hypothenusal distance or longest side of a right-angled triangle, as CB; the column called N or S distance represents the horizontal distance AB; and the column called E or W distance represents the perpendicular AC.

FIC 76

If the horizontal distance AB or Ca is required, when the hypothenusal distance CB is 10 chains, and the angle aCB or CBA is 20°,—look in the table under 20°, and opposite 10, in the column of bearing lengths, will be found in the column of N or S distance 9·40, which will be 9·40 chains, equal to the horizontal distance AB or Ca.

If the horizontal distance AB or Ca is required, when the hypothenusal distance CB is 8 chains, and the angle aCB or CBA is 50°,—look in the tables under 50°, and opposite 8, in the column of bearing lengths, will be found 5·14 chains, in the column of N or S distance, which is equal to AB or Ca, the horizontal distance.

The horizontal distance of a line 20·50 chains, run under an angle of 15° of elevation, is required?

Look in the tables under 15°, and in the column of
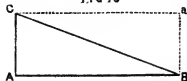
bearing lengths for 20·50 chains, the horizontal distance
will be thus :—

Chains.	Chains.
For 20·00 of hyp. distance	19·32 of horizontal distance.
For 0·50 of hyp. distance	0·48 of horizontal distance.
For 20·50 of hyp. distance	19·80 the whole horizontal distance.

Therefore, 20·50 chains of hypothenusal or inclining
length will be equal to 19 chains 80 links, or 19·80 chains
of horizontal distance.

TRAVERSE TABLES;

OR,

TABLES OF THE NORTHING OR SOUTHING,

AND

EASTING OR WESTING;

WHEREIN THE DISTANCE IS EXTENDED TO ONE HUNDRED,
FOR EVERY DEGREE OF THE QUADRANT.

¾°

Bearing Length	N. or S. Distance	E. or W. Distance	Bearing Length	N. or S. Distance	E. or W. Distance
1	1·00	0·01	51	51·00	0·45
2	2·00	0·02	52	52·00	0·45
3	3·00	0·03	53	53·00	0·46
4	4·00	0·04	54	54·00	0·46
5	5·00	0·04	55	55·00	0·48
6	6·00	0·05	56	56·00	0·49
7	7·00	0·06	57	57·00	0·50
8	8·00	0·07	58	58·00	0·51
9	9·00	0·08	59	59·00	0·52
10	10·00	0·09	60	60·00	0·52
11	11·00	0·10	61	61·00	0·53
12	12·00	0·10	62	62·00	0·54
13	13·00	0·11	63	63·00	0·54
14	14·00	0·12	64	64·00	0·56
15	15·00	0·13	65	65·00	0·56
16	16·00	0·13	66	66·00	0·57
17	17·00	0·14	67	67·00	0·58
18	18·00	0·15	68	68·00	0·59
19	19·00	0·16	69	69·00	0·60
20	20·00	0·17	70	70·00	0·61
21	21·00	0·18	71	71·00	0·62
22	22·00	0·18	72	72·00	0·63
23	23·00	0·19	73	73·00	0·63
24	24·00	0·20	74	74·00	0·64
25	25·00	0·21	75	75·00	0·65
26	26·00	0·22	76	76·00	0·66
27	27·00	0·23	77	77·00	0·67
28	28·00	0·24	78	78·00	0·68
29	29·00	0·25	79	79·00	0·69
30	30·00	0·26	80	80·00	0·70
31	31·00	0·27	81	81·00	0·71
32	32·00	0·27	82	82·00	0·72
33	33·00	0·28	83	83·00	0·73
34	34·00	0·29	84	84·00	0·74
35	35·00	0·30	85	85·00	0·74
36	36·00	0·31	86	86·00	0·75
37	37·00	0·32	87	87·00	0·76
38	38·00	0·33	88	88·00	0·77
39	39·00	0·34	89	89·00	0·78
40	40·00	0·35	90	90·00	0·79
41	41·00	0·36	91	91·00	0·80
42	42·00	0·37	92	92·00	0·81
43	43·00	0·37	93	93·00	0·81
44	44·00	0·38	94	94·00	0·82
45	45·00	0·39	95	95·00	0·83
46	46·00	0·40	96	96·00	0·84
47	47·00	0·41	97	97·00	0·85
48	48·00	0·42	98	98·00	0·85
49	49·00	0·43	99	99·00	0·86
50	50·00	0·44	100	100·00	0·87
	E. or W.	N. or S.		E. or W.	N. or S.

89¼°

1°

Bearing Length	N. or S. Distance	E. or W. Distance	Bearing Length	N. or S. Distance	E. or W. Distance
1	1·00	0·02	51	51·00	0·89
2	2·00	0·03	52	52·00	0·91
3	3·00	0·05	53	53·00	0·92
4	4·00	0·07	54	54·00	0·94
5	5·00	0·08	55	55·00	0·96
6	6·00	0·10	56	56·00	0·98
7	7·00	0·12	57	57·00	0·99
8	8·00	0·14	58	58·00	1·01
9	9·00	0·16	59	59·00	1·03
10	10·00	0·17	60	60·00	1·05
11	11·00	0·19	61	61·00	1·07
12	12·00	0·21	62	62·00	1·08
13	13·00	0·22	63	63·00	1·10
14	14·00	0·24	64	64·00	1·12
15	15·00	0·26	65	65·00	1·14
16	16·00	0·28	66	66·00	1·15
17	17·00	0·29	67	67·00	1·17
18	18·00	0·31	68	68·00	1·19
19	19·00	0·33	69	69·00	1·21
20	20·00	0·35	70	70·00	1·22
21	21·00	0·37	71	71·00	1·24
22	22·00	0·38	72	72·00	1·26
23	23·00	0·40	73	73·00	1·28
24	24·00	0·42	74	74·00	1·29
25	25·00	0·44	75	75·00	1·31
26	26·00	0·45	76	76·00	1·33
27	27·00	0·47	77	77·00	1·34
28	28·00	0·49	78	78·00	1·36
29	29·00	0·51	79	79·00	1·38
30	30·00	0·52	80	80·00	1·40
31	31·00	0·54	81	81·00	1·42
32	32·00	0·56	82	82·00	1·44
33	33·00	0·58	83	83·00	1·45
34	34·00	0·59	84	84·00	1·47
35	35·00	0·61	85	85·00	1·48
36	36·00	0·63	86	86·00	1·50
37	37·00	0·65	87	87·00	1·52
38	38·00	0·66	88	88·00	1·54
39	39·00	0·68	89	89·00	1·55
40	40·00	0·70	90	90·00	1·57
41	40·99	0·72	91	90·99	1·59
42	41·99	0·74	92	91·99	1·61
43	42·99	0·75	93	92·99	1·62
44	43·99	0·77	94	93·99	1·64
45	44·99	0·79	95	94·99	1·66
46	45·99	0·81	96	95·99	1·68
47	46·99	0·83	97	96·99	1·69
48	47·99	0·84	98	97·99	1·71
49	48·99	0·86	99	98·99	1·73
50	49·99	0·87	100	99·99	1·75
	E. or W.	N. or S.		E. or W.	N. or S.

89°

2°						3°					
Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	1.00	0.07	51	50.97	1.78	1	1.00	0.05	51	50.93	2.67
2	2.00	0.07	52	51.97	1.81	2	2.00	0.11	52	51.93	2.72
3	3.00	0.10	53	52.97	1.85	3	3.00	0.16	53	52.93	2.77
4	4.00	0.14	54	53.97	1.88	4	3.99	0.21	54	53.93	2.83
5	5.00	0.17	55	54.97	1.92	5	4.99	0.26	55	54.93	2.88
6	6.00	0.21	56	55.97	1.95	6	5.99	0.31	56	55.92	2.93
7	7.00	0.24	57	56.97	1.99	7	6.99	0.37	57	56.92	2.98
8	8.00	0.28	58	57.97	2.02	8	7.99	0.42	58	57.92	3.04
9	8.99	0.31	59	58.96	2.06	9	8.99	0.47	59	58.92	3.09
10	9.99	0.35	60	59.96	2.09	10	9.99	0.52	60	59.92	3.14
11	10.99	0.38	61	60.96	2.13	11	10.98	0.58	61	60.92	3.19
12	11.99	0.42	62	61.96	2.16	12	11.98	0.63	62	61.92	3.25
13	12.99	0.45	63	62.96	2.20	13	12.98	0.68	63	62.91	3.30
14	13.99	0.49	64	63.96	2.23	14	13.98	0.73	64	63.91	3.35
15	14.99	0.52	65	64.96	2.27	15	14.98	0.78	65	64.91	3.40
16	15.99	0.56	66	65.96	2.30	16	15.98	0.84	66	65.91	3.46
17	16.99	0.59	67	66.96	2.34	17	16.98	0.89	67	66.91	3.51
18	17.99	0.63	68	67.96	2.37	18	17.98	0.94	68	67.91	3.56
19	18.99	0.66	69	68.96	2.40	19	18.97	0.99	69	68.91	3.61
20	19.99	0.70	70	69.96	2.44	20	19.97	1.05	70	69.90	3.66
21	20.99	0.73	71	70.96	2.47	21	20.97	1.10	71	70.90	3.72
22	21.99	0.77	72	71.96	2.51	22	21.97	1.15	72	71.90	3.77
23	22.99	0.80	73	72.96	2.54	23	22.97	1.20	73	72.90	3.82
24	23.99	0.84	74	73.95	2.58	24	23.97	1.26	74	73.90	3.88
25	24.98	0.87	75	74.95	2.62	25	24.97	1.31	75	74.90	3.93
26	25.98	0.91	76	75.95	2.65	26	25.96	1.36	76	75.90	3.98
27	26.98	0.94	77	76.95	2.68	27	26.96	1.41	77	76.90	4.03
28	27.98	0.98	78	77.95	2.72	28	27.96	1.47	78	77.89	4.09
29	28.98	1.01	79	78.95	2.75	29	28.96	1.52	79	78.89	4.14
30	29.98	1.05	80	79.95	2.79	30	29.96	1.57	80	79.89	4.19
31	30.98	1.08	81	80.95	2.82	31	30.96	1.62	81	80.89	4.24
32	31.98	1.12	82	81.95	2.86	32	31.96	1.68	82	81.89	4.29
33	32.98	1.15	83	82.95	2.89	33	32.96	1.73	83	82.89	4.35
34	33.98	1.19	84	83.95	2.93	34	33.95	1.78	84	83.89	4.40
35	34.98	1.22	85	84.95	2.96	35	34.95	1.83	85	84.88	4.45
36	35.98	1.26	86	85.95	3.00	36	35.95	1.88	86	85.88	4.50
37	36.98	1.29	87	86.95	3.03	37	36.95	1.94	87	86.88	4.56
38	37.98	1.33	88	87.95	3.07	38	37.95	1.99	88	87.88	4.61
39	38.98	1.36	89	88.95	3.10	39	38.95	2.04	89	88.88	4.66
40	39.98	1.40	90	89.94	3.14	40	39.95	2.09	90	89.88	4.71
41	40.98	1.43	91	90.94	3.17	41	40.94	2.15	91	90.88	4.76
42	41.98	1.47	92	91.94	3.21	42	41.94	2.20	92	91.87	4.82
43	42.98	1.50	93	92.94	3.24	43	42.94	2.25	93	92.87	4.87
44	43.97	1.53	94	93.94	3.28	44	43.94	2.30	94	93.87	4.92
45	44.97	1.57	95	94.94	3.31	45	44.94	2.36	95	94.87	4.97
46	45.97	1.60	96	95.94	3.35	46	45.94	2.41	96	95.87	5.02
47	46.97	1.64	97	96.94	3.38	47	46.94	2.46	97	96.87	5.08
48	47.97	1.67	98	97.94	3.42	48	47.93	2.51	98	97.87	5.13
49	48.97	1.71	99	98.94	3.45	49	48.93	2.57	99	98.86	5.18
50	49.97	1.74	100	99.94	3.49	50	49.93	2.62	100	99.86	5.23
	E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.
		88°						87°			

Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.
		4°						5°			
1	1·00	0·07	51	50·88	3·56	1	1·00	0·09	51	50·81	4·45
2	1·99	0·14	52	51·87	3·63	2	1·99	0·17	52	51·80	4·53
3	2·99	0·21	53	52·87	3·70	3	2·99	0·26	53	52·80	4·62
4	3·99	0·28	54	53·87	3·77	4	3·98	0·35	54	53·79	4·71
5	4·99	0·35	55	54·87	3·84	5	4·98	0·44	55	54·79	4·79
6	5·99	0·42	56	55·86	3·91	6	5·98	0·52	56	55·79	4·88
7	6·98	0·49	57	56·86	3·98	7	6·97	0·61	57	56·78	4·97
8	7·98	0·56	58	57·86	4·05	8	7·97	0·70	58	57·78	5·06
9	8·98	0·63	59	58·86	4·12	9	8·97	0·78	59	58·78	5·14
10	9·98	0·70	60	59·85	4·19	10	9·96	0·87	60	59·77	5·23
11	10·97	0·77	61	60·85	4·26	11	10·96	0·96	61	60·77	5·32
12	11·97	0·84	62	61·85	4·33	12	11·95	1·05	62	61·76	5·41
13	12·97	0·91	63	62·85	4·39	13	12·95	1·13	63	62·76	5·49
14	13·97	0·98	64	63·84	4·46	14	13·95	1·22	64	63·76	5·58
15	14·96	1·05	65	64·84	4·53	15	14·94	1·31	65	64·75	5·67
16	15·96	1·12	66	65·84	4·60	16	15·94	1·39	66	65·75	5·75
17	16·96	1·19	67	66·84	4·67	17	16·94	1·48	67	66·75	5·84
18	17·96	1·26	68	67·83	4·74	18	17·93	1·57	68	67·74	5·93
19	18·95	1·33	69	68·83	4·81	19	18·93	1·66	69	68·74	6·01
20	19·95	1·40	70	69·83	4·88	20	19·92	1·74	70	69·73	6·10
21	20·95	1·47	71	70·83	4·95	21	20·92	1·83	71	70·73	6·19
22	21·94	1·54	72	71·82	5·02	22	21·92	1·92	72	71·73	6·28
23	22·94	1·61	73	72·82	5·09	23	22·91	2·00	73	72·72	6·37
24	23·94	1·68	74	73·82	5·16	24	23·91	2·09	74	73·72	6·45
25	24·94	1·75	75	74·82	5·23	25	24·91	2·18	75	74·72	6·54
26	25·94	1·82	76	75·81	5·30	26	25·90	2·27	76	75·71	6·63
27	26·93	1·89	77	76·81	5·37	27	26·90	2·35	77	76·71	6·71
28	27·93	1·96	78	77·81	5·44	28	27·89	2·44	78	77·70	6·80
29	28·93	2·03	79	78·81	5·51	29	28·89	2·53	79	78·70	6·89
30	29·93	2·09	80	79·80	5·58	30	29·89	2·61	80	79·70	6·97
31	30·92	2·16	81	80·80	5·65	31	30·88	2·70	81	80·69	7·06
32	31·92	2·23	82	81·80	5·72	32	31·88	2·79	82	81·69	7·15
33	32·92	2·30	83	82·80	5·79	33	32·88	2·88	83	82·68	7·24
34	33·92	2·37	84	83·80	5·86	34	33·87	2·96	84	83·68	7·32
35	34·91	2·44	85	84·79	5·93	35	34·87	3·05	85	84·68	7·41
36	35·91	2·51	86	85·79	6·00	36	35·86	3·14	86	85·67	7·50
37	36·91	2·58	87	86·79	6·07	37	36·86	3·23	87	86·67	7·58
38	37·91	2·65	88	87·79	6·14	38	37·85	3·31	88	87·66	7·67
39	38·90	2·72	89	88·78	6·21	39	38·85	3·40	89	88·66	7·76
40	39·90	2·79	90	89·78	6·28	40	39·85	3·49	90	89·66	7·84
41	40·90	2·86	91	90·78	6·35	41	40·84	3·57	91	90·65	7·93
42	41·90	2·93	92	91·78	6·42	42	41·84	3·66	92	91·65	8·02
43	42·90	3·00	93	92·77	6·49	43	42·84	3·75	93	92·65	8·11
44	43·89	3·07	94	93·77	6·56	44	43·83	3·84	94	93·64	8·19
45	44·89	3·14	95	94·77	6·63	45	44·83	3·92	95	94·64	8·28
46	45·89	3·21	96	95·77	6·70	46	45·83	4·01	96	95·64	8·37
47	46·89	3·28	97	96·76	6·77	47	46·82	4·10	97	96·63	8·45
48	47·88	3·35	98	97·76	6·84	48	47·82	4·18	98	97·63	8·54
49	48·88	3·42	99	98·76	6·91	49	48·81	4·27	99	98·63	8·63
50	49·88	3·49	100	99·76	6·98	50	49·81	4·36	100	99·62	8·72
	E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.
		86°						85°			

6°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·99	0·10	51	50·72	5·33
2	1·99	0·21	52	51·72	5·44
3	2·98	0·31	53	52·71	5·54
4	3·98	0·42	54	53·71	5·64
5	4·97	0·52	55	54·70	5·75
6	5·97	0·63	56	55·69	5·85
7	6·96	0·73	57	56·69	5·96
8	7·96	0·84	58	57·68	6·06
9	8·95	0·94	59	58·68	6·17
10	9·95	1·05	60	59·67	6·27
11	10·94	1·15	61	60·67	6·38
12	11·93	1·25	62	61·66	6·48
13	12·93	1·36	63	62·65	6·59
14	13·92	1·46	64	63·65	6·69
15	14·92	1·57	65	64·64	6·79
16	15·91	1·67	66	65·64	6·90
17	16·91	1·78	67	66·63	7·00
18	17·90	1·88	68	67·63	7·11
19	18·90	1·99	69	68·62	7·21
20	19·89	2·09	70	69·62	7·32
21	20·88	2·20	71	70·61	7·42
22	21·88	2·30	72	71·61	7·53
23	22·87	2·41	73	72·60	7·63
24	23·87	2·51	74	73·59	7·74
25	24·86	2·62	75	74·59	7·84
26	25·86	2·72	76	75·58	7·94
27	26·85	2·82	77	76·58	8·05
28	27·85	2·93	78	77·57	8·15
29	28·84	3·03	79	78·57	8·26
30	29·84	3·14	80	79·56	8·36
31	30·83	3·24	81	80·55	8·47
32	31·82	3·34	82	81·55	8·57
33	32·82	3·45	83	82·55	8·68
34	33·81	3·55	84	83·54	8·78
35	34·81	3·66	85	84·53	8·89
36	35·80	3·76	86	85·53	8·99
37	36·80	3·87	87	86·52	9·10
38	37·79	3·97	88	87·52	9·20
39	38·79	4·08	89	88·51	9·31
40	39·78	4·18	90	89·51	9·41
41	40·77	4·29	91	90·50	9·52
42	41·77	4·39	92	91·50	9·62
43	42·76	4·49	93	92·49	9·73
44	43·76	4·60	94	93·48	9·83
45	44·75	4·70	95	94·48	9·93
46	45·74	4·81	96	95·47	10·04
47	46·74	4·91	97	96·47	10·14
48	47·74	5·02	98	97·46	10·24
49	48·73	5·12	99	98·46	10·35
50	49·73	5·23	100	99·45	10·45
	E. or W.	N. or S.		E. or W.	N. or S.

84°

7°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·99	0·12	51	50·62	6·22
2	1·99	0·24	52	51·61	6·34
3	2·98	0·37	53	52·60	6·46
4	3·97	0·49	54	53·60	6·58
5	4·96	0·61	55	54·59	6·70
6	5·96	0·73	56	55·58	6·82
7	6·94	0·85	57	56·57	6·95
8	7·94	0·98	58	57·57	7·07
9	8·93	1·10	59	58·56	7·19
10	9·93	1·22	60	59·55	7·31
11	10·92	1·34	61	60·54	7·43
12	11·91	1·46	62	61·54	7·56
13	12·90	1·58	63	62·53	7·68
14	13·90	1·71	64	63·52	7·80
15	14·89	1·83	65	64·51	7·92
16	15·88	1·95	66	65·51	8·04
17	16·87	2·07	67	66·50	8·17
18	17·87	2·19	68	67·49	8·29
19	18·86	2·32	69	68·48	8·41
20	19·85	2·44	70	69·48	8·53
21	20·84	2·56	71	70·47	8·65
22	21·84	2·68	72	71·46	8·77
23	22·83	2·80	73	72·45	8·90
24	23·82	2·92	74	73·45	9·02
25	24·81	3·05	75	74·44	9·14
26	25·81	3·17	76	75·43	9·26
27	26·80	3·29	77	76·42	9·38
28	27·79	3·41	78	77·42	9·50
29	28·79	3·53	79	78·41	9·63
30	29·78	3·66	80	79·40	9·75
31	30·77	3·78	81	80·39	9·87
32	31·76	3·90	82	81·39	9·99
33	32·75	4·02	83	82·38	10·12
34	33·75	4·14	84	83·37	10·24
35	34·74	4·27	85	84·36	10·36
36	35·73	4·39	86	85·36	10·48
37	36·72	4·51	87	86·35	10·60
38	37·72	4·63	88	87·34	10·73
39	38·71	4·75	89	88·33	10·85
40	39·70	4·87	90	89·33	10·97
41	40·69	5·00	91	90·32	11·09
42	41·69	5·12	92	91·31	11·21
43	42·68	5·24	93	92·30	11·33
44	43·67	5·36	94	93·30	11·45
45	44·66	5·48	95	94·29	11·58
46	45·66	5·61	96	95·28	11·70
47	46·65	5·73	97	96·26	11·82
48	47·64	5·86	98	97·27	11·94
49	48·63	5·97	99	98·26	12·07
50	49·63	6·10	100	99·26	12·19
	E. or W.	N. or S.		E. or W.	N. or S.

83°

8°

Bearing Lengths, Distance	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·99	0·14	51	50·50	7·10
2	1·98	0·27	52	51·49	7·24
3	2·97	0·42	53	52·48	7·38
4	3·96	0·56	54	53·47	7·52
5	4·95	0·70	55	54·46	7·65
6	5·94	0·84	56	55·46	7·79
7	6·93	0·97	57	56·45	7·93
8	7·92	1·11	58	57·44	8·07
9	8·91	1·25	59	58·43	8·21
10	9·90	1·39	60	59·42	8·35
11	10·89	1·53	61	60·41	8·49
12	11·88	1·67	62	61·40	8·63
13	12·87	1·81	63	62·39	8·77
14	13·86	1·95	64	63·38	8·91
15	14·85	2·09	65	64·37	9·05
16	15·84	2·23	66	65·36	9·19
17	16·83	2·37	67	66·35	9·32
18	17·82	2·51	68	67·34	9·46
19	18·82	2·64	69	68·33	9·60
20	19·81	2·78	70	69·32	9·74
21	20·80	2·92	71	70·31	9·88
22	21·79	3·06	72	71·00	10·02
23	22·78	3·20	73	72·29	10·16
24	23·77	3·34	74	73·28	10·30
25	24·76	3·45	75	74·27	10·44
26	25·75	3·62	76	75·26	10·58
27	26·74	3·76	77	76·25	10·72
28	27·73	3·90	78	77·24	10·86
29	28·72	4·04	79	78·23	10·99
30	29·71	4·18	80	79·22	11·13
31	30·70	4·31	81	80·21	11·27
32	31·69	4·45	82	81·20	11·41
33	32·68	4·59	83	82·19	11·55
34	33·67	4·73	84	83·18	11·69
35	34·66	4·87	85	84·18	11·83
36	35·65	5·01	86	85·16	11·97
37	36·64	5·15	87	86·15	12·11
38	37·63	5·29	88	87·14	12·25
39	38·62	5·43	89	88·13	12·39
40	39·61	5·57	90	89·12	12·53
41	40·60	5·71	91	90·11	12·66
42	41·59	5·85	92	91·10	12·80
43	42·58	5·99	93	92·09	12·94
44	43·57	6·12	94	93·09	13·08
45	44·56	6·27	95	94·08	13·22
46	45·55	6·40	96	95·07	13·36
47	46·54	6·54	97	96·06	13·50
48	47·53	6·68	98	97·05	13·64
49	48·52	6·82	99	98·04	13·78
50	49·51	6·96	100	99·03	13·92
	E. or W.	N. or S.		E. or W.	N. or S.

9°

Bearing Lengths, Distance	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·99	0·16	51	50·37	7·98
2	1·98	0·31	52	51·36	8·13
3	2·96	0·47	53	52·35	8·29
4	3·95	0·63	54	53·34	8·45
5	4·94	0·78	55	54·33	8·60
6	5·93	0·94	56	55·31	8·76
7	6·91	1·10	57	56·30	8·92
8	7·90	1·25	58	57·29	9·07
9	8·89	1·41	59	58·28	9·23
10	9·88	1·56	60	59·26	9·39
11	10·86	1·72	61	60·25	9·54
12	11·85	1·88	62	61·24	9·70
13	12·84	2·03	63	62·22	9·86
14	13·83	2·19	64	63·21	10·01
15	14·82	2·35	65	64·20	10·17
16	15·80	2·50	66	65·19	10·32
17	16·79	2·66	67	66·18	10·48
18	17·78	2·82	68	67·16	10·54
19	18·77	2·97	69	68·15	10·79
20	19·75	3·13	70	69·14	10·95
21	20·74	3·29	71	70·18	11·11
22	21·73	3·44	72	71·11	11·26
23	22·72	3·60	73	72·10	11·42
24	23·70	3·75	74	73·09	11·58
25	24·69	3·91	75	74·08	11·73
26	25·68	4·07	76	75·06	11·89
27	26·67	4·22	77	76·05	12·05
28	27·66	4·38	78	77·04	12·20
29	28·64	4·54	79	78·03	12·36
30	29·63	4·69	80	79·02	12·52
31	30·62	4·85	81	80·00	12·67
32	31·61	5·01	82	80·99	12·83
33	32·59	5·16	83	81·98	12·98
34	33·58	5·32	84	82·97	13·14
35	34·57	5·48	85	83·96	13·30
36	35·56	5·63	86	84·94	13·45
37	36·54	5·79	87	85·93	13·61
38	37·53	5·94	88	86·92	13·77
39	38·52	6·10	89	87·90	13·92
40	39·50	6·26	90	88·89	14·08
41	40·50	6·41	91	89·88	14·24
42	41·48	6·57	92	90·87	14·39
43	42·47	6·73	93	91·86	14·55
44	43·46	6·88	94	92·85	14·70
45	44·45	7·04	95	93·83	14·86
46	45·43	7·20	96	94·82	15·02
47	46·42	7·35	97	95·81	15·17
48	47·41	7·51	98	96·80	15·33
49	48·40	7·67	99	97·78	15·49
50	49·38	7·82	100	98·77	15·64
	E. or W.	N. or S.		E. or W.	N. or S.

82°   81°

	10°						11°				
Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.
1	0·99	0·17	51	50·23	8·86	1	0·98	0·19	51	50·06	9·73
2	1·97	0·35	52	51·21	9·03	2	1·96	0·38	52	51·04	9·92
3	2·95	0·52	53	52·19	9·20	3	2·94	0·57	53	52·03	10·11
4	3·94	0·70	54	53·18	9·38	4	3·93	0·76	54	53·01	10·30
5	4·92	0·87	55	54·16	9·55	5	4·91	0·95	55	53·99	10·49
6	5·91	1·04	56	55·15	9·72	6	5·89	1·14	56	54·97	10·68
7	6·89	1·22	57	56·13	9·90	7	6·87	1·34	57	55·95	10·88
8	7·88	1·39	58	57·12	10·07	8	7·85	1·53	58	56·93	11·07
9	8·86	1·56	59	58·10	10·25	9	8·83	1·72	59	57·92	11·26
10	9·85	1·74	60	59·09	10·42	10	9·82	1·91	60	58·90	11·45
11	10·83	1·91	61	60·07	10·59	11	10·80	2·10	61	59·88	11·64
12	11·82	2·08	62	61·06	10·77	12	11·78	2·29	62	60·86	11·83
13	12·80	2·26	63	62·04	10·94	13	12·76	2·48	63	61·84	12·02
14	13·79	2·43	64	63·03	11·11	14	13·74	2·67	64	62·82	12·21
15	14·77	2·60	65	64·01	11·29	15	14·72	2·86	65	63·80	12·40
16	15·76	2·78	66	65·00	11·46	16	15·71	3·05	66	64·79	12·59
17	16·74	2·95	67	65·98	11·63	17	16·69	3·24	67	65·77	12·78
18	17·73	3·12	68	66·97	11·81	18	17·67	3·43	68	66·75	12·98
19	18·71	3·30	69	67·95	11·98	19	18·65	3·63	69	67·73	13·17
20	19·70	3·47	70	68·94	12·16	20	19·63	3·82	70	68·71	13·36
21	20·68	3·65	71	69·92	12·33	21	20·61	4·01	71	69·69	13·55
22	21·67	3·82	72	70·91	12·50	22	21·60	4·20	72	70·68	13·74
23	22·65	3·99	73	71·89	12·68	23	22·58	4·39	73	71·66	13·93
24	23·64	4·17	74	72·88	12·85	24	23·56	4·58	74	72·64	14·12
25	24·62	4·34	75	73·86	13·02	25	24·54	4·77	75	73·62	14·31
26	25·60	4·51	76	74·85	13·20	26	25·52	4·96	76	74·60	14·50
27	26·59	4·69	77	75·83	13·37	27	26·50	5·15	77	75·58	14·69
28	27·57	4·86	78	76·82	13·54	28	27·49	5·34	78	76·57	14·88
29	28·56	5·04	79	77·80	13·72	29	28·47	5·53	79	77·55	15·07
30	29·54	5·21	80	78·78	13·89	30	29·45	5·72	80	78·53	15·26
31	30·53	5·38	81	79·77	14·07	31	30·43	5·92	81	79·51	15·46
32	31·51	5·56	82	80·75	14·24	32	31·41	6·11	82	80·49	15·65
33	32·50	5·73	83	81·74	14·41	33	32·39	6·30	83	81·47	15·84
34	33·48	5·90	84	82·72	14·59	34	33·37	6·49	84	82·46	16·03
35	34·47	6·08	85	83·71	14·76	35	34·36	6·68	85	83·44	16·22
36	35·45	6·25	86	84·69	14·93	36	35·34	6·87	86	84·42	16·41
37	36·44	6·43	87	85·68	15·11	37	36·32	7·06	87	85·40	16·60
38	37·42	6·60	88	86·66	15·28	38	37·30	7·25	88	86·38	16·79
39	38·41	6·77	89	87·65	15·45	39	38·28	7·44	89	87·36	16·98
40	39·39	6·95	90	88·63	15·63	40	39·26	7·63	90	88·35	17·17
41	40·38	7·12	91	89·62	15·80	41	40·25	7·82	91	89·33	17·36
42	41·36	7·29	92	90·60	15·98	42	41·23	8·01	92	90·31	17·55
43	42·35	7·47	93	91·59	16·15	43	42·21	8·20	93	91·29	17·75
44	43·33	7·64	94	92·57	16·32	44	43·19	8·40	94	92·27	17·94
45	44·32	7·81	95	93·56	16·50	45	44·17	8·59	95	93·25	18·13
46	45·30	7·99	96	94·54	16·67	46	45·15	8·78	96	94·24	18·32
47	46·29	8·16	97	95·53	16·84	47	46·14	8·97	97	95·22	18·51
48	47·27	8·34	98	96·51	17·02	48	47·12	9·16	98	96·20	18·70
49	48·26	8·51	99	97·50	17·19	49	48·10	9·35	99	97·18	18·89
50	49·24	8·68	100	98·48	17·37	50	49·08	9·54	100	98·16	19·08
	E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.

	12°					13°			
Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.
1	0·98	0·21	51	49·89	10·60	1	0·97	0·22	51	49·69	11·47
2	1·96	0·42	52	50·86	10·81	2	1·95	0·45	52	50·67	11·70
3	2·93	0·62	53	51·84	11·02	3	2·92	0·67	53	51·64	11·92
4	3·91	0·83	54	52·82	11·23	4	3·90	0·90	54	52·62	12·15
5	4·89	1·04	55	53·80	11·44	5	4·87	1·12	55	53·59	12·37
6	5·87	1·25	56	54·78	11·64	6	5·75	1·35	56	54·57	12·60
7	6·85	1·46	57	55·75	11·85	7	6·82	1·57	57	55·54	12·82
8	7·83	1·66	58	56·73	12·06	8	7·79	1·80	58	56·51	13·05
9	8·80	1·87	59	57·71	12·27	9	8·77	2·02	59	57·49	13·27
10	9·78	2·08	60	58·69	12·47	10	9·74	2·25	60	58·46	13·50
11	10·76	2·29	61	59·67	12·68	11	10·72	2·47	61	59·44	13·72
12	11·74	2·49	62	60·65	12·89	12	11·69	2·70	62	60·41	13·95
13	12·72	2·70	63	61·62	13·10	13	12·67	2·92	63	61·39	14·17
14	13·69	2·91	64	62·60	13·31	14	13·64	3·15	64	62·36	14·40
15	14·67	3·12	65	63·58	13·51	15	14·62	3·37	65	63·33	14·62
16	15·65	3·33	66	64·54	13·72	16	15·59	3·60	66	64·31	14·85
17	16·63	3·53	67	65·54	13·93	17	16·56	3·82	67	65·28	15·07
18	17·61	3·74	68	66·51	14·14	18	17·54	4·05	68	66·26	15·30
19	18·58	3·95	69	67·49	14·35	19	18·51	4·27	69	67·23	15·52
20	19·56	4·16	70	68·47	14·55	20	19·49	4·50	70	68·21	15·75
21	20·54	4·37	71	69·45	14·76	21	20·46	4·72	71	69·18	15·97
22	21·52	4·57	72	70·43	14·97	22	21·44	4·95	72	70·16	16·20
23	22·50	4·78	73	71·40	15·18	23	22·41	5·17	73	71·13	16·42
24	23·48	4·99	74	72·38	15·39	24	23·38	5·40	74	72·10	16·65
25	24·45	5·20	75	73·36	15·59	25	24·36	5·62	75	73·08	16·87
26	25·43	5·41	76	74·34	15·80	26	25·33	5·85	76	74·05	17·10
27	26·41	5·61	77	75·32	16·01	27	26·31	6·07	77	75·03	17·32
28	27·39	5·82	78	76·30	16·22	28	27·28	6·30	78	76·00	17·55
29	28·37	6·03	79	77·27	16·43	29	28·26	6·52	79	76·98	17·77
30	29·34	6·24	80	78·25	16·63	30	29·23	6·75	80	77·95	18·00
31	30·32	6·45	81	79·23	16·84	31	30·21	6·97	81	78·92	18·22
32	31·30	6·65	82	80·21	17·05	32	31·18	7·20	82	79·90	18·45
33	32·28	6·86	83	81·19	17·26	33	32·15	7·42	83	80·87	18·67
34	33·26	7·07	84	82·16	17·46	34	33·13	7·65	84	81·85	18·90
35	34·24	7·28	85	83·14	17·67	35	34·10	7·87	85	82·82	19·12
36	35·21	7·48	86	84·12	17·88	36	35·08	8·10	86	83·80	19·35
37	36·19	7·69	87	85·10	18·09	37	36·05	8·32	87	84·77	19·57
38	37·17	7·90	88	86·08	18·30	38	37·03	8·55	88	85·74	19·80
39	38·15	8·11	89	87·06	18·50	39	38·00	8·77	89	86·72	20·02
40	39·13	8·32	90	88·03	18·71	40	38·97	9·00	90	87·69	20·25
41	40·10	8·52	91	89·01	19·92	41	39·95	9·22	91	88·67	20·47
42	41·08	8·73	92	89·99	19·13	42	40·92	9·45	92	89·64	20·70
43	42·06	8·94	93	90·97	19·34	43	41·90	9·67	93	90·62	20·92
44	43·04	9·15	94	91·95	19·54	44	42·87	9·90	94	91·59	21·15
45	44·02	9·36	95	92·92	19·75	45	43·85	10·12	95	92·57	21·37
46	44·99	9·56	96	93·90	19·96	46	44·82	10·35	96	93·54	21·60
47	45·97	9·77	97	94·88	20·17	47	45·80	10·57	97	94·51	21·82
48	46·95	9·98	98	95·86	20·38	48	46·77	10·80	98	95·49	22·05
49	47·93	10·19	99	96·84	20·58	49	47·74	11·02	99	96·46	22·27
50	48·91	10·40	100	97·81	20·79	50	48·72	11·25	100	97·44	22·50
	E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.
		78°						77°			

14°						15°				
N. or S. Distance	E. or W. Distance	Bearing Length	N. or S. Distance	E. or W. Distance	Bearing Length	N. or S. Distance	E. or W. Distance	Bearing Length	N. or S. Distance	E. or W. Distance
0.97	0.24	51	49.49	12.34	1	0.97	0.26	51	49.26	13.20
1.94	0.48	52	50.46	12.58	2	1.93	0.52	52	50.23	13.46
2.91	0.72	53	51.43	12.82	3	2.90	0.78	53	51.19	13.73
3.88	0.97	54	52.40	13.06	4	3.86	1.04	54	52.16	13.99
4.85	1.21	55	53.37	13.31	5	4.83	1.29	55	53.13	14.24
5.82	1.45	56	54.34	13.55	6	5.80	1.55	56	54.09	14.49
6.79	1.69	57	55.31	13.79	7	6.77	1.81	57	55.06	14.75
7.76	1.93	58	56.28	14.03	8	7.73	2.07	58	56.02	15.01
8.73	2.18	59	57.25	14.27	9	8.69	2.33	59	56.99	15.27
9.70	2.42	60	58.22	14.52	10	9.66	2.59	60	57.96	15.53
10.67	2.66	61	59.19	14.76	11	10.63	2.85	61	58.92	15.79
11.64	2.90	62	60.16	15.00	12	11.59	3.11	62	59.89	16.05
12.61	3.14	63	61.13	15.24	13	12.56	3.36	63	60.85	16.31
13.58	3.39	64	62.10	15.48	14	13.52	3.62	64	61.82	16.56
14.55	3.63	65	63.07	15.72	15	14.49	3.88	65	62.79	16.82
15.52	3.87	66	64.04	15.97	16	15.45	4.14	66	63.75	17.08
16.50	4.11	67	65.01	16.21	17	16.42	4.40	67	64.72	17.34
17.47	4.35	68	65.98	16.45	18	17.39	4.66	68	65.68	17.60
18.44	4.60	69	66.95	16.69	19	18.35	4.92	69	66.65	17.86
19.41	4.84	70	67.92	16.94	20	19.32	5.18	70	67.61	18.12
20.38	5.08	71	68.89	17.18	21	20.28	5.44	71	68.58	18.38
21.35	5.32	72	69.86	17.42	22	21.25	5.69	72	69.55	18.64
22.32	5.56	73	70.83	17.66	23	22.22	5.95	73	70.51	18.89
23.29	5.81	74	71.80	17.90	24	23.18	6.21	74	71.48	19.15
24.26	6.05	75	72.77	18.14	25	24.15	6.47	75	72.44	19.41
25.23	6.29	76	73.74	18.39	26	25.11	6.73	76	73.41	19.67
26.20	6.53	77	74.71	18.63	27	26.08	6.99	77	74.38	19.93
27.17	6.77	78	75.68	18.87	28	27.05	7.25	78	75.34	20.19
28.14	7.02	79	76.65	19.11	29	28.01	7.51	79	76.31	20.45
29.11	7.26	80	77.62	19.35	30	28.98	7.76	80	77.27	20.71
30.08	7.50	81	78.59	19.60	31	29.94	8.02	81	78.24	20.96
31.05	7.74	82	79.56	19.84	32	30.91	8.28	82	79.21	21.22
32.02	7.98	83	80.53	20.08	33	31.88	8.54	83	80.17	21.48
32.99	8.23	84	81.50	20.32	34	32.84	8.80	84	81.14	21.74
33.96	8.47	85	82.48	20.56	35	33.81	9.06	85	82.10	22.00
34.93	8.71	86	83.45	20.81	36	34.77	9.32	86	83.07	22.26
35.90	8.95	87	84.42	21.05	37	35.74	9.58	87	84.04	22.52
36.87	9.19	88	85.39	21.29	38	36.71	9.84	88	85.00	22.78
37.84	9.43	89	86.36	21.53	39	37.67	10.09	89	85.97	23.03
38.81	9.68	90	87.33	21.77	40	38.64	10.35	90	86.93	23.29
39.78	9.92	91	88.30	22.01	41	39.60	10.61	91	87.90	23.55
40.75	10.16	92	89.27	22.26	42	40.57	10.87	92	88.87	23.81
41.72	10.40	93	90.24	22.50	43	41.53	11.13	93	89.83	24.07
42.69	10.64	94	91.21	22.74	44	42.50	11.39	94	90.80	24.33
43.66	10.88	95	92.18	22.98	45	43.47	11.65	95	91.76	24.59
44.63	11.13	96	93.15	23.22	46	44.43	11.91	96	92.73	24.85
45.60	11.37	97	94.12	23.47	47	45.40	12.16	97	93.70	25.11
46.57	11.61	98	95.09	23.71	48	46.36	12.42	98	94.66	25.36
47.54	11.85	99	96.06	23.95	49	47.33	12.68	99	95.63	25.62
48.51	12.10	100	97.03	24.19	50	48.30	12.94	100	96.59	25.88
E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.
		76°						75°		

	16°						17°				
Bearing Length.	N. or S. Distance.	E. or W. Distance.	Bearing Length.	N. or S. Distance.	E. or W. Distance.	Bearing Length.	N. or S. Distance.	E. or W. Distance.	Bearing Length.	N. or S. Distance.	E. or W. Distance.
1	0·96	0·28	51	49·02	14·06	1	0·96	0·29	51	48·77	14·91
2	1·92	0·55	52	49·99	14·33	2	1·91	0·58	52	49·73	15·20
3	2·88	0·83	53	50·95	14·61	3	2·87	0·88	53	50·68	15·50
4	3·84	1·10	54	51·91	14·88	4	3·83	1·17	54	51·64	15·79
5	4·81	1·38	55	52·87	15·16	5	4·78	1·46	55	52·60	16·08
6	5·77	1·65	56	53·83	15·44	6	5·74	1·75	56	53·55	16·37
7	6·73	1·93	57	54·79	15·71	7	6·69	2·05	57	54·51	16·67
8	7·69	2·21	58	55·75	15·99	8	7·65	2·34	58	55·47	16·96
9	8·65	2·48	59	56·71	16·26	9	8·61	2·63	59	56·42	17·25
10	9·61	2·76	60	57·68	16·54	10	9·56	2·92	60	57·38	17·54
11	10·57	3·03	61	58·64	16·81	11	10·52	3·22	61	58·33	17·83
12	11·54	3·31	62	59·60	17·09	12	11·48	3·51	62	59·29	18·13
13	12·50	3·58	63	60·56	17·37	13	12·43	3·80	63	60·25	18·42
14	13·46	3·86	64	61·52	17·64	14	13·39	4·09	64	61·20	18·71
15	14·42	4·13	65	62·48	17·92	15	14·34	4·39	65	62·16	19·00
16	15·38	4·41	66	63·44	18·19	16	15·30	4·68	66	63·12	19·30
17	16·34	4·69	67	64·40	18·47	17	16·26	4·97	67	64·07	19·59
18	17·30	4·96	68	65·37	18·74	18	17·21	5·26	68	65·03	19·88
19	18·26	5·24	69	66·33	19·02	19	18·17	5·55	69	65·98	20·17
20	19·23	5·51	70	67·29	19·29	20	19·13	5·85	70	66·94	20·47
21	20·19	5·79	71	68·25	19·57	21	20·08	6·14	71	67·90	20·76
22	21·15	6·06	72	69·21	19·85	22	21·04	6·43	72	68·85	21·05
23	22·11	6·34	73	70·17	20·12	23	21·99	6·72	73	69·81	21·34
24	23·07	6·62	74	71·13	20·40	24	22·95	7·02	74	70·77	21·64
25	24·03	6·89	75	72·09	20·67	25	23·91	7·31	75	71·72	21·93
26	24·99	7·17	76	73·06	20·95	26	24·86	7·60	76	72·68	22·22
27	25·95	7·44	77	74·02	21·22	27	25·82	7·89	77	73·64	22·51
28	26·92	7·72	78	74·98	21·50	28	26·78	8·19	78	74·59	22·80
29	27·88	7·99	79	75·94	21·78	29	27·73	8·48	79	75·55	23·10
30	28·84	8·27	80	76·90	22·05	30	28·69	8·77	80	76·50	23·39
31	29·80	8·54	81	77·86	22·33	31	29·65	9·06	81	77·46	23·68
32	30·76	8·82	82	78·82	22·60	32	30·60	9·36	82	78·42	23·97
33	31·72	9·10	83	79·78	22·88	33	31·56	9·65	83	79·37	24·27
34	32·68	9·37	84	80·75	23·15	34	32·51	9·94	84	80·33	24·56
35	33·64	9·65	85	81·71	23·43	35	33·47	10·23	85	81·29	24·85
36	34·61	9·92	86	82·67	23·70	36	34·43	10·53	86	82·24	25·14
37	35·57	10·20	87	83·63	23·98	37	35·38	10·82	87	83·20	25·44
38	36·53	10·47	88	84·59	24·26	38	36·34	11·11	88	84·15	25·73
39	37·49	10·75	89	85·55	24·53	39	37·30	11·40	89	85·11	26·02
40	38·45	11·03	90	86·51	24·81	40	38·25	11·69	90	86·07	26·31
41	39·41	11·30	91	87·47	25·08	41	39·21	11·99	91	87·02	26·61
42	40·37	11·58	92	88·44	25·36	42	40·16	12·28	92	87·98	26·90
43	41·33	11·85	93	89·40	25·63	43	41·12	12·57	93	88·94	27·19
44	42·30	12·13	94	90·36	25·91	44	42·08	12·86	94	89·89	27·48
45	43·26	12·40	95	91·32	26·19	45	43·03	13·16	95	90·85	27·78
46	44·22	12·68	96	92·28	26·46	46	43·99	13·45	96	91·81	28·07
47	45·18	12·96	97	93·24	26·74	47	44·95	13·74	97	92·76	28·36
48	46·14	13·23	98	94·20	27·01	48	45·90	14·03	98	93·72	28·65
49	47·10	13·51	99	95·16	27·29	49	46·86	14·33	99	94·67	28·94
50	48·06	13·78	100	96·13	27·56	50	47·82	14·62	100	95·63	29·24
	E. or W. Distance.	N. or S. Distance.		E. or W. Distance.	N. or S. Distance.		E. or W. Distance.	N. or S. Distance.		E. or W. Distance.	N. or S. Distance.
	74°						73°				

	18°			19°	
Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.
1	0.95	0.31	51	48.50	15.76
2	1.90	0.62	52	49.45	16.07
3	2.85	0.93	53	50.41	16.38
4	3.80	1.24	54	51.36	16.69
5	4.76	1.55	55	52.31	17.00
6	5.71	1.85	56	53.26	17.30
7	6.66	2.16	57	54.21	17.61
8	7.61	2.47	58	55.16	17.92
9	8.56	2.78	59	56.11	18.23
10	9.51	3.09	60	57.06	18.54
11	10.46	3.40	61	58.01	18.85
12	11.41	3.71	62	58.97	19.16
13	12.36	4.02	63	59.92	19.47
14	13.31	4.33	64	60.87	19.78
15	14.27	4.64	65	61.82	20.09
16	15.22	4.94	66	62.77	20.40
17	16.17	5.25	67	63.72	20.70
18	17.12	5.56	68	64.67	21.01
19	18.07	5.87	69	65.62	21.32
20	19.02	6.18	70	66.57	21.63
21	19.97	6.49	71	67.53	21.94
22	20.92	6.80	72	68.48	22.25
23	21.87	7.11	73	69.43	22.56
24	22.83	7.42	74	70.38	22.87
25	23.78	7.73	75	71.33	23.18
26	24.73	8.03	76	72.28	23.49
27	25.68	8.34	77	73.23	23.79
28	26.63	8.65	78	74.18	24.10
29	27.58	8.96	79	75.13	24.41
30	28.53	9.27	80	76.08	24.72
31	29.48	9.58	81	77.04	25.03
32	30.43	9.89	82	77.99	25.34
33	31.38	10.20	83	78.94	25.65
34	32.34	10.51	84	79.89	25.96
35	33.29	10.82	85	80.84	26.27
36	34.24	11.12	86	81.79	26.58
37	35.19	11.43	87	82.74	26.88
38	36.14	11.74	88	83.69	27.19
39	37.09	12.05	89	84.64	27.50
40	38.04	12.36	90	85.60	27.81
41	38.99	12.67	91	86.55	28.12
42	39.94	12.98	92	87.50	28.43
43	40.90	13.29	93	88.45	28.74
44	41.85	13.60	94	89.40	29.05
45	42.80	13.91	95	90.36	29.36
46	43.75	14.21	96	91.30	29.67
47	44.70	14.52	97	92.25	29.97
48	45.65	14.83	98	93.20	30.28
49	46.60	15.14	99	94.15	30.59
50	47.55	15.45	100	95.10	30.90
	E. or W.	N. or S.		E. or W.	N. or S.
	72°			71°	

	19°				
Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.
1	0.95	0.33	51	48.22	16.60
2	1.89	0.65	52	49.17	16.93
3	2.84	0.98	53	50.11	17.26
4	3.78	1.30	54	51.06	17.58
5	4.73	1.63	55	52.00	17.91
6	5.67	1.95	56	52.95	18.23
7	6.62	2.28	57	53.89	18.56
8	7.56	2.60	58	54.84	18.88
9	8.51	2.93	59	55.79	19.21
10	9.46	3.26	60	56.73	19.53
11	10.40	3.58	61	57.68	19.86
12	11.35	3.91	62	58.62	20.19
13	12.29	4.23	63	59.57	20.51
14	13.24	4.56	64	60.51	20.84
15	14.18	4.88	65	61.46	21.16
16	15.13	5.21	66	62.40	21.49
17	16.07	5.53	67	63.35	21.81
18	17.02	5.86	68	64.30	22.14
19	17.96	6.19	69	65.24	22.46
20	18.91	6.51	70	66.19	22.79
21	19.86	6.84	71	67.13	23.12
22	20.80	7.16	72	68.08	23.44
23	21.75	7.49	73	69.02	23.77
24	22.69	7.81	74	69.97	24.09
25	23.64	8.14	75	70.91	24.42
26	24.58	8.46	76	71.86	24.74
27	25.53	8.79	77	72.81	25.07
28	26.47	9.12	78	73.75	25.39
29	27.42	9.44	79	74.70	25.72
30	28.37	9.77	80	75.64	26.05
31	29.31	10.09	81	76.59	26.37
32	30.26	10.42	82	77.53	26.70
33	31.20	10.74	83	78.48	27.02
34	32.15	11.07	84	79.42	27.35
35	33.09	11.39	85	80.37	27.67
36	34.04	11.72	86	81.31	28.00
37	34.98	12.05	87	82.26	28.32
38	35.93	12.37	88	83.21	28.65
39	36.87	12.70	89	84.15	28.98
40	37.82	13.02	90	85.10	29.30
41	38.77	13.35	91	86.04	29.63
42	39.71	13.67	92	86.99	29.95
43	40.66	14.00	93	87.93	30.28
44	41.60	14.32	94	88.88	30.60
45	42.55	14.65	95	89.82	30.93
46	43.49	14.98	96	90.77	31.25
47	44.44	15.30	97	91.72	31.58
48	45.38	15.63	98	92.66	31.91
49	46.33	15.95	99	93.61	32.23
50	47.28	16.28	100	94.55	32.56

Bearing Length	N. or S. Distance	E. or W. Distance	Bearing Length	N. or S. Distance	E. or W. Distance	Bearing Length	N. or S. Distance	E. or W. Distance	Bearing Length	N. or S. Distance	E. or W. Distance
	20°						**21°**				
1	0·94	0·34	51	47·92	17·44	1	0·93	0·36	51	47·61	18·28
2	1·88	0·68	52	48·86	17·79	2	1·87	0·72	52	48·55	18·63
3	2·82	1·03	53	49·80	18·13	3	2·80	1·08	53	49·48	18·99
4	3·76	1·37	54	50·74	18·47	4	3·73	1·43	54	50·41	19·35
5	4·70	1·71	55	51·68	18·81	5	4·67	1·79	55	51·35	19·71
6	5·64	2·05	56	52·62	19·15	6	5·60	2·15	56	52·28	20·07
7	6·58	2·39	57	53·56	19·50	7	6·53	2·51	57	53·21	20·43
8	7·52	2·74	58	54·50	19·84	8	7·47	2·87	58	54·15	20·78
9	8·46	3·08	59	55·44	20·18	9	8·40	3·23	59	55·08	21·14
10	9·40	3·42	60	56·38	20·52	10	9·34	3·59	60	56·01	21·50
11	10·34	3·76	61	57·32	20·86	11	10·27	3·94	61	56·95	21·86
12	11·28	4·10	62	58·26	21·21	12	11·20	4·30	62	57·88	22·22
13	12·22	4·45	63	59·20	21·55	13	12·14	4·66	63	58·82	22·58
14	13·16	4·79	64	60·14	21·89	14	13·07	5·02	64	59·75	22·93
15	14·10	5·13	65	61·08	22·23	15	14·00	5·38	65	60·68	23·29
16	15·04	5·47	66	62·02	22·57	16	14·94	5·73	66	61·62	23·65
17	15·97	5·81	67	62·96	22·92	17	15·87	6·09	67	62·55	24·01
18	16·91	6·16	68	63·90	23·26	18	16·80	6·45	68	63·48	24·37
19	17·85	6·50	69	64·84	23·60	19	17·74	6·81	69	64·42	24·73
20	18·79	6·84	70	65·78	23·94	20	18·67	7·17	70	65·35	25·08
21	19·73	7·18	71	66·72	24·28	21	19·61	7·53	71	66·28	25·44
22	20·67	7·52	72	67·66	24·63	22	20·54	7·89	72	67·22	25·80
23	21·61	7·87	73	68·60	24·97	23	21·47	8·24	73	68·15	26·16
24	22·55	8·21	74	69·54	25·31	24	22·41	8·60	74	69·08	26·52
25	23·49	8·55	75	70·48	25·65	25	23·34	8·96	75	70·02	26·88
26	24·43	8·89	76	71·42	25·99	26	24·27	9·32	76	70·95	27·23
27	25·37	9·23	77	72·36	26·34	27	25·21	9·68	77	71·89	27·59
28	26·31	9·58	78	73·30	26·68	28	26·14	10·03	78	72·82	27·95
29	27·25	9·92	79	74·24	27·02	29	27·07	10·39	79	73·75	28·31
30	28·19	10·26	80	75·18	27·36	30	28·01	10·75	80	74·68	28·67
31	29·13	10·60	81	76·12	27·70	31	28·94	11·11	81	75·62	29·03
32	30·07	10·94	82	77·06	28·05	32	29·87	11·47	82	76·55	29·39
33	31·01	11·29	83	77·99	28·39	33	30·81	11·83	83	77·49	29·74
34	31·95	11·63	84	78·93	28·73	34	31·74	12·18	84	78·42	30·10
35	32·89	11·97	85	79·87	29·07	35	32·68	12·54	85	79·35	30·46
36	33·83	12·31	86	80·81	29·41	36	33·61	12·90	86	80·29	30·82
37	34·77	12·65	87	81·75	29·76	37	34·54	13·26	87	81·22	31·18
38	35·71	13·00	88	82·69	30·10	38	35·48	13·62	88	82·16	31·54
39	36·65	13·34	89	83·63	30·44	39	36·41	13·98	89	83·09	31·89
40	37·59	13·68	90	84·57	30·78	40	37·34	14·33	90	84·02	32·25
41	38·53	14·02	91	85·51	31·12	41	38·28	14·69	91	84·96	32·61
42	39·47	14·36	92	86·45	31·47	42	39·21	15·05	92	85·89	32·97
43	40·41	14·71	93	87·39	31·81	43	40·14	15·41	93	86·82	33·33
44	41·35	15·05	94	88·33	32·15	44	41·08	15·77	94	87·76	33·69
45	42·29	15·39	95	89·27	32·49	45	42·01	16·13	95	88·69	34·04
46	43·23	15·73	96	90·21	32·83	46	42·94	16·48	96	89·62	34·40
47	44·17	16·07	97	91·15	33·18	47	43·88	16·84	97	90·56	34·76
48	45·11	16·42	98	92·09	33·52	48	44·81	17·20	98	91·49	35·12
49	46·05	16·76	99	93·03	33·86	49	45·75	17·56	99	92·42	35·48
50	46·98	17·10	100	94·20	34·20	50	46·68	17·92	100	93·35	35·84
	E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.
	70°						**69°**				

H

22°

Bearing Lengths	N. or S. Distances	E. or W. Distances	Bearing Lengths	N. or S. Distances	E. or W. Distances
1	0·93	0·37	51	47·29	19·10
2	1·85	0·75	52	48·21	19·48
3	2·78	1·12	53	49·14	19·85
4	3·71	1·50	54	50·07	20·23
5	4·64	1·87	55	51·00	20·60
6	5·56	2·25	56	51·92	20·98
7	6·49	2·63	57	52·85	21·35
8	7·42	3·00	58	53·78	21·73
9	8·34	3·37	59	54·70	22·10
10	9·27	3·75	60	55·63	22·48
11	10·20	4·12	61	56·56	22·85
12	11·13	4·50	62	57·49	23·23
13	12·05	4·87	63	58·41	23·60
14	12·98	5·24	64	59·34	23·97
15	13·91	5·62	65	60·27	24·35
16	14·83	5·99	66	61·19	24·72
17	15·76	6·37	67	62·12	25·10
18	16·69	6·74	68	63·05	25·47
19	17·62	7·12	69	63·98	25·85
20	18·54	7·49	70	64·90	26·22
21	19·47	7·87	71	65·83	26·60
22	20·40	8·24	72	66·76	26·97
23	21·33	8·62	73	67·68	27·35
24	22·25	8·99	74	68·61	27·72
25	23·18	9·37	75	69·54	28·10
26	24·11	9·74	76	70·47	28·47
27	25·03	10·11	77	71·39	28·84
28	25·96	10·49	78	72·32	29·22
29	26·89	10·86	79	73·25	29·59
30	27·82	11·24	80	74·17	29·97
31	28·74	11·61	81	75·10	30·34
32	29·67	11·99	82	76·03	30·72
33	30·60	12·36	83	76·96	31·09
34	31·52	12·74	84	77·88	31·47
35	32·45	13·11	85	78·81	31·84
36	33·38	13·49	86	79·74	32·22
37	34·31	13·86	87	80·66	32·59
38	35·23	14·24	88	81·59	32·97
39	36·16	14·61	89	82·52	33·34
40	37·09	14·98	90	83·45	33·71
41	38·01	15·36	91	84·37	34·09
42	38·94	15·73	92	85·30	34·46
43	39·87	16·11	93	86·23	34·84
44	40·80	16·48	94	87·16	35·21
45	41·72	16·86	95	88·08	35·59
46	42·65	17·23	96	89·01	35·96
47	43·58	17·61	97	89·94	36·34
48	44·50	17·98	98	90·81	36·71
49	45·43	18·36	99	91·79	37·09
50	46·36	18·73	100	92·72	37·46
	E. or W.	N. or S.		E. or W.	N. or S.

68°

23°

Bearing Lengths	N. or S. Distances	E. or W. Distances	Bearing Lengths	N. or S. Distances	E. or W. Distances
1	0·92	0·39	51	46·95	19·92
2	1·84	0·78	52	47·87	20·32
3	2·76	1·17	53	48·79	20·72
4	3·68	1·56	54	49·71	21·10
5	4·60	1·95	55	50·63	21·49
6	5·52	2·34	56	51·55	21·89
7	6·44	2·74	57	52·47	22·27
8	7·36	3·13	58	53·39	22·66
9	8·28	3·52	59	54·31	23·05
10	9·21	3·91	60	55·23	23·44
11	10·13	4·30	61	56·15	23·88
12	11·05	4·69	62	57·07	24·23
13	11·97	5·08	63	57·99	24·62
14	12·89	5·47	64	58·91	25·01
15	13·81	5·86	65	59·83	25·40
16	14·73	6·25	66	60·75	25·79
17	15·65	6·64	67	61·67	26·18
18	16·57	7·03	68	62·59	26·57
19	17·49	7·42	69	63·51	26·96
20	18·41	7·81	70	64·44	27·35
21	19·33	8·21	71	65·36	27·74
22	20·25	8·60	72	66·28	28·13
23	21·17	8·99	73	67·20	28·52
24	22·09	9·38	74	68·12	28·91
25	23·01	9·77	75	69·04	29·30
26	23·93	10·16	76	69·96	29·70
27	24·85	10·55	77	70·88	30·09
28	25·77	10·94	78	71·80	30·48
29	26·69	11·33	79	72·72	30·87
30	27·62	11·72	80	73·64	31·26
31	28·54	12·11	81	74·56	31·65
32	29·46	12·50	82	75·48	32·04
33	30·38	12·89	83	76·40	32·43
34	31·30	13·28	84	77·32	32·82
35	32·22	13·68	85	78·24	33·21
36	33·14	14·07	86	79·16	33·60
37	34·06	14·46	87	80·08	33·99
38	34·98	14·85	88	81·00	34·38
39	35·90	15·24	89	81·92	34·78
40	36·82	15·63	90	82·85	35·17
41	37·74	16·03	91	83·77	35·56
42	38·66	16·41	92	84·69	35·95
43	39·58	16·80	93	85·61	36·34
44	40·50	17·19	94	86·53	36·73
45	41·42	17·58	95	87·45	37·12
46	42·34	17·97	96	88·37	37·51
47	43·26	18·36	97	89·29	37·90
48	44·18	18·76	98	90·21	38·29
49	45·10	19·15	99	91·13	38·68
50	46·02	19·54	100	92·05	39·07
	E. or W.	N. or S.		E. or W.	N. or S.

67°

24°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·91	0·41	51	46·59	20·74
2	1·83	0·81	52	47·50	21·15
3	2·74	1·22	53	48·42	21·56
4	3·65	1·63	54	49·33	21·96
5	4·57	2·03	55	50·25	22·37
6	5·48	2·44	56	51·16	22·78
7	6·39	2·85	57	52·07	23·18
8	7·31	3·25	58	52·99	23·59
9	8·22	3·66	59	53·90	24·00
10	9·14	4·07	60	54·81	24·40
11	10·05	4·47	61	55·73	24·81
12	10·96	4·88	62	56·64	25·22
13	11·88	5·29	63	57·55	25·63
14	12·79	5·69	64	58·47	26·03
15	13·70	6·10	65	59·38	26·44
16	14·62	6·51	66	60·29	26·84
17	15·53	6·91	67	61·21	27·25
18	16·44	7·32	68	62·12	27·66
19	17·36	7·73	69	63·03	28·06
20	18·27	8·13	70	63·95	28·47
21	19·18	8·54	71	64·86	28·88
22	20·10	8·95	72	65·77	29·28
23	21·01	9·35	73	66·69	29·69
24	21·93	9·76	74	67·60	30·10
25	22·84	10·17	75	68·52	30·50
26	23·75	10·58	76	69·43	30·91
27	24·67	10·98	77	70·34	31·32
28	25·58	11·39	78	71·25	31·72
29	26·49	11·80	79	72·17	32·13
30	27·41	12·20	80	73·08	32·54
31	28·32	12·61	81	74·00	32·94
32	29·23	13·02	82	74·91	33·35
33	30·15	13·42	83	75·82	33·76
34	31·06	13·83	84	76·74	34·16
35	31·97	14·24	85	77·65	34·57
36	32·89	14·64	86	78·56	34·98
37	33·80	15·05	87	79·48	35·38
38	34·71	15·46	88	80·39	35·79
39	35·63	15·86	89	81·31	36·20
40	36·54	16·27	90	82·22	36·60
41	37·46	16·68	91	83·13	37·01
42	38·37	17·08	92	84·05	37·42
43	39·28	17·49	93	84·96	37·82
44	40·20	17·90	94	85·87	38·23
45	41·11	18·30	95	86·79	38·64
46	42·02	18·71	96	87·70	39·04
47	42·94	19·12	97	88·61	39·45
48	43·85	19·52	98	89·53	39·85
49	44·76	19·93	99	90·44	40·26
50	45·68	20·34	100	91·35	40·67
	E. or W.	N. or S.		E. or W.	N. or S.

66°

25°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·91	0·42	51	46·22	21·55
2	1·81	0·85	52	47·13	21·98
3	2·72	1·27	53	48·04	22·40
4	3·63	1·69	54	48·94	22·82
5	4·53	2·11	55	49·85	23·24
6	5·44	2·54	56	50·75	23·67
7	6·34	2·96	57	51·66	24·09
8	7·25	3·38	58	52·57	24·51
9	8·16	3·80	59	53·47	24·93
10	9·06	4·23	60	54·38	25·36
11	9·97	4·65	61	55·28	25·78
12	10·88	5·07	62	56·19	26·20
13	11·78	5·49	63	57·10	26·62
14	12·69	5·92	64	58·00	27·05
15	13·59	6·34	65	58·91	27·47
16	14·50	6·76	66	59·82	27·89
17	15·41	7·18	67	60·72	28·32
18	16·31	7·61	68	61·63	28·74
19	17·22	8·03	69	62·54	29·16
20	18·13	8·45	70	63·44	29·60
21	19·03	8·87	71	64·35	30·01
22	19·94	9·30	72	65·25	30·43
23	20·85	9·72	73	66·16	30·85
24	21·75	10·14	74	67·07	31·27
25	22·66	10·57	75	67·97	31·70
26	23·56	10·99	76	68·88	32·12
27	24·47	11·41	77	69·79	32·54
28	25·38	11·83	78	70·69	32·96
29	26·28	12·26	79	71·60	33·39
30	27·19	12·68	80	72·50	33·81
31	28·10	13·10	81	73·41	34·23
32	29·00	13·52	82	74·32	34·65
33	29·91	13·95	83	75·22	35·08
34	30·82	14·37	84	76·13	35·50
35	31·72	14·79	85	77·04	35·92
36	32·63	15·21	86	77·94	36·35
37	33·54	15·63	87	78·85	36·77
38	34·44	16·06	88	79·76	37·19
39	35·35	16·48	89	80·66	37·61
40	36·25	16·90	90	81·57	38·04
41	37·16	17·33	91	82·47	38·46
42	38·06	17·75	92	83·38	38·88
43	38·97	18·17	93	84·29	39·30
44	39·88	18·60	94	85·19	39·73
45	40·78	19·02	95	86·10	40·15
46	41·69	19·44	96	87·01	40·57
47	42·60	19·86	97	87·91	40·99
48	43·50	20·29	98	88·82	41·42
49	44·41	20·71	99	89·73	41·84
50	45·31	21·13	100	90·63	42·26
	E. or W.	N. or S.		E. or W.	N. or S.

65°

26°

Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.
1	0·90	0·44	51	45·84	22·36
2	1·80	0·88	52	46·74	22·80
3	2·70	1·32	53	47·64	23·23
4	3·60	1·75	54	48·53	23·67
5	4·49	2·19	55	49·43	24·11
6	5·39	2·63	56	50·23	24·55
7	6·29	3·07	57	51·33	24·99
8	7·19	3·50	58	52·13	25·43
9	8·09	3·95	59	53·03	25·86
10	8·99	4·38	60	53·93	26·30
11	9·89	4·82	61	54·83	26·74
12	10·79	5·26	62	55·73	27·18
13	11·68	5·70	63	56·62	27·62
14	12·58	6·14	64	57·52	28·06
15	13·48	6·58	65	58·42	28·49
16	14·38	7·01	66	59·32	28·93
17	15·28	7·45	67	60·22	29·37
18	16·18	7·89	68	61·12	29·81
19	17·08	8·33	69	62·02	30·25
20	17·98	8·77	70	62·92	30·69
21	18·87	9·21	71	63·81	31·12
22	19·77	9·64	72	64·71	31·56
23	20·67	10·08	73	65·61	32·00
24	21·57	10·52	74	66·51	32·44
25	22·47	10·96	75	67·41	32·88
26	23·37	11·40	76	68·31	33·32
27	24·27	11·84	77	69·21	33·75
28	25·17	12·27	78	70·11	34·19
29	26·06	12·71	79	71·00	34·63
30	26·96	13·15	80	71·90	35·07
31	27·86	13·59	81	72·80	35·51
32	28·76	14·03	82	73·70	35·95
33	29·66	14·47	83	74·60	36·38
34	30·56	14·90	84	75·50	36·82
35	31·46	15·34	85	76·40	37·26
36	32·36	15·78	86	77·30	37·70
37	33·26	16·22	87	78·19	38·14
38	34·15	16·66	88	79·09	38·58
39	35·05	17·10	89	79·99	39·02
40	35·95	17·53	90	80·89	39·45
41	36·85	17·97	91	81·79	39·89
42	37·75	18·41	92	82·69	40·33
43	38·65	18·85	93	83·59	40·77
44	39·55	19·29	94	84·49	41·21
45	40·45	19·73	95	85·39	41·65
46	41·34	20·17	96	86·28	42·08
47	42·24	20·60	97	87·18	42·52
48	43·14	21·04	98	88·08	42·96
49	44·04	21·48	99	88·98	43·40
50	44·94	21·92	100	89·88	43·84
	E. or W.	N. or S.		E. or W.	N. or S.

64°

27°

Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.
1	0·89	0·45	51	45·44	23·15
2	1·78	0·91	52	46·33	23·61
3	2·67	1·36	53	47·22	24·06
4	3·56	1·82	54	48·11	24·52
5	4·46	2·27	55	49·01	24·97
6	5·35	2·72	56	49·90	25·42
7	6·24	3·18	57	50·79	25·88
8	7·13	3·63	58	51·68	26·33
9	8·02	4·09	59	52·57	26·79
10	8·91	4·54	60	53·46	27·24
11	9·80	4·99	61	54·35	27·69
12	10·69	5·45	62	55·24	28·15
13	11·58	5·90	63	56·13	28·60
14	12·47	6·36	64	57·02	29·06
15	13·37	6·81	65	57·92	29·51
16	14·26	7·26	66	58·81	29·96
17	15·15	7·72	67	59·70	30·42
18	16·04	8·17	68	60·59	30·87
19	16·93	8·63	69	61·48	31·33
20	17·82	9·08	70	62·37	31·78
21	18·71	9·53	71	63·26	32·23
22	19·60	9·99	72	64·15	32·69
23	20·49	10·44	73	65·04	33·14
24	21·38	10·90	74	65·93	33·60
25	22·28	11·35	75	66·83	34·05
26	23·17	11·80	76	67·72	34·50
27	24·06	12·26	77	68·61	34·96
28	24·95	12·71	78	69·50	35·41
29	25·84	13·17	79	70·39	35·87
30	26·73	13·62	80	71·28	36·32
31	27·63	14·07	81	72·17	36·77
32	28·51	14·53	82	73·06	37·23
33	29·40	14·98	83	73·95	37·68
34	30·29	15·44	84	74·84	38·14
35	31·19	15·89	85	75·74	38·59
36	32·08	16·34	86	76·63	39·04
37	32·97	16·80	87	77·52	39·50
38	33·86	17·25	88	78·41	39·95
39	34·75	17·71	89	79·30	40·41
40	35·64	18·16	90	80·19	40·86
41	36·53	18·61	91	81·08	41·31
42	37·42	19·07	92	81·97	41·77
43	38·31	19·52	93	82·86	42·23
44	39·20	19·98	94	83·75	42·68
45	40·10	20·43	95	84·65	43·13
46	40·99	20·88	96	85·54	43·58
47	41·88	21·34	97	86·43	44·04
48	42·77	21·79	98	87·32	44·49
49	43·66	22·25	99	88·21	44·95
50	44·55	22·70	100	89·10	45·40
	E. or W.	N. or S.		E. or W.	N. or S.

63°

28°

Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.
1	0·88	0·47	51	45·03	23·94
2	1·77	0·94	52	45·91	24·41
3	2·65	1·41	53	46·80	24·88
4	3·53	1·88	54	47·68	25·35
5	4·41	2·35	55	48·56	25·82
6	5·30	2·82	56	49·45	26·29
7	6·18	3·29	57	50·33	26·76
8	7·06	3·76	58	51·21	27·23
9	7·95	4·23	59	52·09	27·70
10	8·83	4·69	60	52·98	28·17
11	9·71	5·16	61	53·86	28·64
12	10·60	5·63	62	54·76	29·11
13	11·48	6·10	63	55·63	29·58
14	12·36	6·57	64	56·51	30·05
15	13·24	7·04	65	57·39	30·52
16	14·13	7·51	66	58·27	30·99
17	15·01	7·98	67	59·16	31·45
18	15·89	8·45	68	60·04	31·92
19	16·78	8·92	69	60·92	32·39
20	17·66	9·39	70	61·81	32·86
21	18·54	9·86	71	62·69	33·33
22	19·42	10·33	72	63·57	33·80
23	20·31	10·80	73	64·46	34·27
24	21·19	11·27	74	65·34	34·74
25	22·07	11·74	75	66·22	35·21
26	22·96	12·21	76	67·10	35·68
27	23·84	12·68	77	67·99	36·15
28	24·72	13·15	78	68·87	36·62
29	25·61	13·61	79	69·75	37·09
30	26·49	14·08	80	70·64	37·56
31	27·37	14·55	81	71·52	38·03
32	28·25	15·02	82	72·40	38·50
33	29·14	15·49	83	73·28	38·97
34	30·02	15·96	84	74·17	39·44
35	30·90	16·43	85	75·05	39·91
36	31·79	16·90	86	75·93	40·37
37	32·67	17·37	87	76·82	40·84
38	33·55	17·84	88	77·70	41·31
39	34·43	18·31	89	78·58	41·78
40	35·32	18·78	90	79·47	42·25
41	36·20	19·25	91	80·35	42·72
42	37·08	19·72	92	81·23	43·19
43	37·97	20·19	93	82·11	43·66
44	38·85	20·66	94	83·00	44·13
45	39·73	21·13	95	83·88	44·60
46	40·62	21·60	96	84·76	45·07
47	41·50	22·07	97	85·65	45·54
48	42·38	22·53	98	86·53	46·01
49	43·26	23·00	99	87·41	46·48
50	44·15	23·47	100	88·29	46·95
	E. or W.	N. or S.		E. or W.	N. or S.

62°

29°

Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.
1	0·87	0·48	51	44·61	24·73
2	1·75	0·97	52	45·48	25·21
3	2·62	1·45	53	46·36	25·69
4	3·50	1·94	54	47·23	26·18
5	4·37	2·42	55	48·10	26·66
6	5·25	2·91	56	48·98	27·15
7	6·12	3·39	57	49·85	27·63
8	7·00	3·88	58	50·73	28·12
9	7·87	4·36	59	51·60	28·60
10	8·75	4·85	60	52·48	29·09
11	9·62	5·33	61	53·35	29·57
12	10·50	5·82	62	54·23	30·06
13	11·37	6·30	63	55·10	30·54
14	12·24	6·79	64	55·98	31·03
15	13·12	7·27	65	56·85	31·51
16	13·99	7·76	66	57·72	32·00
17	14·87	8·24	67	58·60	32·48
18	15·74	8·73	68	59·47	32·97
19	16·62	9·21	69	60·35	33·45
20	17·49	9·70	70	61·22	33·94
21	18·37	10·18	71	62·10	34·42
22	19·24	10·67	72	62·97	34·91
23	20·12	11·15	73	63·85	35·39
24	20·99	11·64	74	64·72	35·88
25	21·87	12·12	75	65·60	36·36
26	22·74	12·61	76	66·47	36·85
27	23·61	13·09	77	67·35	37·33
28	24·49	13·57	78	68·22	37·82
29	25·36	14·06	79	69·09	38·30
30	26·24	14·54	80	69·97	38·78
31	27·11	15·03	81	70·84	39·27
32	27·99	15·51	82	71·72	39·75
33	28·86	16·00	83	72·59	40·24
34	29·74	16·48	84	73·47	40·72
35	30·61	16·97	85	74·34	41·21
36	31·49	17·45	86	75·22	41·69
37	32·36	17·94	87	76·09	42·18
38	33·23	18·42	88	76·97	42·66
39	34·11	18·91	89	77·84	43·15
40	34·98	19·39	90	78·72	43·63
41	35·86	19·88	91	79·59	44·12
42	36·73	20·36	92	80·47	44·60
43	37·61	20·85	93	81·34	45·02
44	38·48	21·33	94	82·21	45·57
45	39·36	21·82	95	83·09	46·06
46	40·24	22·30	96	83·96	46·54
47	41·11	22·79	97	84·84	47·03
48	41·98	23·27	98	85·71	47·51
49	42·86	23·76	99	86·59	48·00
50	43·73	24·24	100	87·46	48·48
E. or W.	N. or S.		E. or W.	N. or S.	

61°

30°						31°					
Bearing Lengths.	N. or S. Distances.	E. or W. Distances.	Bearing Lengths.	N. or S. Distances.	E. or W. Distances.	Bearing Lengths.	N. or S. Distances.	E. or W. Distances.	Bearing Lengths.	N. or S. Distances.	E. or W. Distances.
1	0·87	0·50	51	44·17	25·50	1	0·86	0·52	51	43·72	26·27
2	1·73	1·00	52	45·03	26·00	2	1·71	1·03	52	44·57	26·78
3	2·60	1·50	53	45·90	26·50	3	2·57	1·55	53	45·43	27·81
4	3·46	2·00	54	46·77	27·00	4	3·43	2·06	54	46·29	27·81
5	4·33	2·50	55	47·63	27·50	5	4·29	2·58	55	47·14	28·33
6	5·20	3·00	56	48·50	28·00	6	5·14	3·09	56	48·00	28·84
7	6·06	3·50	57	49·36	28·50	7	6·00	3·61	57	48·86	29·36
8	6·93	4·00	58	50·23	29·00	8	6·86	4·12	58	49·72	29·87
9	7·79	4·50	59	51·10	29·50	9	7·71	4·64	59	50·57	30·39
10	8·66	5·00	60	51·96	30·00	10	8·57	5·15	60	51·43	30·90
11	9·53	5·50	61	52·83	30·50	11	9·43	5·67	61	52·29	31·42
12	10·39	6·00	62	53·69	31·00	12	10·29	6·18	62	53·14	31·93
13	11·26	6·50	63	54·56	31·50	13	11·14	6·70	63	54·00	32·45
14	12·12	7·00	64	55·43	32·00	14	12·00	7·21	64	54·86	32·96
15	12·99	7·50	65	56·29	32·50	15	12·86	7·73	65	55·72	33·48
16	13·86	8·00	66	57·16	33·00	16	13·71	8·24	66	56·57	33·99
17	14·72	8·50	67	58·02	33·50	17	14·57	8·76	67	57·43	34·51
18	15·59	9·00	68	58·89	34·00	18	15·43	9·27	68	58·29	35·02
19	16·45	9·50	69	59·76	34·50	19	16·29	9·79	69	59·14	35·54
20	17·32	10·00	70	60·62	35·00	20	17·14	10·30	70	60·00	36·05
21	18·19	10·50	71	61·49	35·50	21	18·00	10·82	71	60·86	36·57
22	19·05	11·00	72	62·35	36·00	22	18·86	11·33	72	61·72	37·08
23	19·92	11·50	73	63·22	36·50	23	19·71	11·85	73	62·57	37·60
24	20·78	12·00	74	64·08	37·00	24	20·58	12·36	74	63·43	38·11
25	21·65	12·50	75	64·95	37·50	25	21·43	12·88	75	64·29	38·63
26	22·52	13·00	76	65·82	38·00	26	22·29	13·39	76	65·14	39·14
27	23·38	13·50	77	66·68	38·50	27	23·14	13·91	77	66·00	39·66
28	24·25	14·00	78	67·55	39·00	28	24·00	14·42	78	66·86	40·17
29	25·11	14·50	79	68·42	39·50	29	24·86	14·94	79	67·72	40·69
30	25·98	15·00	80	69·28	40·00	30	25·72	15·45	80	68·57	41·20
31	26·85	15·50	81	70·15	40·50	31	26·57	15·97	81	69·43	41·72
32	27·71	16·00	82	71·01	41·00	32	27·43	16·48	82	70·29	42·23
33	28·58	16·50	83	71·88	41·50	33	28·29	17·00	83	71·15	42·75
34	29·44	17·00	84	72·75	42·00	34	29·14	17·51	84	72·00	43·26
35	30·31	17·50	85	73·61	42·50	35	30·00	18·03	85	72·86	43·78
36	31·18	18·00	86	74·48	43·00	36	30·86	18·54	86	73·72	44·29
37	32·04	18·50	87	75·35	43·50	37	31·72	19·06	87	74·57	44·81
38	32·91	19·00	88	76·21	44·00	38	32·57	19·57	88	75·43	45·32
39	33·78	19·50	89	77·08	44·50	39	33·43	20·09	89	76·29	45·84
40	34·64	20·00	90	77·94	45·00	40	34·29	20·60	90	77·15	46·35
41	35·51	20·50	91	78·81	45·50	41	35·14	21·12	91	78·00	46·87
42	36·37	21·00	92	79·68	46·00	42	36·00	21·63	92	78·86	47·38
43	37·24	21·50	93	80·54	46·50	43	36·86	22·15	93	79·72	47·90
44	38·11	22·00	94	81·41	47·00	44	37·72	22·66	94	80·57	48·41
45	38·97	22·50	95	82·27	47·50	45	38·57	23·18	95	81·43	48·93
46	39·84	23·00	96	83·14	48·00	46	39·43	23·69	96	82·29	49·44
47	40·70	23·50	97	84·00	48·50	47	40·29	24·21	97	83·15	49·96
48	41·57	24·00	98	84·87	49·00	48	41·14	24·72	98	84·00	50·47
49	42·44	24·50	99	85·74	49·50	49	42·00	25·24	99	84·86	50·99
50	43·30	25·00	100	86·60	50·00	50	42·86	25·75	100	85·72	51·50
	E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.		E. or W.	N. or S.
		60°						59°			

32°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·85	0·53	51	43·25	27·03
2	1·70	1·06	52	44·10	27·56
3	2·54	1·59	53	44·95	28·09
4	3·39	2·12	54	45·79	28·62
5	4·24	2·65	55	46·64	29·15
6	5·09	3·18	56	47·49	29·68
7	5·94	3·71	57	48·34	30·21
8	6·78	4·23	58	49·19	30·74
9	7·63	4·77	59	50·03	31·27
10	8·48	5·30	60	50·88	31·80
11	9·33	5·83	61	51·73	32·33
12	10·18	6·36	62	52·58	32·86
13	11·02	6·89	63	53·43	33·38
14	11·87	7·42	64	54·28	33·91
15	12·72	7·95	65	55·13	34·44
16	13·57	8·48	66	55·97	34·97
17	14·42	9·01	67	56·82	35·50
18	15·26	9·54	68	57·67	36·03
19	16·11	10·07	69	58·57	36·56
20	16·96	10·60	70	59·36	37·09
21	17·81	11·13	71	60·21	37·62
22	18·66	11·66	72	61·06	38·15
23	19·51	12·19	73	61·91	38·68
24	20·35	12·72	74	62·75	39·21
25	21·20	13·25	75	63·60	39·74
26	22·05	13·78	76	64·45	40·27
27	22·90	14·31	77	65·30	40·80
28	23·75	14·84	78	66·15	41·33
29	24·59	15·37	79	67·00	41·86
30	25·44	15·90	80	67·84	42·39
31	26·29	16·43	81	68·69	42·92
32	27·14	16·96	82	69·54	43·45
33	27·99	17·49	83	70·39	43·98
34	28·83	18·02	84	71·24	44·51
35	29·68	18·55	85	72·08	45·04
36	30·53	19·08	86	72·93	45·57
37	31·38	19·61	87	73·78	46·10
38	32·23	20·14	88	74·63	46·63
39	33·07	20·67	89	75·48	47·16
40	33·92	21·20	90	76·32	47·69
41	34·77	21·73	91	77·17	48·22
42	35·62	22·26	92	78·02	48·75
43	36·47	22·79	93	78·87	49·28
44	37·31	23·32	94	79·72	49·81
45	38·16	23·85	95	80·56	50·34
46	39·01	24·38	96	81·41	50·87
47	39·86	24·91	97	82·26	51·40
48	40·71	25·44	98	83·11	51·93
49	41·55	25·97	99	83·96	52·46
50	42·40	26·50	100	84·81	52·99
	E. or W.	N. or S.		E. or W.	N. or S.

58°

33°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·84	0·54	51	42·77	27·78
2	1·68	1·09	52	43·61	28·32
3	2·52	1·63	53	44·45	28·87
4	3·35	2·18	54	45·29	29·41
5	4·19	2·72	55	46·13	29·96
6	5·03	3·27	56	46·97	30·50
7	5·87	3·81	57	47·80	31·05
8	6·71	4·36	58	48·64	31·59
9	7·55	4·90	59	49·48	32·15
10	8·39	5·45	60	50·32	32·68
11	9·23	5·99	61	51·16	33·22
12	10·06	6·54	62	52·00	33·77
13	10·90	7·08	63	52·84	34·31
14	11·74	7·62	64	53·67	34·86
15	12·58	8·17	65	54·51	35·40
16	13·42	8·71	66	55·35	35·95
17	14·26	9·26	67	56·19	36·49
18	15·10	9·80	68	57·03	37·04
19	15·93	10·35	69	57·87	37·58
20	16·77	10·89	70	58·71	38·13
21	17·61	11·44	71	59·55	38·67
22	18·45	11·98	72	60·38	39·21
23	19·29	12·53	73	61·22	39·76
24	20·13	13·07	74	62·06	40·30
25	20·97	13·62	75	62·90	40·85
26	21·81	14·16	76	63·74	41·39
27	22·64	14·71	77	64·58	41·94
28	23·48	15·25	78	65·42	42·48
29	24·32	15·79	79	66·25	43·03
30	25·16	16·34	80	67·09	43·57
31	26·00	16·88	81	67·93	44·12
32	26·84	17·43	82	68·77	44·66
33	27·68	17·97	83	69·61	45·21
34	28·51	18·52	84	70·45	45·75
35	29·35	19·06	85	71·29	46·29
36	30·19	19·61	86	72·13	46·84
37	31·03	20·15	87	72·96	47·38
38	31·87	20·70	88	73·80	47·93
39	32·71	21·24	89	74·64	48·47
40	33·55	21·79	90	75·48	49·02
41	34·39	22·33	91	76·32	49·56
42	35·22	22·88	92	77·16	50·11
43	36·06	23·42	93	78·00	50·65
44	36·90	23·97	94	78·84	51·20
45	37·74	24·51	95	79·67	51·74
46	38·58	25·05	96	80·51	52·29
47	39·42	25·60	97	81·35	52·83
48	40·26	26·14	98	82·19	53·37
49	41·09	26·69	99	83·03	53·92
50	41·93	27·23	100	83·87	54·46
	E. or W.	N. or S.		E. or W.	N. or S.

57°

34°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·83	0·56	51	42·28	28·52
2	1·66	1·12	52	43·11	29·08
3	2·49	1·68	53	43·94	29·64
4	3·32	2·24	54	44·77	30·20
5	4·15	2·80	55	45·60	30·76
6	4·97	3·36	56	46·43	31·31
7	5·80	3·91	57	47·26	31·87
8	6·63	4·47	58	48·08	32·43
9	7·46	5·03	59	48·91	32·99
10	8·29	5·59	60	49·74	33·55
11	9·12	6·15	61	50·57	34·11
12	9·95	6·71	62	51·40	34·67
13	10·78	7·27	63	52·23	35·23
14	11·61	7·83	64	53·06	35·79
15	12·44	8·39	65	53·89	36·35
16	13·26	8·95	66	54·72	36·91
17	14·09	9·51	67	55·55	37·47
18	14·92	10·07	68	56·37	38·02
19	15·75	10·62	69	57·20	38·58
20	16·58	11·18	70	58·03	39·14
21	17·41	11·74	71	58·86	39·70
22	18·24	12·30	72	59·69	40·26
23	19·07	12·86	73	60·52	40·82
24	19·90	13·42	74	61·35	41·38
25	20·73	13·98	75	62·18	41·94
26	21·56	14·54	76	63·01	42·50
27	22·38	15·10	77	63·84	43·06
28	23·21	15·66	78	64·67	43·62
29	24·04	16·22	79	65·49	44·18
30	24·87	16·78	80	66·32	44·74
31	25·70	17·33	81	67·15	45·29
32	26·53	17·89	82	67·98	45·85
33	27·36	18·45	83	68·81	46·41
34	28·19	19·01	84	69·64	46·97
35	29·02	19·57	85	70·47	47·53
36	29·85	20·13	86	71·30	48·09
37	30·67	20·69	87	72·13	48·65
38	31·50	21·25	88	72·96	49·21
39	32·33	21·81	89	73·78	49·77
40	33·16	22·37	90	74·61	50·33
41	33·99	22·93	91	75·44	50·89
42	34·82	23·49	92	76·27	51·45
43	35·65	24·05	93	77·10	52·00
44	36·48	24·60	94	77·93	52·56
45	37·31	25·16	95	78·76	53·12
46	38·14	25·72	96	79·59	53·68
47	38·96	26·28	97	80·42	54·24
48	39·79	26·84	98	81·25	54·80
49	40·62	27·40	99	82·07	55·36
50	41·45	27·96	100	82·90	55·92
	E. or W.	N. or S.		E. or W.	N. or S.

56°

35°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·82	0·57	51	41·78	29·25
2	1·64	1·15	52	42·59	29·83
3	2·46	1·72	53	43·41	30·40
4	3·28	2·29	54	44·23	30·97
5	4·10	2·87	55	45·05	31·55
6	4·91	3·44	56	45·87	32·12
7	5·73	4·02	57	46·69	32·69
8	6·55	4·59	58	47·51	33·27
9	7·37	5·16	59	48·33	33·84
10	8·19	5·74	60	49·15	34·41
11	9·01	6·31	61	49·97	34·99
12	9·83	6·88	62	50·79	35·56
13	10·65	7·46	63	51·61	36·14
14	11·47	8·03	64	52·43	36·71
15	12·29	8·60	65	53·24	37·28
16	13·11	9·18	66	54·06	37·86
17	13·93	9·75	67	54·88	38·43
18	14·74	10·32	68	55·70	39·00
19	15·56	10·90	69	56·52	39·58
20	16·38	11·47	70	57·34	40·15
21	17·20	12·05	71	58·16	40·72
22	18·02	12·62	72	58·96	41·30
23	18·84	13·19	73	59·80	41·87
24	19·66	13·77	74	60·62	42·44
25	20·48	14·34	75	61·44	43·02
26	21·30	14·91	76	62·26	43·59
27	22·12	15·49	77	63·07	44·17
28	22·94	16·06	78	63·89	44·74
29	23·76	16·63	79	64·71	45·31
30	24·57	17·21	80	65·53	45·89
31	25·39	17·78	81	66·35	46·46
32	26·21	18·35	82	67·17	47·03
33	27·03	18·93	83	67·99	47·61
34	27·85	19·50	84	68·81	48·18
35	28·67	20·08	85	69·63	48·75
36	29·49	20·65	86	70·45	49·33
37	30·31	21·22	87	71·27	49·90
38	31·13	21·80	88	72·09	50·48
39	31·95	22·37	89	72·90	51·05
40	32·77	22·94	90	73·72	51·62
41	33·59	23·52	91	74·54	52·20
42	34·40	24·09	92	75·36	52·77
43	35·22	24·66	93	76·18	53·34
44	36·04	25·24	94	77·00	53·92
45	36·86	25·81	95	77·82	54·49
46	37·68	26·38	96	78·64	55·06
47	38·50	26·96	97	79·46	55·64
48	39·32	27·53	98	80·28	56·21
49	40·14	28·11	99	81·10	56·78
50	40·96	28·68	100	81·92	57·36
	E. or W.	N. or S.		E. or W.	N. or S.

55°

	36°							37°				
Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance		Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·81	0·59	51	41·26	29·98		1	0·80	0·60	51	40·73	30·69
2	1·62	1·18	52	42·07	30·57		2	1·60	1·20	52	41·53	31·29
3	2·43	1·76	53	42·88	31·15		3	2·40	1·81	53	42·33	31·90
4	3·24	2·35	54	43·69	31·74		4	3·19	2·41	54	43·18	32·50
5	4·05	2·94	55	44·50	32·33		5	3·99	3·01	55	43·93	33·10
6	4·85	3·53	56	45·31	32·92		6	4·79	3·61	56	44·72	33·70
7	5·66	4·12	57	46·11	33·50		7	5·59	4·21	57	45·52	34·30
8	6·47	4·70	58	46·92	34·09		8	6·39	4·81	58	46·32	34·90
9	7·28	5·29	59	47·73	34·68		9	7·19	5·42	59	47·12	35·51
10	8·09	5·88	60	48·54	35·27		10	7·99	6·02	60	47·92	36·11
11	8·90	6·47	61	49·35	35·86		11	8·79	6·62	61	48·72	36·71
12	9·71	7·05	62	50·16	36·44		12	9·58	7·22	62	49·52	37·31
13	10·52	7·64	63	50·97	37·03		13	10·38	7·82	63	50·31	37·91
14	11·33	8·23	64	51·78	37·62		14	11·18	8·43	64	51·11	38·52
15	12·14	8·82	65	52·59	38·21		15	11·98	9·03	65	51·91	39·12
16	12·94	9·40	66	53·40	38·79		16	12·78	9·63	66	52·71	39·72
17	13·75	9·99	67	54·20	39·38		17	13·58	10·23	67	53·51	40·32
18	14·56	10·58	68	55·01	39·97		18	14·38	10·83	68	54·31	40·92
19	15·37	11·17	69	55·82	40·56		19	15·17	11·43	69	55·11	41·52
20	16·18	11·76	70	56·63	41·14		20	15·97	12·04	70	55·90	42·13
21	16·99	12·34	71	57·44	41·73		21	16·77	12·64	71	56·70	42·73
22	17·80	12·93	72	58·25	42·32		22	17·57	13·24	72	57·50	43·33
23	18·61	13·52	73	59·06	42·91		23	18·37	13·84	73	58·30	43·93
24	19·42	14·11	74	59·87	43·50		24	19·17	14·44	74	59·10	44·53
25	20·23	14·69	75	60·68	44·08		25	19·97	15·05	75	59·90	45·14
26	21·03	15·28	76	61·49	44·67		26	20·76	15·65	76	60·70	45·74
27	21·84	15·87	77	62·29	45·26		27	21·56	16·25	77	61·50	46·34
28	22·65	16·46	78	63·10	45·85		28	22·36	16·85	78	62·29	46·94
29	23·46	17·05	79	63·91	46·44		29	23·16	17·45	79	63·09	47·54
30	24·27	17·63	80	64·72	47·02		30	23·96	18·05	80	63·89	48·14
31	25·08	18·22	81	65·53	47·61		31	24·76	18·66	81	64·69	48·75
32	25·89	18·81	82	66·34	48·20		32	25·56	19·26	82	65·49	49·35
33	26·70	19·40	83	67·15	48·79		33	26·36	19·86	83	66·29	49·95
34	27·51	19·98	84	67·96	49·37		34	27·15	20·46	84	67·09	50·55
35	28·32	20·57	85	68·77	49·96		35	27·95	21·06	85	67·89	51·15
36	29·12	21·16	86	69·58	50·55		36	28·75	21·67	86	68·68	51·76
37	29·93	21·75	87	70·38	51·14		37	29·55	22·27	87	69·48	52·36
38	30·74	22·34	88	71·19	51·73		38	30·35	22·87	88	70·28	52·96
39	31·55	22·92	89	72·00	52·31		39	31·15	23·47	89	71·08	53·56
40	32·36	23·51	90	72·81	52·90		40	31·95	24·07	90	71·88	54·16
41	33·17	24·10	91	73·62	53·49		41	32·74	24·67	91	72·68	54·76
42	33·98	24·69	92	74·43	54·08		42	33·54	25·28	92	73·47	55·37
43	34·79	25·27	93	75·24	54·66		43	34·34	25·88	93	74·27	55·97
44	35·60	25·86	94	76·05	55·25		44	35·14	26·48	94	75·07	56·57
45	36·41	26·45	95	76·86	55·84		45	35·94	27·08	95	75·87	57·17
46	37·21	27·04	96	77·67	56·43		46	36·74	27·68	96	76·67	57·77
47	38·02	27·63	97	78·47	57·02		47	37·54	28·29	97	77·47	58·38
48	38·83	28·21	98	79·28	57·60		48	38·33	28·89	98	78·27	58·98
49	39·64	28·80	99	80·09	58·19		49	39·13	29·49	99	79·07	59·58
50	40·45	29·39	100	80·90	58·78		50	39·93	30·09	100	79·86	60·18
	E. or W.	N. or S.		E. or W.	N. or S.			E. or W.	N. or S.		E. or W.	N. or S.
	54°							53°				

38°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·79	0·62	51	40·19	31·40
2	1·58	1·23	52	40·98	32·01
3	2·36	1·85	53	41·76	32·63
4	3·15	2·46	54	42·55	33·25
5	3·94	3·08	55	43·34	33·86
6	4·73	3·69	56	44·13	34·48
7	5·52	4·31	57	44·92	35·09
8	6·30	4·93	58	45·70	35·71
9	7·09	5·54	59	46·49	36·32
10	7·88	6·16	60	47·28	36·94
11	8·67	6·77	61	48·07	37·56
12	9·46	7·39	62	48·86	38·17
13	10·24	8·00	63	49·61	38·79
14	11·03	8·62	64	50·43	39·40
15	11·82	9·23	65	51·22	40·02
16	12·61	9·85	66	52·01	40·63
17	13·40	10·47	67	52·80	41·25
18	14·18	11·08	68	53·58	41·86
19	14·97	11·70	69	54·37	42·48
20	15·76	12·31	70	55·16	43·10
21	16·55	12·93	71	55·95	43·71
22	17·34	13·54	72	56·74	44·33
23	18·12	14·16	73	57·52	44·94
24	18·91	14·78	74	58·31	45·56
25	19·70	15·39	75	59·10	46·17
26	20·49	16·01	76	59·89	46·79
27	21·28	16·62	77	60·68	47·41
28	22·06	17·24	78	61·46	48·02
29	22·85	17·85	79	62·25	48·64
30	23·64	18·47	80	63·04	49·25
31	24·43	19·09	81	63·83	49·87
32	25·22	19·70	82	64·62	50·48
33	26·00	20·32	83	65·40	51·10
34	26·79	20·93	84	66·19	51·72
35	27·58	21·55	85	66·98	52·33
36	28·37	22·16	86	67·77	52·95
37	29·16	22·78	87	68·56	53·56
38	29·94	23·40	88	69·34	54·18
39	30·73	24·01	89	70·13	54·79
40	31·52	24·63	90	70·92	55·41
41	32·31	25·24	91	71·71	56·03
42	33·10	25·86	92	72·50	56·64
43	33·88	26·47	93	73·28	57·26
44	34·67	27·09	94	74·07	57·87
45	35·46	27·70	95	74·86	58·49
46	36·25	28·32	96	75·65	59·10
47	37·04	28·94	97	76·44	59·72
48	37·82	29·55	98	77·22	60·33
49	38·61	30·17	99	78·01	60·95
50	39·40	30·78	100	78·80	61·57
	E. or W.	N. or S.		E. or W.	N. or S.

52°

39°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·78	0·63	51	39·63	32·09
2	1·55	1·26	52	40·41	32·72
3	2·33	1·89	53	41·19	33·35
4	3·11	2·52	54	41·97	33·98
5	3·89	3·15	55	42·74	34·61
6	4·66	3·78	56	43·52	35·24
7	5·44	4·41	57	44·30	35·87
8	6·22	5·04	58	45·07	36·50
9	6·99	5·66	59	45·85	37·13
10	7·77	6·29	60	46·63	37·76
11	8·55	6·92	61	47·41	38·39
12	9·33	7·55	62	48·18	39·02
13	10·10	8·18	63	48·96	39·65
14	10·88	8·81	64	49·74	40·28
15	11·66	9·44	65	50·51	40·91
16	12·43	10·07	66	51·29	41·53
17	13·21	10·70	67	52·07	42·16
18	13·99	11·33	68	52·85	42·79
19	14·77	11·96	69	53·62	43·42
20	15·54	12·59	70	54·40	44·05
21	16·32	13·22	71	55·18	44·68
22	17·10	13·84	72	55·95	45·31
23	17·87	14·47	73	56·73	45·94
24	18·65	15·10	74	57·51	46·57
25	19·43	15·73	75	58·29	47·20
26	20·21	16·36	76	59·06	47·83
27	20·98	16·99	77	59·84	48·46
28	21·76	17·62	78	60·62	49·09
29	22·54	18·25	79	61·39	49·72
30	23·31	18·88	80	62·17	50·34
31	24·09	19·51	81	62·95	50·97
32	24·87	20·14	82	63·73	51·60
33	25·65	20·77	83	64·50	52·23
34	26·42	21·40	84	65·28	52·86
35	27·20	22·03	85	66·06	53·49
36	27·98	22·66	86	66·83	54·12
37	28·75	23·29	87	67·61	54·75
38	29·53	23·91	88	68·39	55·38
39	30·31	24·54	89	69·17	56·01
40	31·09	25·17	90	69·94	56·64
41	31·86	25·80	91	70·72	57·27
42	32·64	26·43	92	71·50	57·90
43	33·42	27·06	93	72·27	58·53
44	34·19	27·69	94	73·05	59·16
45	34·97	28·32	95	73·83	59·78
46	35·75	28·95	96	74·61	60·41
47	36·53	29·58	97	75·38	61·04
48	37·30	30·21	98	76·16	61·67
49	38·08	30·84	99	76·94	62·30
50	38·86	31·47	100	77·72	62·93
	E. or W.	N. or S.		E. or W.	N. or S.

51°

40°

Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.
1	0·77	0·64	51	39·07	32·78
2	1·53	1·29	52	39·83	33·43
3	2·30	1·93	53	40·60	34·07
4	3·06	2·57	54	41·37	34·71
5	3·83	3·21	55	42·13	35·35
6	4·60	3·86	56	42·90	36·00
7	5·36	4·50	57	43·66	36·64
8	6·13	5·14	58	44·43	37·28
9	6·89	5·79	59	45·20	37·93
10	7·66	6·43	60	45·96	38·57
11	8·43	7·07	61	46·73	39·21
12	9·19	7·71	62	47·49	39·85
13	9·96	8·36	63	48·26	40·50
14	10·72	9·00	64	49·03	41·14
15	11·49	9·64	65	49·79	41·78
16	12·26	10·28	66	50·56	42·43
17	13·02	10·93	67	51·32	43·07
18	13·79	11·57	68	52·09	43·71
19	14·55	12·21	69	52·86	44·35
20	15·32	12·86	70	53·62	45·00
21	16·09	13·50	71	54·39	45·64
22	16·85	14·14	72	55·15	46·28
23	17·62	14·78	73	55·92	46·92
24	18·38	15·43	74	56·69	47·57
25	19·15	16·07	75	57·45	48·21
26	19·92	16·71	76	58·22	48·85
27	20·68	17·36	77	58·99	49·49
28	21·45	18·00	78	59·75	50·14
29	22·21	18·64	79	60·52	50·78
30	22·98	19·28	80	61·30	51·42
31	23·75	19·93	81	62·06	52·07
32	24·51	20·57	82	62·82	52·71
33	25·28	21·21	83	63·59	53·35
34	26·05	21·85	84	64·35	53·99
35	26·81	22·50	85	65·11	54·64
36	27·58	23·14	86	65·88	55·28
37	28·34	23·78	87	66·65	55·92
38	29·11	24·43	88	67·41	56·57
39	29·88	25·07	89	68·18	57·21
40	30·64	25·71	90	68·94	57·85
41	31·41	26·35	91	69·71	58·49
42	32·17	27·00	92	70·48	59·14
43	32·94	27·64	93	71·24	59·78
44	33·71	28·28	94	72·01	60·42
45	34·47	28·93	95	72·77	61·07
46	35·24	29·57	96	73·54	61·71
47	36·00	30·21	97	74·31	62·35
48	36·77	30·85	98	75·07	62·99
49	37·54	31·50	99	75·84	63·64
50	38·30	32·14	100	76·60	64·28
	E. or W.	N. or S.		E. or W.	N. or S.

50°

41°

Bearing Lengths.	N. or S. Distance.	E. or W. Distance.	Bearing Lengths.	N. or S. Distance.	E. or W. Distance.
1	0·75	0·66	51	38·49	33·46
2	1·51	1·31	52	39·24	34·12
3	2·26	1·97	53	40·00	34·77
4	3·02	2·62	54	40·75	35·43
5	3·77	3·28	55	41·51	36·08
6	4·53	3·94	56	42·26	36·74
7	5·28	4·59	57	43·02	37·40
8	6·04	5·25	58	43·77	38·05
9	6·79	5·90	59	44·53	38·71
10	7·55	6·56	60	45·28	39·36
11	8·30	7·22	61	46·04	40·02
12	9·06	7·87	62	46·79	40·68
13	9·81	8·53	63	47·55	41·33
14	10·57	9·18	64	48·30	41·99
15	11·32	9·84	65	49·06	42·64
16	12·08	10·50	66	49·81	43·30
17	12·83	11·15	67	50·57	43·96
18	13·58	11·81	68	51·32	44·61
19	14·34	12·47	69	52·07	45·27
20	15·09	13·12	70	52·83	45·92
21	15·85	13·78	71	53·58	46·58
22	16·60	14·43	72	54·34	47·24
23	17·36	15·09	73	55·09	47·89
24	18·11	15·75	74	55·85	48·55
25	18·87	16·40	75	56·60	49·20
26	19·62	17·06	76	57·36	49·86
27	20·38	17·71	77	58·11	50·52
28	21·13	18·37	78	58·87	51·17
29	21·89	19·03	79	59·62	51·83
30	22·64	19·68	80	60·38	52·48
31	23·40	20·34	81	61·13	53·14
32	24·15	20·99	82	61·89	53·80
33	24·91	21·65	83	62·64	54·45
34	25·66	22·31	84	63·40	55·11
35	26·41	22·96	85	64·15	55·77
36	27·17	23·62	86	64·91	56·42
37	27·92	24·27	87	65·66	57·08
38	28·68	24·93	88	66·41	57·73
39	29·43	25·58	89	67·17	58·39
40	30·19	26·24	90	67·92	59·05
41	30·94	26·90	91	68·68	59·70
42	31·70	27·55	92	69·43	60·36
43	32·45	28·21	93	70·19	61·01
44	33·21	28·87	94	70·94	61·67
45	33·96	29·52	95	71·70	62·33
46	34·72	30·18	96	72·45	62·98
47	35·47	30·83	97	73·21	63·64
48	36·23	31·49	98	73·96	64·29
49	36·98	32·15	99	74·72	64·95
50	37·74	32·80	100	75·47	65·61
	E. or W.	N. or S.		E. or W.	N. or S.

49°

42°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·74	0·67	51	37·30	34·13
2	1·49	1·34	52	38·04	34·79
3	2·23	2·01	53	38·39	35·46
4	2·97	2·68	54	40·13	36·13
5	3·72	3·35	55	40·87	36·80
6	4·46	4·01	56	41·62	37·47
7	5·20	4·68	57	42·36	38·14
8	5·95	5·35	58	43·10	38·81
9	6·69	6·02	59	43·85	39·48
10	7·43	6·69	60	44·59	40·15
11	8·17	7·36	61	45·33	40·82
12	9·92	8·03	62	46·07	41·49
13	9·66	8·70	63	46·82	42·16
14	10·40	9·37	64	47·56	42·82
15	11·15	10·04	65	48·30	43·49
16	11·89	10·71	66	49·05	44·16
17	12·63	11·38	67	49·79	44·83
18	13·38	12·04	68	50·53	45·50
19	14·12	12·71	69	51·28	46·17
20	14·86	13·38	70	52·02	46·84
21	15·61	14·05	71	52·76	47·51
22	16·35	14·72	72	53·51	48·18
23	17·09	15·39	73	54·25	48·85
24	17·84	16·06	74	54·99	49·52
25	18·58	16·73	75	55·68	50·19
26	19·32	17·40	76	56·48	50·85
27	20·06	18·07	77	57·22	51·52
28	20·81	18·74	78	57·96	52·19
29	21·55	19·40	79	58·71	52·86
30	22·29	20·07	80	59·45	53·53
31	23·04	20·74	81	60·19	54·20
32	23·78	21·41	82	60·94	54·87
33	24·52	22·08	83	61·68	55·54
34	25·27	22·75	84	62·42	56·21
35	26·01	23·42	85	63·17	56·88
36	26·75	24·09	86	63·91	57·55
37	27·50	24·76	87	64·65	58·21
38	28·24	25·43	88	65·40	58·88
39	28·98	26·10	89	66·14	59·55
40	29·73	26·80	90	66·88	60·22
41	30·47	27·43	91	67·63	60·89
42	31·21	28·10	92	68·37	61·56
43	31·95	28·77	93	69·11	62·23
44	32·70	29·44	94	69·85	62·90
45	33·44	30·11	95	70·60	63·57
46	34·18	30·78	96	71·34	64·24
47	34·93	31·45	97	72·08	64·91
48	35·67	32·12	98	72·83	65·57
49	36·41	32·79	99	73·57	66·24
50	37·20	33·50	100	74·31	66·91
	E. or W.	N. or S.		E. or W.	N. or S.

48°

43°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·73	0·68	51	37·30	34·78
2	1·46	1·36	52	38·03	35·46
3	2·19	2·05	53	38·76	36·15
4	2·93	2·73	54	39·49	36·83
5	3·66	3·41	55	40·23	37·51
6	4·39	4·09	56	40·96	38·19
7	5·12	4·77	57	41·69	38·87
8	5·85	5·46	58	42·42	39·56
9	6·58	6·14	59	43·15	40·24
10	7·31	6·82	60	43·88	40·92
11	8·04	7·50	61	44·61	41·60
12	8·78	8·18	62	45·34	42·28
13	9·51	8·87	63	46·08	42·97
14	10·24	9·55	64	46·81	43·65
15	10·97	10·23	65	47·54	44·33
16	11·70	10·91	66	48·27	45·01
17	12·43	11·59	67	49·00	45·69
18	13·16	12·28	68	49·73	46·38
19	13·90	12·96	69	50·46	47·06
20	14·63	13·64	70	51·19	47·74
21	15·36	14·32	71	51·93	48·42
22	16·09	15·00	72	52·66	49·10
23	16·82	15·69	73	53·39	49·79
24	17·55	16·37	74	54·12	50·47
25	18·28	17·05	75	54·85	51·15
26	19·02	17·73	76	55·58	51·83
27	19·75	18·41	77	56·31	52·51
28	20·48	19·10	78	57·05	53·20
29	21·21	19·78	79	57·78	53·88
30	21·94	20·46	80	58·51	54·56
31	22·67	21·14	81	59·24	55·24
32	23·40	21·82	82	59·97	55·92
33	24·13	22·51	83	60·70	56·61
34	24·87	23·19	84	61·43	57·29
35	25·60	23·87	85	62·16	57·97
36	26·33	24·55	86	62·90	58·65
37	27·06	25·23	87	63·63	59·33
38	27·79	25·92	88	64·36	60·02
39	28·52	26·60	89	65·09	60·70
40	29·25	27·28	90	65·82	61·38
41	29·99	27·96	91	66·55	62·06
42	30·72	28·64	92	67·28	62·74
43	31·45	29·33	93	68·02	63·43
44	32·18	30·01	94	68·75	64·11
45	32·91	30·69	95	69·48	64·79
46	33·64	31·37	96	70·21	65·47
47	34·37	32·05	97	70·94	66·15
48	35·10	32·74	98	71·67	66·84
49	35·84	33·42	99	72·40	67·52
50	36·57	34·10	100	73·14	68·20
	E. or W.	N. or S.		E. or W.	N. or S.

47°

44°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·72	0·69	51	36·69	35·43
2	1·44	1·39	52	37·41	36·12
3	2·16	2·08	53	38·13	36·82
4	2·88	2·78	54	38·84	37·51
5	3·60	3·47	55	39·56	38·21
6	4·32	4·17	56	40·28	38·90
7	5·04	4·86	57	41·00	39·60
8	5·75	5·55	58	41·72	40·29
9	6·47	6·25	59	42·44	40·99
10	7·19	6·95	60	43·16	41·68
11	7·91	7·64	61	43·88	42·37
12	8·63	8·34	62	44·60	43·07
13	9·35	9·03	63	45·32	43·76
14	10·07	9·73	64	46·04	44·46
15	10·79	10·42	65	46·76	45·15
16	11·51	11·11	66	47·48	45·85
17	12·23	11·81	67	48·20	46·54
18	12·95	12·50	68	48·92	47·24
19	13·67	13·20	69	49·63	47·93
20	14·39	13·89	70	50·35	48·63
21	15·11	14·59	71	51·07	49·32
22	15·83	15·28	72	51·79	50·02
23	16·54	15·98	73	52·51	50·71
24	17·26	16·67	74	53·23	51·40
25	17·98	17·37	75	53·95	52·10
26	18·70	18·06	76	54·67	52·79
27	19·42	18·76	77	55·39	53·49
28	20·14	19·45	78	56·11	54·18
29	20·86	20·15	79	56·83	54·88
30	21·58	20·84	80	57·55	55·57
31	22·30	21·53	81	58·27	56·27
32	23·02	22·23	82	58·99	56·96
33	23·74	22·92	83	59·71	57·66
34	24·46	23·62	84	60·42	58·35
35	25·18	24·31	85	61·14	59·05
36	25·90	25·01	86	61·86	59·74
37	26·62	25·70	87	62·58	60·44
38	27·33	26·40	88	63·30	61·13
39	28·05	27·09	89	64·02	61·82
40	28·77	27·79	90	64·74	62·52
41	29·49	28·48	91	65·46	63·21
42	30·21	29·18	92	66·18	63·91
43	30·93	29·87	93	66·90	64·60
44	31·65	30·57	94	67·62	65·30
45	32·37	31·26	95	68·34	65·99
46	33·09	31·96	96	69·06	66·69
47	33·81	32·65	97	69·78	67·38
48	34·53	33·34	98	70·50	68·08
49	35·25	34·04	99	71·21	68·77
50	35·97	34·73	100	71·93	69·47
	E. or W.	N. or S.		E. or W.	N. or S.

46°

45°

Bearing Lengths	N. or S. Distance	E. or W. Distance	Bearing Lengths	N. or S. Distance	E. or W. Distance
1	0·71	0·71	51	36·06	36·06
2	1·41	1·41	52	36·77	36·77
3	2·12	2·12	53	37·48	37·48
4	2·83	2·83	54	38·18	38·18
5	3·54	3·54	55	38·89	38·89
6	4·24	4·24	56	39·60	39·60
7	4·95	4·95	57	40·31	40·31
8	5·66	5·66	58	41·01	41·01
9	6·36	6·36	59	41·72	41·72
10	7·07	7·07	60	42·43	42·43
11	7·78	7·78	61	43·13	43·13
12	8·49	8·49	62	43·84	43·84
13	9·19	9·19	63	44·55	44·55
14	9·90	9·90	64	45·26	45·26
15	10·61	10·61	65	45·96	45·96
16	11·31	11·31	66	46·67	46·67
17	12·02	12·02	67	47·38	47·38
18	12·73	12·73	68	48·08	48·08
19	13·44	13·44	69	48·79	48·79
20	14·14	14·14	70	49·50	49·50
21	14·85	14·85	71	50·20	50·20
22	15·56	15·56	72	50·91	50·91
23	16·26	16·26	73	51·62	51·62
24	16·97	16·97	74	52·33	52·33
25	17·68	17·68	75	53·03	53·03
26	18·38	18·38	76	53·74	53·74
27	19·09	19·09	77	54·45	54·45
28	19·80	19·80	78	55·15	55·15
29	20·51	20·51	79	55·86	55·86
30	21·21	21·21	80	56·57	56·57
31	21·92	21·92	81	57·28	57·28
32	22·63	22·63	82	57·98	57·98
33	23·33	23·33	83	58·69	58·69
34	24·04	24·04	84	59·40	59·40
35	24·75	24·75	85	60·10	60·10
36	25·46	25·46	86	60·81	60·81
37	26·16	26·16	87	61·52	61·52
38	26·87	26·87	88	62·23	62·23
39	27·58	27·58	89	62·93	62·93
40	28·28	28·28	90	63·64	63·64
41	28·99	28·99	91	64·35	64·33
42	29·70	29·70	92	65·05	65·05
43	30·41	30·41	93	65·76	65·76
44	31·11	31·11	94	66·47	66·47
45	31·82	31·82	95	67·18	67·18
46	32·53	32·53	96	67·88	67·88
47	33·23	33·23	97	68·59	68·59
48	33·94	33·94	98	69·30	69·30
49	34·65	34·65	99	70·00	70·00
50	35·35	35·35	100	70·71	70·71
	E. or W.	N. or S.		E. or W.	N. or S.

45°

OF THE PRODUCE OF SEAMS OF COAL.

(61.) From the various experiments which have been made on the produce of tracts of coal mines, in the neighbourhood of Newcastle-upon-Tyne, it has been found that a cubic yard of coal weighs ·936 of a ton ; therefore, an acre of that stratum, 1 foot thick, will produce (if all wrought out) 1510 tons ; consequently an equal area of stratum, 2, 3, 4, &c., feet in thickness, will produce 2, 3, 4, &c., times the quantity of tons of coal that a seam of 1 foot thick will produce.

From this datum easy rules may be constructed for the use of the practical miner, which with facility may be retained for application in calculating the produce of seams of any given thickness in tons.

To find the number of tons of coal contained per acre by a seam of any given thickness.

RULE I.—Multiply 1510 by the thickness or height of the seam in feet, and the product will be the number of tons of coal contained in an acre of that seam.

To find the number of tons of coal produced per acre by a seam, where part thereof is only worked or taken away, the other part being left as a support to the roof.

RULE II.—As the sum of the two parts, *i.e.*, that left and that taken away, is to the part excavated or taken away, so is the whole number of tons contained in an acre of the seam to the number of tons produced per acre by the excavated part.

EXAMPLE I.—What number of tons of coal is contained in an acre of coal stratum 6 feet thick ?

From rule 1st, 1510 × 6 = 9060 tons, the content.

EXAMPLE II.—What number of tons of coal is contained in an area of coal stratum of 100 acres, 5 feet thick ?

1510 × 5 = 7550 tons contained in one acre.

Then 7550 × 100 = 755,000 tons contained in 100 acres.

EXAMPLE III.—What number of tons of coal is contained in 400 acres of coal stratum 5 feet 3 inches thick ?

First 5 ft. 3 in. $= \frac{21}{4}$ ft.

And $\frac{1510 \times 21 \times 400}{4} = 3,171,000$ tons.

EXAMPLE IV.—What number of tons of coal is contained in 400 acres of coal stratum 8 feet 4 inches thick ?

First 8 ft. 4 in. $= \frac{25}{3}$ ft.

And $\frac{1510 \times 25 \times 400}{3} = 5,033,333$ tons.

EXAMPLE V.—What number of tons of coal is contained in 500 acres of coal stratum 4 feet 9 inches thick, excluding a band of stone which lies therein 6 inches thick ?

4·75 − ·50 = 4·25 feet, the thickness of the coal stratum, exclusive of the band of stone.

Then 1510 × 4·25 × 500 = 3,208,750 tons contained in 500 acres.

EXAMPLE VI.—In a seam of coal which is 7 feet 3 inches thick ; that is to say, 6 feet of its thickness is marketable, and 1 foot 3 inches inferior; I wish to know the produce in tons per acre, both of the marketable and the inferior parts of the seam ?

1510 × 6 = 9060 tons per acre, the marketable produce of the seam

First 1 ft. 3 in. $= \frac{5}{4}$ ft.

And $\frac{1510 \times 5}{4} = 1887\frac{1}{2}$ tons of the inferior parts.

EXAMPLE VII.—In a seam of coal 6 feet thick, I wish to know what number of tons it produces per acre, when 1 part is taken away, and 2 left for pillars or supports ?

1510 × 6 = 9060 tons, the whole content per acre.

From rule 2nd, as $2 + 1 = 3 : 1 : : 9060 : 3020$ tons, the produce per acre of the part taken away.

EXAMPLE VIII.—In a seam of coal 3 feet 6 inches thick, I wish to know what number of tons it will produce per acre, when two parts are taken away and 1 left?

$1510 \times 3.5 = 5285$ tons, the content per acre.

As $2 + 1 = 3 : 2 : : 5285 : 3523.33$ tons, the produce per acre of the part taken away.

EXAMPLE IX.—In 1000 acres of coal 5 feet thick, whereof 2 parts are worked and 1 left, I wish to know how many years this stratum of coal will produce an annual quantity of 50,000 tons?

$1510 \times 5 = 7550$ tons, the whole produce of the seam per acre.

Then as $3 : 2 : : 7550 : 5033$, the quantity got per acre.

And $\dfrac{5033 \times 1000}{50,000} = 100.66$ years.

EXAMPLE X.—I have a tract of 600 acres of coal stratum, containing 2 seams, the first 5 feet 3 inches thick, and the second 3 feet 6 inches thick: Out of the first seam 3 parts are got and 1 left; and out of the second 4 parts are got and 1 left. Now, if the annual vend of the two seams together is 75,000 tons, what number must be wrought out of each seam yearly, so that they may terminate together; and how many years will the colliery last?

$\dfrac{1510 \times 21}{4} = 7927\frac{1}{2}$ tons, the whole produce per acre of the first seam.

And $4 : 3 : : 7927\frac{1}{2} : 5945$ tons, the quantity wrought per acre out of the first seam.

Then $5945 \times 600 = 3,567,000$ tons, total produce of the first seam.

Again, $\dfrac{1510 \times 7}{2} = 5285$ tons, the whole produce per acre of the second seam.

And $5 : 4 : : 5285 : 4228$ tons, the quantity wrought per acre out of the second seam.

Then $4228 \times 600 = 2,536,800$ tons, total produce of the second seam.

Now, to make the two seams terminate together, the quantity wrought out of each seam annually must bear the same proportion to each other as the quantity wrought out of each acre of each seam.

Therefore $5945 + 4228 = 10,173 : 5945 : : 75,000 :$ $43,829$ tons, the quantity to be wrought out of the first seam annually.

And $75000 - 43829 = 31,171$ tons, the quantity to be wrought out of the second seam annually.

Whence $\dfrac{3567000 + 2536800}{75000} = 80$ years 18 days, the duration of the colliery.

Note.—Elaborate statistics and details of the extent, the probable produce and duration of all the coal-fields in the United Kingdom, also the extent and thickness of the strata of those of the United States and the British colonies, as far as they are known ; as well as those of Belgium, France, Germany, and other foreign countries, are given in the *Reports of the Institution of Mining Engineers of Newcastle-upon-Tyne*, to which the student is referred, who may be desirous to be acquainted with these subjects.

Questions in Mine Surveying.

Note.—The solutions to the two following Questions in Mine Surveying will require a knowledge of the application of Algebra to Geometry, and the latter of the two will require a further knowledge of the application of Spherical Trigonometry to Astronomy. See *Question XVII, page* 211, *Baker's Land and Engineering Surveying. Weale's Series.* The student will have no difficulty in sketching the figures and assigning the dimensions to the given parts in the two Questions.

Question 1.—There are four drifts in a coal mine forming a trapezium, the given lengths of which are $a, b, c, d,$ and the sums of the opposite angles of the trapezium are known to be equal to two right angles, none of the angles being separately given. It is required to plot this subterraneous survey by the help of the following formula.

Let S = half the sum of the lengths of the four drifts = $\frac{1}{2}$ (*a* + *b* + *c* + *d*), and D the diameter of circle, which will circumscribe the trapezium ; then

$$D = \sqrt{\left\{ \frac{(ac + bd)\ (ab + cd)\ (ad + bc)}{(S-a)\ (S-b)\ (S-c)\ (S-d)} \right\}}$$

Note.—This formula will divest the preceding Question of its chief difficulty, while it will accustom the student to the application of this species of mathematical analysis.

Question 2.—There are five straight drifts, AB, BC, CD, DE, EA, in a coal-mine, forming an irregular polygon ; now, the several lengths of each of the five drifts are given, and the angles at B, C, and D are known to be equal to one another, but are not given : also at each of the angles B and D is a shaft, and the tops of these two shafts range with the sun at 3 h. 35′ P.M. on the 22d of October, 1860. It is required from these data to plot this subterraneous survey in its true position with respect to the cardinal points.

NOTE.—This question was proposed by B. Gompertz, Esq., F.R.S., in the *Gentleman's Mathematical Companion*; to which he gave a solution in a concise, novel, and ingenious manner by his *Principles of Imaginary Quantities*: other-solutions by the ordinary methods were also given to the same problem.

THE END.

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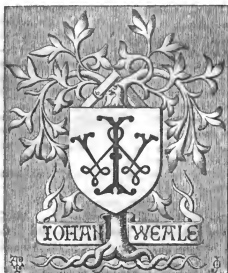
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